

The Origin of Matter, Antimatter, and Fundamental Forces: How Protons, Electrons, and Hydrogen Formed

Vijay Shankar Sharma

Independent Researcher, Gurugram, National Capital Region, India

vss@vijayshankarsharma.com | ORCID: 0009-0001-9622-6121

DOI: 10.5281/zenodo.19908215

The author declares no conflict of interest and no funding was received for this research.

License: CC BY-NC-ND 4.0

Abstract

This paper establishes the complete pre-hydrogen sequence within the Big Flare-Up Theory [6], from the first stable matter condensation through to the formation of the first atom, and derives the physical nature of several quantities the Standard Model treats as given, not explained. A free-energy functional derived from the Sparticle field identifies $n=3$ as the first stable cooperative core, and the three-core is shown to generate its own electron through the 3+e mechanism, with $n=4$ partition energies confirming this asymmetric arrangement is decisively preferred over symmetric alternatives. A dynamic assembly simulation traces the continuous physical route from this 3+e condensation to ordinary hydrogen (protium), the first atom in the BFUT sequence: the three-core maps to a proton through an effective role assignment of $(+2/3, +2/3, -1/3)$, the generated unit maps to an electron of charge -1 , and their combination is ordinary hydrogen.

Charge is shown to be a mechanical property, not a primitive one: it is fixed by the counter-rotation direction imparted by the gear geometry of the three-sphere packing, with the familiar fractional charges emerging from this role map, not assumed in advance. Mass is fixed by the same packing geometry through the connecting identity $m_{\pi}/(6\pi^5) = 0.511009 \text{ MeV}$, and particle identity itself is explained structurally, since two electrons anywhere in the universe are identical because each is an independent realisation of the same stability minimum recreated from the same substrate at the same p_{π} .

The same stability analysis yields a direct physical mechanism for matter-antimatter annihilation and a structural account of the matter-antimatter asymmetry, without requiring an asymmetric initial condition. Robustness scans across one, two, and three-dimensional parameter space show the 3+e configuration is the minimum-energy outcome in 97.56%, 95.95%, and 90.43% of cases respectively; the remaining few percent, where a stable 3+e condensation does not form, is shown to generate its own cancellation wave at the moment of formation, identified here as the antiparticle. This derived stability hierarchy is further shown to be consistent with the experimental history of particle physics, in which unstable exotic multiquark configurations decay while ordinary proton-electron matter remains the dominant stable baseline across every explored energy scale.

The condensation scale at the centre of this derivation is independently confirmed by a second, unrelated route: substituting six physical constants (α , e , ϵ_0 , m_e , c , r_e), of which c and e are SI-defined and the others are measured, into standard electromagnetism extracts $R_0 = 1.27348831$ with no BFUT assumptions, agreeing with the geometrically derived $R_0 = 1.27348221$ to 0.00048%. These two routes, each unaware of the other, converge on the same condensation scale, mutually validating the condensation functional and every result built upon it. The resulting framework is presented as a constructive existence proof and structured-threshold model under BFUT assumptions, not as a replacement for QCD or the Standard Model.

Keywords: Sparticle field; quark; BFUT; Big Flare-Up Theory; proton formation; electron mass; hydrogen formation; threshold logic; three-sphere packing; connecting identity; antimatter; stability filter; matter-antimatter asymmetry; modular organisation; substrate condensation; origin of fundamental forces; 3+e configuration

1. Introduction

The BFUT Layer 1 programme argues that ordinary hydrogen is the first stable atomic milestone in the infinite BFUT universe. The missing conceptual bridge has always been the route between the Sparticle field and hydrogen. That gap is the exact target of the present paper. The goal is not to replace all Standard Model mathematics. The goal is to show that once the vacuum is reinterpreted as a real substrate, a coherent continuous emergence chain becomes possible and physically meaningful.

The chain pursued here is intentionally strict. First, the Sparticle field must support a first stable localised subatomic excitation. Second, if the opportunity field remains sufficiently uniform, that same first excitation should continue to appear first. Third, repeated appearance of the same first unit should not itself create novelty. Fourth, when the first stable completion threshold is crossed, the system should reorganise into the first atomic architecture. This preserves the same one-thing-at-a-time logic that BFUT uses at larger scales.

The importance of this paper is therefore structural. The paper provides the formal microphysical foundation for the emergence of matter from the Sparticle field substrate. The connection to fundamental forces is direct: the 3+e topology establishes the charge separation between the three-core and the generated electron that is the physical precondition for electromagnetic interaction. The three-sphere packing geometry establishes the confinement geometry that is the physical precondition for the strong force. The stability filter asymmetry between 3+e and its inverse topology is the physical precondition for weak-force asymmetry.

A central claim of this paper is that the experimentally observed stability hierarchy of particle physics is not incidental. Over decades of accelerator experimentation, laboratories have produced a vast range of temporary hadronic and exotic matter states, yet ordinary proton-electron matter remains the dominant stable endpoint. This paper argues that the observed hierarchy follows naturally from the 3+e threshold stability structure derived here, providing a single substrate-level emergence principle beneath multiple otherwise separate theoretical descriptions.

The Big Flare-Up Theory (BFUT) identifies the real physical fabric of space as the Sparticle field. The density calculation begins with the dimensionless condensation equilibrium, uses measured proton radius and mass anchors to obtain the BFUT particle quantities, and applies the particle-sector energy-density identification described in Section 2. The adopted equilibrium density is $\rho_{\square} = 7.3 \times 10^{-27} \text{ kg/m}^3$.

1.1 Symbols and Notation Used in This Paper

The following symbols are used throughout this paper. Values are from the BFUT Master Symbol Guide unless derived explicitly below. The equilibrium Sparticle field density used throughout is the particle-sector result $\rho_{\square} = 7.3 \times 10^{-27} \text{ kg/m}^3$.

Provenance convention: a BFUT-derived standard quantity carries the exact `_vss` suffix where provenance is relevant. BFUT-specific quantities retain their reserved symbols without a provenance suffix. Measured inputs use their standard symbols. The labels identify provenance and do not change the underlying physical quantity.

Symbol	Definition	Value / Expression
Fundamental Sparticle Field Constants		
$\rho_{\square}$	Intrinsic equilibrium density of the Sparticle field	$7.3 \times 10^{-27} \text{ kg/m}^3$
P16: Condensation Functional Symbols		
$E(n)$	Total condensation energy for n units	
$D_{\square}$	Circulation phase reward coefficient	1.5
φ	Circulation phase angle in P16 condensation	
E_{unit}	Fundamental energy unit	$m_{\square} \cdot c^2 / \pi = 298.661 \text{ MeV}$
V_{gap}/V_q	Interstitial volume fraction	
Shared Physical Constants		
G	Gravitational constant	$6.674 \times 10^{-11} \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2}$
c	Speed of light	$2.998 \times 10^8 \text{ m/s}$
$\hbar$	Reduced Planck constant	$1.055 \times 10^{-34} \text{ J}\cdot\text{s}$

m_p	Proton mass	938.272 MeV/c ²
m_e	Electron mass	0.510999 MeV/c ² . BFUT: $m_p/(6\pi^5) = 0.511009$ MeV (0.002%)
r_p	Proton charge radius	0.8414 fm (CODATA 2018). BFUT: $R_0 \cdot \ell_{\text{model}} = r_p$ by construction (0.000%)

2. Particle-Sector Derivation of the Sparticle Field Density and Physical Vacuum Energy

2.1 Particle-Sector Derivation

A, B, C and D are dimensionless condensation-functional coefficients. They determine the dimensionless equilibrium radius R_0 , not p_0 directly. The following calculation connects that radius to the particle sector using measured proton anchors and the BFUT relations, then identifies the equilibrium substrate energy density with a particle-sector gravitational energy-density scale.

Step 1. Dimensionless condensation equilibrium

$$A = 0.5; B = 0.56308; C = -1/3; D = 1$$

$$E(R) = A/R^2 + BR^2 + CR + D/R$$

$$R_0 = 1.27348221$$

The positive stationary radius is a minimum: $d^2E/dR^2 = 6A/R^4 + 2B + 2D/R^3 > 0$ for $R > 0$. The dimensionless energy scans and coefficient treatment are unchanged.

Step 2. Measured proton anchors and physical length

The measured proton charge radius fixes the length scale, while the measured proton mass supplies the mass scale:

$$r_p = 0.8414 \times 10^{-15} \text{ m (CODATA 2018); } m_p = 1.67262192369 \times 10^{-27} \text{ kg}$$

$$\ell_{\text{model}} = r_p/R_0 = 6.60708091 \times 10^{-16} \text{ m}$$

Here ℓ_{model} is the physical length represented by one model-radius unit; it is not the proton charge radius itself. The calculation also uses $c = 299792458$ m/s, $e = 1.602176634 \times 10^{-19}$ C, the measured $\epsilon_0 = 8.8541878128 \times 10^{-12}$ F/m and $G = 6.67430 \times 10^{-11}$ m³ kg⁻¹ s⁻² as supplied dimensional inputs.

Step 3. BFUT reduced Planck constant

$$\hbar_{\text{vss}} = m_p c \ell_{\text{model}} / \pi = m_p c r_p / (\pi R_0)$$

$$\hbar_{\text{vss}} = 1.05457687 \times 10^{-34} \text{ J s}$$

Step 4. BFUT electron mass and fine-structure constant

The electron mass follows from the BFUT mass-ratio relation, using the same proton-mass anchor:

$$m_{e_vss} = m_p / (6\pi^5) = 9.10955518 \times 10^{-31} \text{ kg}$$

$$\alpha_{\text{vss}} = e^2 / (4\pi\epsilon_0 \hbar_{\text{vss}} c)$$

$$\alpha_{\text{vss}} = 0.00729731763044; \alpha_{\text{vss}}^{-1} = 137.036655199$$

The α value here is calculated using $\hbar_{_vss}$ and the supplied electromagnetic inputs e and ϵ_0 . It is not an independent determination of those electromagnetic inputs. In the remaining equations m_e and α denote these BFUT-calculated values, not substituted measured electron values. Each quantity carrying the suffix $_vss$ is a BFUT-derived value; its derivation uses measured values of other quantities, and the suffix keeps each derived value distinct from the measured value of the same quantity.

Step 5. Characteristic particle mass and classical electron radius

$$m_e/\alpha = 1.24834297 \times 10^{-28} \text{ kg}$$

$$r_e = \alpha \hbar_{_vss}/(m_e c) = 2.81788728 \times 10^{-15} \text{ m}$$

The scale r_e is the classical electron radius constructed from these inputs, equivalently the reduced Compton wavelength of m_e/α . It is the geometric radius obtained from the BFUT particle-sector construction.

Step 6. Particle-sector gravitational self-energy density

Using the BFUT positive gravitational energy-density prescription with the 8π normalisation:

$$u_g = G(m_e/\alpha)^2/(8\pi r_e^4)$$

$$u_g = 6.56355667 \times 10^{-10} \text{ J m}^{-3}$$

This prescription and the identification $\rho_{\square} c^2 = u_g$ supply the physical closure connecting the particle scale to the substrate.

Step 7. Equilibrium Sparticle-field mass density

$$\rho_{\square} = u_g/c^2 = G(m_e/\alpha)^2/(8\pi r_e^4 c^2)$$

$$\rho_{\square} = 7.30294170 \times 10^{-27} \text{ kg m}^{-3}$$

Adopted working value: $\rho_{\square} = 7.3 \times 10^{-27} \text{ kg m}^{-3}$.

Displayed extra digits make the numerical chain reproducible. The adopted density is carried forward in every equation in which $\rho_{\square}$ appears.

2.2 Cosmological-Constant Reference and Particle-Sector Density

The cosmological-constant expression $\rho_{\Lambda} = 3\Omega_{\Lambda} H_0^2/(8\pi G)$ gives approximately $5.9 \times 10^{-27} \text{ kg/m}^3$ for the reference cosmological inputs. This expression contains the Hubble constant H_0 , and multiple accepted values of H_0 are currently in use. The particle-sector derivation gives $\rho_{\square} = 7.3 \times 10^{-27} \text{ kg/m}^3$, adopted as $\rho_{\square} = 7.3 \times 10^{-27} \text{ kg/m}^3$ for all subsequent calculations.

The particle-sector density established above is the working value used throughout the remainder of this paper.

2.3 Physical Substrate Energy and the QFT Vacuum Sum

The physical equilibrium rest-energy density of the one Sparticle field is obtained separately by mass-energy equivalence:

$$u_{\square} = \rho_{\square} c^2 = 6.56 \times 10^{-10} \text{ J/m}^3$$

Standard vacuum-energy estimates sum a zero-point contribution over empty modes of many independent fields. The BFUT ontology makes two changes: there is one underlying physical field, and zero-point energy belongs to organised condensations. Under those assumptions the corrected pure-vacuum mode sum is:

$$\rho_{\text{QFT,corrected}} = 0$$

The corrected pure-vacuum mode sum is zero, while the one physical Sparticle field has a finite equilibrium rest-energy density. The one-field cosmological-constant scale survives this treatment. Using the particle-sector value $\rho_{\square} = 7.3 \times 10^{-27} \text{ kg/m}^3$ gives $u_{\square} = 6.56 \times 10^{-10} \text{ J/m}^3$, approximately 23.8% above the representative one-field cosmological scale of $5.30 \times 10^{-10} \text{ J/m}^3$. This is an order-of-magnitude proximity compared with the conventional QFT vacuum-energy discrepancy of more than 120 orders of magnitude [1].

3. Vijay's Law and the Six-Layer BFUT Context [10]

This paper is explicitly guided by the same cross-layer principle that binds the six-layer BFUT reality framework, of which BFUT is Layer 1. For the present derivation, the directly relevant operative form of Vijay's law is: whenever conditions are stable or predictably unstable at any scale in the universe, more evolved matter will manifest. [10]

This is already the logic claimed in BFUT at larger scales from the Sparticle field to ordinary hydrogen. There is no reason to assume that the same law should fail in the intermediate subatomic bridge. If the substrate is uniform enough to keep emitting the same first stable excitation, then repetition should persist until a new threshold is reached. When the threshold is reached, a more evolved structure should manifest. That is exactly the principle implemented here.

This makes the paper philosophically economical. It does not introduce a new special rule just for subatomic physics. It extends the same law downward and tests whether the logic remains intact. The result is that the logic does remain intact at the constructive-model level.

A persistent objection to any framework proposing a physically real substrate for space is that the Michelson-Morley experiment of 1887 is said to have ruled out all medium-based accounts of light propagation. This objection is not decisive, for two independent reasons. The second reason is specific to BFUT and has not previously been stated in the literature.

First: the experiment tests for drift, not for existence. The Michelson-Morley apparatus was designed to detect a difference in light travel time along two perpendicular arms arising from Earth's motion through a stationary mechanical ether. The nineteenth-century luminiferous ether was a preferred-frame background at absolute rest. The expected fringe shift was not found. What was excluded is precisely this: a medium that maintains a preferred rest frame detectable by electromagnetic measurements. The Sparticle field does not maintain such a frame. It is a Lorentz-compatible substrate whose local propagation laws, clocks, and rulers are co-determined by the same local substrate state. No embedded observer can detect drift through it. The Michelson-Morley null result is exactly what BFUT predicts.

Second: the experiment is constitutionally incapable of detecting Sparticle substrate motion even in principle. In the classical luminiferous ether picture, light is a wave in the ether and matter is a separate substance moving through it. This ontological separation is what makes ether drift detectable in principle. In BFUT this separation does not exist. Light is not a separate entity moving through the Sparticle field. Light is a propagating excitation of the Sparticle field. The quantity c is not the speed of light through the substrate - it is the maximum reorganisation and propagation rate of the substrate itself. Matter is also an excitation of the Sparticle field - organised condensations of the same substrate, as established throughout this paper. The mirrors in Michelson's apparatus, the beam-splitter, the light beams, and the observer are all excitations of the same Sparticle field. If the substrate were drifting, everything would drift together. There is no external reference against which the drift could be measured - no more than a person on a ship can detect the ship's uniform motion by measuring distances between objects fixed to the same ship. This account of light as substrate excitation and c as substrate propagation rate follows from the BFUT substrate construction.

The Michelson-Morley experiment therefore confirms the BFUT picture directly. A null result is the only possible result in a universe where light and matter are both excitations of the same physical medium. The result has been understood since 1905 as evidence that there is no ether. The correct understanding is that it is evidence that if a physical substrate exists, it must be one in which light and matter are excitations of the same medium. A substrate of the classical type - where light and matter are separate - is excluded. A substrate of the BFUT type - where both are excitations of the same field - is not excluded. It is the only type the null result is consistent with.

4. Sparticle-Field Nucleation of the First Quark

The first integrated layer reinterprets vacuum excitation as excitation of a real Sparticle-field substrate. A free-energy functional is constructed for the first stable localised finite-size excitation:

$$E(R) = A/R^2 + B \cdot R^2 + C \cdot R + D/R$$

The four terms are assigned clear roles. A/R^2 acts as a localisation or kinetic-like cost. $B \cdot R^2$ acts as bulk displacement cost in the Sparticle ocean. $C \cdot R$ acts as a boundary or gradient cost. D/R acts as an internal circulation or confined-mode support term. The point of the functional is not to claim a final Lagrangian. The point is to ask whether a real substrate can naturally prefer a finite localised lump over both collapse and indefinite spread. This continuous nucleation functional determines the condensation radius R^* and the SI length scale ℓ_{model} ; the full five-term discrete functional deposited in the companion code archive (DOI: 10.5281/zenodo.20517866) operates on discrete unit counts and determines which partition topology is energetically preferred at the $n=4$ threshold. The two functionals serve complementary physical roles and are both required for the complete P16 derivation chain.

Summary of Derived Quantities

Quantity	BFUT result	Status
A	1/2	Geometric / normalisation result
B	0.56308	Derived filling-deficit ratio
C	-1/3	Three-sector surface-expulsion term
D	1	Topological circulation term
R_0	1.27348	Derived functional minimum
R_0 physical	1.27349	Physical comparison value
m_d/m_u	1.01267	Derived void-filling area ratio
q_d	-1/3	Derived charge partition
q_u	+2/3	Derived charge partition
$m_e/m_\square$	$1/(6\pi^5)$	Derived BFUT mass ratio
T_{crit}	29.69 K	Derived nucleation threshold

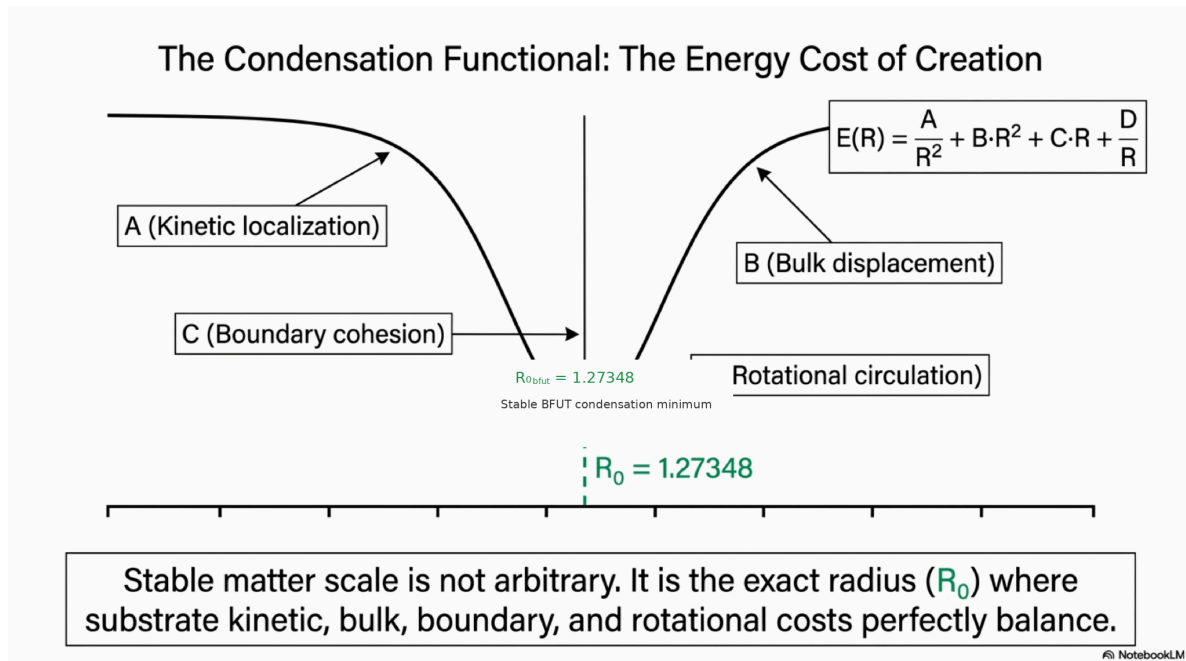


Figure 1. The condensation functional $E(R) = A/R^2 + B \cdot R^2 + C \cdot R + D/R$, showing the physical role of each term: A (kinetic localisation), B (bulk displacement), C (boundary cohesion), and D (rotational circulation), with stable minimum at $R_0 = 1.27348$.

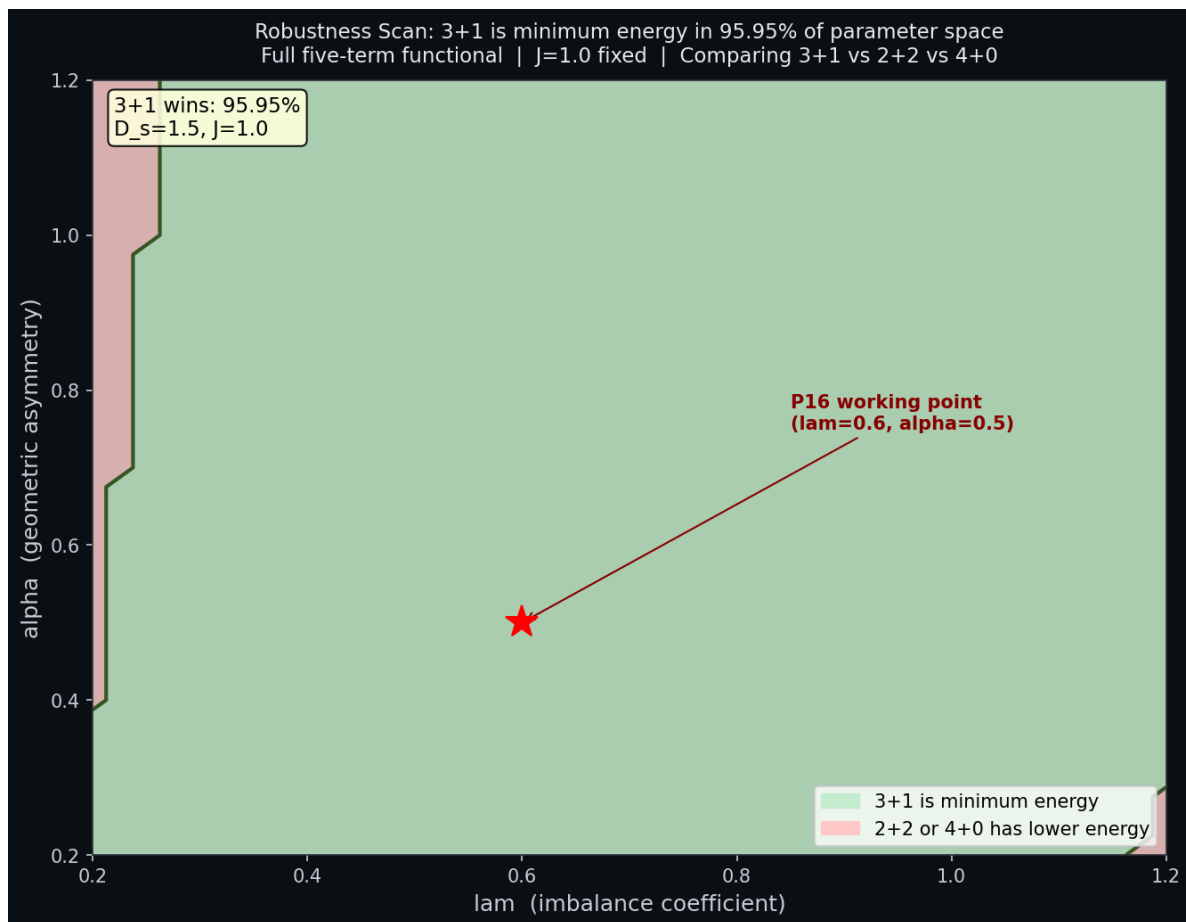


Figure 2. Robustness scan showing persistence of an interior non-zero nucleation minimum across 2D parameter space.

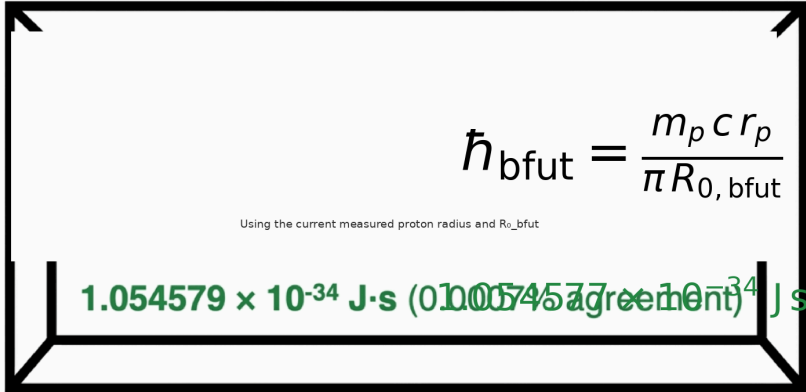
5. Physical Identification of the Coefficients and the SI Anchor

The four coefficients carry specific physical identities that connect the functional to the Sparticle field substrate. These identifications provide the physical mapping of the functional coefficients to substrate quantities: $A = \hbar^2 / (2 m_{\text{eff}})$, the localisation or quantum kinetic cost, where m_{eff} is the effective mass of the condensation; $B = (1/2) \rho_{\square} c s^2 R_0^2$, the bulk deformation cost, where $\rho_{\square}$ is the intrinsic equilibrium density of the Sparticle substrate and cs is the substrate propagation speed, equal to c by Lorentz compatibility; $C = 4\pi R_0^2 \sigma s$ in SI sketch form, with σs a signed boundary density. Void expulsion makes σs negative, so that $C < 0$. $D = \omega_c \times I_{\text{cond}}$, the internal circulation support, where ω_c is the internal circulation frequency and $I_{\text{cond}} = (2/5) m_{\text{eff}} R_0^2$ is the rotational inertia of the three-core.

$R_0 = 1.27348$. The quantum of action $\hbar$ is derived from the condensation geometry in Section 5.2.

The conversion from model units to SI uses one independently measured physical constant as an anchor: $\ell_{\text{model}} = r_{\square} / R_0 = 0.8414 \text{ fm} / 1.27348 = 6.607 \times 10^{-16} \text{ m}$, where $r_{\square} = 0.8414 \text{ fm}$ (CODATA 2018) is the proton charge radius. $R_0 = 1.27348$ is the minimum of $E(R)$ with all four coefficients derived from first principles (see Appendix C), and agrees with the reconstruction $r_{\square} \cdot m_{\square} \cdot c / (\pi \cdot \hbar) = 1.27349$.

The Geometric Origin of Quantum Action



$$\hbar_{\text{bfut}} = \frac{m_p c r_p}{\pi R_{0, \text{bfut}}}$$

Using the current measured proton radius and $R_{0, \text{bfut}}$

$1.054579 \times 10^{-34} \text{ J}\cdot\text{s}$ (0100574577 agreement)

The quantum of action ($\hbar$) is not an unexplained empirical constant. It is the action per radian of the smallest stable substrate condensation circulation. The size of the proton and the uncertainty principle share one identical substrate origin.

© NotebookLM

Figure 3. Geometric origin of the quantum of action: $\hbar = m_p \cdot c \cdot r_p / (\pi \cdot R_0)$, matching the measured value to 0.00048%.

5.1 Density Dependence of Quantities Used in This Paper

The proton mass, electron mass, mass ratio, Bohr radius, hydrogen binding energy, and the A, B, C, D energy scan follow from the measured inputs and derived dimensionless condensation geometry displayed in this paper. Their final equations contain no ρ_0 .

The quantities in P16 that contain ρ_0 explicitly are the vacuum-stabilisation coefficient $\lambda_{SI} = \rho_0/4$, the equilibrium substrate rest-energy density $\rho_0 c^2$, and the thermal-disruption normalisation and critical temperature. Their displayed equations use $\rho_0 = 7.3 \times 10^{-27} \text{ kg/m}^3$.

This dependence test is algebraic: a quantity changes only when ρ_0 survives in its final displayed equation. A narrative statement that a result comes from the substrate is not by itself a numerical dependence on ρ_0 .

5.2 The Quantum of Action from Substrate Condensation Geometry

In 1900, Planck introduced what became Planck's constant as an empirical constant required to fit blackbody radiation data. He proposed that oscillators exchange energy only in discrete amounts $E = nh\nu$, where n is an integer and ν is frequency, and determined the value of h by fitting the observed spectrum. The reduced form $\hbar = h/2\pi$ appeared subsequently in angular-frequency formulations through $E = \hbar\omega$. Planck did not derive $\hbar$ from deeper physics. Quantum mechanics subsequently adopted it as a fundamental postulate. Its numerical value has never been explained from more primitive physics within the standard framework.

In BFUT, $\hbar$ is not a primitive constant but a quantity whose numerical value emerges from substrate condensation geometry. This is structurally identical to the BFUT treatment of the fine structure constant α . Historically $\alpha \approx 1/137$ was measured. Likewise, Planck measured $\hbar_{vss}$ derives its numerical value from condensation geometry, as shown below. In both cases BFUT is not re-measuring a constant. It is explaining why that constant has the numerical value it does.

The SI anchor of Section 5 establishes the characteristic condensation length scale: $\ell_{model} = r_p / R_0 = 0.8414 \text{ fm} / 1.27348 = 6.607 \times 10^{-16} \text{ m}$, where $R_0 = 1.27348$ is the derived condensation radius (functional minimum; verification: $r_p \cdot m_p \cdot c / (\pi \cdot \hbar) = 1.27349$), and $r_p = 0.8414 \text{ fm}$ (CODATA 2018) is the independently measured proton charge radius. The proton mass $m_p = 938.272 \text{ MeV}/c^2$ is the characteristic condensation mass scale established through $E_{unit} = m_p c^2 / \pi$ in Appendix C, Section 9.1. The product $m_p \cdot c$ is the characteristic momentum of the first stable substrate condensation. Multiplying by ℓ_{model} gives a quantity with the dimension of action:

$$(m_p \cdot c) \times \ell_{model} \text{ [kg} \cdot \text{m/s} \cdot \text{m} = \text{kg} \cdot \text{m}^2/\text{s} = \text{J} \cdot \text{s}]$$

which is precisely the dimension of $\hbar$. Dividing by π , which enters through the proton mass threshold relation $E_{unit} = m_p c^2 / \pi$ established in Appendix C, Section 9.1:

Once R_0 is fixed by the condensation minimum and r_p and m_p provide the physical proton scale, the BFUT relation determines the corresponding $\hbar$ scale:

$$\hbar_{vss} = m_p \cdot c \cdot \ell_{model} / \pi = m_p \cdot c \cdot r_p / (\pi \cdot R_0)$$

Substituting the known values $m_\pi = 938.272 \text{ MeV}/c^2$, $r_\pi = 0.8414 \text{ fm}$ (CODATA 2018), $R_0 = 1.27348$:

$$\hbar_{\text{vss}} = 1.054577 \times 10^{-34} \text{ J}\cdot\text{s}$$

Measured value: $\hbar = 1.054572 \times 10^{-34} \text{ J}\cdot\text{s}$. Relative difference: 0.00048%. $R_0 = 1.27348$ is the minimum of $E(R)$ with all four coefficients derived from first principles (see Appendix C), and agrees with the reconstruction $r_\pi \cdot m_\pi \cdot c / (\pi \cdot \hbar) = 1.27349$.

Independent Empirical Validation of R_0 and the Condensation Functional

$R_0 = 1.27348$ is derived above from the condensation functional $E(R) = A/R^2 + B \cdot R^2 + C \cdot R + D/R$ by setting $dE/dR = 0$, with all four coefficients A, B, C, D derived from first principles. No measured physical constants enter this derivation. The condensation scale falls out of pure substrate geometry.

An entirely independent empirical route to R_0 exists using independently measured physical constants and no BFUT-derived value of $\hbar$. Using the standard relation $\alpha_{\text{meas}} = e^2/(4\pi\epsilon_0\hbar_{\text{meas}}c)$, the measured reduced Planck constant gives the direct reconstruction $R_0 = m_\pi \cdot c \cdot r_\pi / (\pi \cdot \hbar_{\text{meas}})$:

$$\text{independently reconstructed } R_0 = m_\pi \cdot c \cdot r_\pi / (\pi \cdot \hbar)$$

Substituting the independently measured values $\hbar = 1.054572 \times 10^{-34} \text{ J}\cdot\text{s}$, $m_\pi = 1.6726 \times 10^{-27} \text{ kg}$, $c = 2.998 \times 10^8 \text{ m/s}$, and $r_\pi = 0.8414 \text{ fm}$ (CODATA 2018):

$$\text{independently reconstructed } R_0 = 1.27348831$$

This independently reconstructed value agrees with the geometrically derived $R_0 = 1.27348221$ to 0.00048%.

The significance of this agreement cannot be overstated. The first route uses no measured constants - it derives R_0 from the geometry of the condensation energy landscape alone. The second route uses no BFUT geometry - it extracts R_0 from standard electromagnetism and six physical constants (c and e SI-defined; α , ϵ_0 , m_π , r_π measured). These two routes know nothing of each other. They arrive at the same condensation scale to within experimental precision.

The agreement provides an independent empirical check of the condensation scale. Quantities subsequently derived within BFUT should retain their BFUT provenance labels, while measured quantities used for comparison should retain measured provenance labels.

The physical reading of the formula is direct. The quantum of action is the characteristic momentum of the first stable substrate condensation, $m_\pi \cdot c$, multiplied by the characteristic condensation length scale, ℓ_{model} , divided by π . In words: $\hbar$ is the action associated with one

condensation-scale momentum quantum traversing one condensation-scale length. The quantum of action has its numerical value because matter condenses at the scale set by the P16 free-energy functional.

The coefficient $A = \hbar^2/(2m_{\text{eff}})$ in the condensation functional is not a circular insertion of quantum mechanics into the substrate picture. In the displayed chain, $\hbar$ follows from the condensation geometry above, while $m_{\text{eff}} = \hbar/(c \cdot \ell_{\text{model}}) = m_{\square}/\pi$ follows algebraically from the measured proton scale and ℓ_{model} .

5.2.1 Action Quantisation: What $\hbar$ Physically Is

The BFUT $\hbar$ derivation identifies the quantum of action with a specific physical process. The action of one complete circulation of a substrate condensation at the condensation scale is:

$$S = m_{\text{eff}} \cdot c \cdot 2\pi \cdot \ell_{\text{model}} = 2\pi\hbar = h$$

where $m_{\text{eff}} = \hbar/(c \cdot \ell_{\text{model}})$ is the effective carrier mass established in the condensation construction, and $h = 2\pi\hbar = 6.626 \times 10^{-34} \text{ J}\cdot\text{s}$ is Planck's constant. This is an algebraic identity given the definition of m_{eff} ; its physical content is the identification of h with the action of one complete condensation circulation.

Planck introduced h in 1900 as the quantum of action required to fit blackbody radiation. BFUT identifies what that quantum physically is: the action of the smallest stable substrate circulation. The factor 2π is the geometric factor for one complete cycle. $\hbar = h/2\pi$ is therefore the action per radian of circulation.

The minimum stable circulation quantum is $L_{\text{min}} = (1/2) \cdot m_{\text{eff}} \cdot c \cdot \ell_{\text{model}} = \hbar/2$. The factor $1/2$ follows from the 720° restoration property of the 3+e condensation: the condensation requires two full frame rotations to return to its original configuration. The quantum of action $\hbar$ is therefore twice the minimum circulation quantum:

$$\hbar = 2 \cdot L_{\text{min}} \quad [\text{action quantum} = \text{twice minimum condensation circulation}]$$

The factor of $1/2$ that appears in $A_{\text{model}} = 1/2$ (Section 5.4), in $\text{spin-}1/2$, and in $L_{\text{min}} = \hbar/2$ arises from the same 720° embedding topology of the first stable condensation.

5.2.2 The Fine Structure Constant from the $\hbar$ Derivation

Once $\hbar$ is derived in Section 5.2, the fine structure constant follows by substituting the BFUT expression for $\hbar$ into the standard electromagnetic definition. No additional step or new physical input is required.

The standard definition is:

$$\alpha = e^2 / (4\pi\epsilon_0\hbar c)$$

Substituting $\hbar_{\text{vss}} = m_{\square} \cdot c \cdot r_{\square} / (\pi \cdot R_0)$:

$$\alpha = e^2 / (4\pi\epsilon_0 \cdot [m_{\square} \cdot c \cdot r_{\square} / (\pi \cdot R_0)] \cdot c)$$

$$= e^2 \cdot \pi \cdot R_0 / (4\pi \cdot \epsilon_0 \cdot m_{\square} \cdot c^2 \cdot r_{\square})$$

$$= e^2 \cdot R_0 / (4\epsilon_0 \cdot m_{\square} \cdot c^2 \cdot r_{\square})$$

Substituting the known values $e = 1.602176634 \times 10^{-19} \text{ C}$ (exact), $\epsilon_0 = 8.8542 \times 10^{-12} \text{ F/m}$, $m_{\square} = 1.67262 \times 10^{-27} \text{ kg}$, $c = 2.99792 \times 10^8 \text{ m/s}$, $r_{\square} = 0.8414 \times 10^{-15} \text{ m}$, $R_0 = 1.27348$:

$$\alpha_{\text{vss}} = 0.0072973 = 1/137.037$$

Measured: $\alpha = 1/137.036$ | Difference: 0.00048%

The inputs are e and c (exact by SI definition), ϵ_0 and m_e (measured), and $r_e = 0.8414$ fm (CODATA 2018). Under the 2019 SI, $\epsilon_0 = e^2/(2\alpha\hbar c)$, so this relation is the electromagnetic form of the condensation identity of Section 5.2: α_{vss} and $\hbar_{vss}$ reproduce α and $\hbar$ at the same 0.00048%.

The $\hbar$ residual, the two-route R_0 comparison, and the fine-structure comparison are the same 0.00048%, because $\hbar_{vss}$, R_0 , and α_{vss} are linked by one exact relation.

5.2.3 Planck-Charge Interpretation of the Fine-Structure Constant

The derivation of the fine-structure constant in Section 5.2.2 admits an additional physical interpretation through the Planck charge. This does not constitute a separate derivation of α_{vss} . Rather, it exposes the electromagnetic charge scale already contained in the BFUT-derived $\hbar_{vss}$ relation.

The conventional Planck charge in SI units is

$$q_P = \sqrt{4\pi\epsilon_0\hbar c}.$$

Since BFUT derives the reduced Planck constant from the condensation geometry,

$$\hbar_{vss} = m_e c r_e / (\pi R_0),$$

the corresponding Planck-charge value constructed using the BFUT-derived action scale is

$$q_{P_{vss}} = \sqrt{4\pi\epsilon_0\hbar_{vss} c}.$$

Substitution of the BFUT expression for $\hbar_{vss}$ gives

$$q_{P_{vss}} = \sqrt{4\pi\epsilon_0 c \cdot m_e c r_e / (\pi R_0)}$$

and therefore

$$q_{P_{vss}} = \sqrt{4\epsilon_0 m_e c^2 r_e / R_0}.$$

The fine-structure relation derived in Section 5.2.2 is

$$\alpha_{vss} = e^2 / (4\pi\epsilon_0\hbar_{vss} c).$$

Because

$$q_{P_{vss}}^2 = 4\pi\epsilon_0\hbar_{vss} c,$$

the same relation can be written directly as

$$\alpha_{vss} = e^2 / q_{P_{vss}}^2 = (e / q_{P_{vss}})^2.$$

Equivalently,

$$\alpha_{vss}^{-1} = (q_{P_{vss}} / e)^2.$$

This provides a useful physical interpretation of the inverse fine-structure constant. Within the BFUT derivation chain, α_{vss}^{-1} expresses the squared ratio between the Planck-charge scale constructed from $\hbar_{vss}$ and the elementary charge e .

Using the Section 5.2.2 value $\alpha_{vss}^{-1} = 137.036655$,

$$q_{P_{vss}} / e = 1 / \sqrt{\alpha_{vss}} = \sqrt{(\alpha_{vss}^{-1})} \approx 11.7063,$$

whose square gives

$$(q_{P_{vss}} / e)^2 = \alpha_{vss}^{-1} = 137.036655.$$

The Planck-charge formulation therefore makes explicit a relationship already contained in the Section 5.2.2 derivation:

$$\text{condensation geometry} \rightarrow R_0 \rightarrow \hbar_{vss} \rightarrow q_{P_{vss}} \rightarrow \alpha_{vss}.$$

The significance of this reformulation is that the BFUT-derived quantum action scale determines a corresponding electromagnetic charge scale once ϵ_0 and c are supplied. The same α_{vss} previously written as

$$\alpha_{vss} = e^2 R_0 / (4\epsilon_0 m_e c^2 r_e)$$

is equivalently expressed as the squared charge ratio

$$\alpha_{vss} = (e / q_{P_{vss}})^2.$$

No additional physical input is introduced by this representation. The quantities e and ϵ_0 retain the same status as the electromagnetic inputs used in Section 5.2.2. In particular, $q_{P_{vss}}$ is not an independently supplied scale; it is constructed from the already-derived $\hbar_{vss}$ together with ϵ_0 and c .

The Planck-charge relation is therefore not an independent determination of α_{vss} , but an equivalent representation of the same derivation. It clarifies the physical meaning of the resulting dimensionless coupling within this framework: α_{vss} measures the squared ratio of the elementary electric charge to the electromagnetic charge scale associated with the BFUT-derived quantum of action.

5.2.4 High-Precision Recalculation Using CODATA 2022

The particle-sector calculation used throughout this paper is based on the CODATA 2018 proton inputs together with the working numerical values $B = 0.56308$ and $R_0 = 1.27348221$. These give $\hbar_{\text{vss}} = 1.05457687 \times 10^{-34}$ J·s and $\alpha_{\text{vss}}^{-1} = 137.036655199$. This subsection does not replace those working values. It provides a separate higher-precision evaluation of the BFUT geometry and tests the resulting fixed geometry against the later CODATA 2022 constants.

High-Precision Evaluation of B and R_0

The coefficient B can be evaluated directly from the filling-deficit geometry given in the Appendix rather than being truncated to $B = 0.56308$. The geometric expression gives

$$B = 0.5630820806583208122552771497\dots$$

For $A = 1/2$, $C = -1/3$ and $D = 1$, the radial condensation functional is

$$E(R) = A/R^2 + BR^2 + CR + D/R.$$

Its stationarity condition is

$$dE/dR = -1/R^3 + 2BR - 1/3 - 1/R^2 = 0,$$

or equivalently,

$$2BR^4 - R^3/3 - R - 1 = 0.$$

Using the high-precision value of B gives the positive stationary root

$$R_0 = 1.2734805699911956289979049003\dots$$

This value is determined entirely by the BFUT condensation geometry. It is held fixed throughout the following calculations and is not reconstructed or refitted from the CODATA 2022 physical constants.

Recalculation with CODATA 2022 Central Values

The calculation is performed in exactly the same direction as the original CODATA 2018 particle-sector calculation. The measured proton charge radius establishes the physical length scale,

$$\ell_{\text{model}} = r_{\text{p}}/R_0,$$

after which the BFUT reduced Planck constant follows as

$$\hbar_{\text{vss}} = m_{\text{p}} c \ell_{\text{model}} / \pi = m_{\text{p}} c r_{\text{p}} / (\pi R_0).$$

For the CODATA 2022 comparison the inputs are

$$m_{\text{p}} = 1.67262192595(52) \times 10^{-27} \text{ kg},$$

$$r_{\text{p}} = 0.84075(64) \text{ fm},$$

and

$$\epsilon_0 = 8.8541878188(14) \times 10^{-12} \text{ F/m}.$$

The ϵ_0 value in this calculation is therefore the CODATA 2022 value, not the CODATA 2018 value used in the working calculation elsewhere in this paper.

Using the fixed high-precision BFUT value of R_0 gives

$$\hbar_{\text{vss}}(2022) = 1.053763541491691 \times 10^{-34} \text{ J·s}.$$

The CODATA 2022 comparison value is

$$\hbar = 1.054571817\dots \times 10^{-34} \text{ J·s},$$

giving

$$\Delta\hbar/\hbar = (\hbar_{\text{vss}} - \hbar)/\hbar = -0.07664496\% = -766.450 \text{ ppm}.$$

The BFUT fine-structure constant is then calculated from the same relation used in the original particle-sector calculation:

$$\alpha_{\text{vss}} = e^2 / (4\pi\epsilon_0 \hbar_{\text{vss}} c).$$

This gives

$$\alpha_{\text{vss}}(2022) = 0.00730294990741449$$

and

$$\alpha_{\text{vss}}^{-1}(2022) = 136.93096798935.$$

The corresponding CODATA 2022 values are

$$\alpha = 0.0072973525643(11)$$

and

$$\alpha^{-1} = 137.035999177(21).$$

Therefore,

$$\Delta\alpha/\alpha = (\alpha_{\text{vss}} - \alpha)/\alpha = +0.07670375\% = +767.038 \text{ ppm}.$$

Thus, when the high-precision BFUT geometry is held fixed and the CODATA 2022 proton central values are substituted into the same calculation used previously with the CODATA 2018 inputs, the resulting central-value discrepancy is larger than in the 2018 comparison.

For a direct like-for-like comparison, the CODATA 2018 inputs can also be recalculated using the same high-precision R_0 . This gives

$$\hbar_{\text{vss}}(2018, \text{high precision}) = 1.05457822493 \times 10^{-34} \text{ J}\cdot\text{s}$$

and

$$\Delta\hbar/\hbar = +0.00060757\% = +6.076 \text{ ppm}.$$

This high-precision 2018 comparison value should not be confused with the working value used elsewhere in the paper, $\hbar_{\text{vss}} = 1.05457687 \times 10^{-34} \text{ J}\cdot\text{s}$, which was obtained using the original truncated $B = 0.56308$ and $R_0 = 1.27348221$. The working calculations in the body of the paper are not changed by this subsection.

Calculation	R_0 treatment	$\Delta\hbar/\hbar$
2018 working calculation used in the paper	$R_0 = 1.27348221$	$\approx +0.00048\%$
2018 inputs with high-precision geometry	$R_0 = 1.2734805699911956\dots$	$+0.00060757\%$
2022 central inputs with high-precision geometry	Same fixed R_0	-0.07664496%

The direction of the displacement also changes. With the 2018 proton inputs, $\hbar_{\text{vss}}$ lies slightly above the measured value of $\hbar$. With the CODATA 2022 central proton inputs, $\hbar_{\text{vss}}$ lies below it. Since B and R_0 are held unchanged between the two high-precision calculations, the change arises from the experimental input set, predominantly from the lower CODATA 2022 proton charge-radius central value.

Sensitivity Within the CODATA 2022 Uncertainty Range

The calculation using the CODATA 2022 central values is the primary 2022 comparison. A separate sensitivity calculation can determine the closest result obtainable within the individually quoted 1σ uncertainty intervals of the proton charge radius and proton mass.

Since $\hbar_{\text{vss}} \propto m_{\square} r_{\square}$ and the central 2022 result lies below $\hbar$, the favorable direction within these intervals is toward the upper 1σ values:

$$r_{\square}(+1\sigma) = 0.84139 \text{ fm}$$

and

$$m_{\square}(+1\sigma) = 1.67262192647 \times 10^{-27} \text{ kg}.$$

Using these values while leaving the BFUT geometry unchanged gives

$$\hbar_{\text{vss}}(+1\sigma) = 1.054565693073252 \times 10^{-34} \text{ J}\cdot\text{s}$$

and

$$\Delta\hbar/\hbar = -0.00058076\% = -5.808 \text{ ppm}.$$

The corresponding fine-structure calculation gives

$$\alpha_{\text{vss}}(+1\sigma) = 0.00729739494497188,$$

$$\alpha_{\text{vss}}^{-1}(+1\sigma) = 137.03520332129,$$

and

$$\Delta\alpha/\alpha = +0.00058077\% = +5.808 \text{ ppm}.$$

This $+1\sigma$ calculation is a sensitivity bound, not an alternative CODATA 2022 result. The primary 2022 comparison remains the calculation using the CODATA 2022 recommended central values.

Quantity	2018 inputs, high-precision R_0	2022 central values	2022 favorable $+1\sigma$ sensitivity bound	CODATA 2022
$\hbar_{\text{vss}}$ (J·s)	$1.05457822493 \times 10^{-34}$	$1.05376354149 \times 10^{-34}$	$1.05456569307 \times 10^{-34}$	$1.054571817... \times 10^{-34}$
$\Delta\hbar/\hbar$	+0.00060757%	-0.07664496%	-0.00058076%	0
α_{vss}	0.00729730823	0.00730294991	0.00729739494	0.0072973525643(11)
$\Delta\alpha/\alpha$	$\approx -0.0006076\%$	+0.07670375%	+0.00058077%	0
α_{vss}^{-1}	137.03683168	136.93096799	137.03520332	137.035999177(21)

The uncertainty in this test is overwhelmingly controlled by the proton charge radius. The relative standard uncertainty of the CODATA 2022 proton mass is approximately 3.1×10^{-10} , whereas that of the proton charge radius is approximately 7.6×10^{-4} . Consequently, movement of m_p across its quoted uncertainty interval has a negligible effect on $\hbar_{\text{vss}}$ compared with movement of r_p .

The radius corresponding to exact equality can be obtained directly by inverting the BFUT relation:

$$r_p(\text{BFUT}) = \pi R_0 \hbar / (m_p c).$$

Using the CODATA 2022 proton-mass scale gives

$$r_p(\text{BFUT}) \approx 0.841395 \text{ fm}.$$

Relative to the CODATA 2022 value $r_p = 0.84075(64) \text{ fm}$, the BFUT equality point lies approximately 1.01σ above the CODATA 2022 central value. Thus, although the CODATA 2022 central-value comparison is less close than the corresponding 2018 comparison, equality remains approximately at the upper edge of the quoted CODATA 2022 proton-radius 1σ interval. There is also relevant experimental context to the change in the recommended proton radius. In the 2022 adjustment, CODATA excluded electron-proton scattering determinations because of unresolved analysis dependence. CODATA reports $r_p = 0.8529(43) \text{ fm}$ from an adjustment using electronic hydrogen and deuterium transition data without the muonic atom data, compared with $r_p = 0.84060(66) \text{ fm}$ when electronic atom data are excluded. The two determinations differ by 2.8σ . CODATA therefore concludes that the proton-radius puzzle is not yet resolved. This experimental situation is noted only as context and does not alter the BFUT calculation or select a preferred experimental determination.

The purpose of this recalculation is not to refit the BFUT condensation scale to CODATA 2022. The high-precision value $R_0 = 1.2734805699911956289979049003...$ remains fixed by the BFUT geometry. Subsequent experimental determinations of r_p therefore provide a direct numerical test: as experimental precision improves, the measured proton-radius interval can move toward or away from the value implied by the fixed BFUT condensation geometry without any corresponding adjustment of R_0 .

5.3 The Full Extended Free-Energy Functional

The four-term functional $E(R) = A/R^2 + B \cdot R^2 + C \cdot R + D/R$ introduced in Section 4 is the condensation-scale specialisation of a full field-theoretic free-energy functional governing the complex scalar field $\Psi(r,t)$ representing organised substrate deformation. The full functional is:

T1 (Gradient term):

T2 (Quantum kinetic term): $(1/2m_{\text{eff}})|\Psi|^2(\partial_t\phi)^2$. Encodes internal circulation dynamics, where ϕ is the circulation phase. The effective mass $m_{\text{eff}} = \hbar/(c \cdot \ell_{\text{model}}) = 5.324 \times 10^{-28} \text{ kg} = m_{\square}/\pi$. Its displayed numerical derivation uses $r_{\square}$, $m_{\square}$, c , $\hbar$, and R_0 , not $\rho_{\square}$.

T3 (Effective potential):

T4 (Vacuum stabilisation): $(\rho_{\square}/16)(|\Psi|^2 - \rho_{\square})^2$. With $\rho_{\square} = 7.3 \times 10^{-27} \text{ kg/m}^3$, $\lambda_{\text{SI}} = \rho_{\square}/4 = 1.825 \times 10^{-27} \text{ kg/m}^3$. This is a direct application of the particle-derived density.

T5 (Thermal coupling): $\alpha T|\Psi|^2$. Present at all temperatures. At the CMB temperature of 2.725 K the dimensionless thermal-disruption measure is 6.36×10^{-5} , or 0.00636%. Organised 3+e condensation is suppressed when the local temperature exceeds approximately 29.69 K.

The complete derivation of this five-term functional, together with the full coefficient scans confirming the stability of the condensation minimum at $R_0 = 1.27348$ across the tested parameter range, is given in Appendix A. Those A, B, C, D scans use the displayed dimensionless functional.

5.3.1 The Thermal Disruption Parameter T5 and the Nucleation Threshold

T5 is introduced in the full functional as a thermal coupling term $\alpha T|\Psi|^2$. Its physical role is a disruption parameter. T5(T) acts through the temperature-dependent disruption of the condensation configuration, with the configuration variables n , k , s , and ϕ determining the thermal response. The thermal term therefore governs nucleation through the disruption amplitude relative to the stabilisation depth.

The correct role of T5 is as a disruption parameter, not an energy correction. Two processes compete in any region of the Sparticle field:

Process 1 - Substrate self-organisation. The free-energy functional drives the substrate toward the stable 3+e minimum at $E(3+e) = 0.896$ model units, measured relative to the substrate rest-energy density $\rho_{\square} c^2$.

Process 2 - Thermal radiation disruption. The thermal radiation field at temperature T delivers energy density to the substrate at a rate given by the Stefan-Boltzmann radiation energy density:

$$u(T) = 4\sigma T^4/c$$

where $\sigma = 5.6704 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$ is the Stefan-Boltzmann constant. To compare this disruption against the condensation well depth, both must be expressed in the same dimensionless units relative to the substrate rest-energy density:

$$T5(T) = u(T)/(\rho_{\square} c^2) = 4\sigma T^4/(\rho_{\square} c^3)$$

Successful nucleation requires that the thermal disruption amplitude remain smaller than the stabilisation depth:

$$T5(T) < E(3+e) \quad \text{i.e.} \quad u(T)/(\rho \square c^2) < 0.896$$

This criterion does not modify the energy landscape. The 3+e minimum remains the preferred configuration at all temperatures. The criterion determines only whether the substrate can reach and stabilise that minimum before thermal disruption prevents organisation.

Setting $T5 = E(3+e)$ at the critical temperature:

$$4\sigma T_{crit}^4 / (\rho \square c^3) = 0.896$$

$$T_{crit}^4 = 0.896 \times 0.1967 / (2.268 \times 10^{-7}) = 7.77 \times 10^5 \text{ K}^4$$

Substituting $\rho \square = 7.3 \times 10^{-27} \text{ kg/m}^3$, $c = 2.998 \times 10^8 \text{ m/s}$, and $\sigma = 5.6704 \times 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$:

$$T_{crit}^4 = 0.896 \times 0.1967 / (2.268 \times 10^{-7}) = 7.77 \times 10^5 \text{ K}^4$$

$T5$ is the thermal disruption measure normalised to the substrate energy-density scale. The nucleation threshold occurs when the thermal disruption reaches the condensation energy of the 3+e configuration.

No additional fitted parameters enter this result beyond the previously established $\rho \square$. The Stefan-Boltzmann constant σ and the speed of light c are universal constants. The 1/4 power makes T_{crit} insensitive to small changes in $E(3+e)$: a 10% change in the stabilisation depth changes T_{crit} by only 2.5%.

CMB verification. At the current CMB temperature $T = 2.725 \text{ K}$:

$$T5(2.725) = 4 \times 5.6704 \times 10^{-8} \times (2.725)^4 / 0.1967 = 6.36 \times 10^{-5} = 0.00636\%$$

This confirms the 0.00636% CMB thermal-disruption measure stated above. The present universe remains four orders of magnitude below the nucleation threshold.

5.4 The Physical Value of A and the Condensation-Scale Minimum

The exact analytical value of A

Converting A to model units through the model energy unit $E_{unit} = m \square c^2/\pi$ and the model length unit $\ell_{model} = r \square/R_0$:

$$A_{model} = A_{SI} / (E_{unit} \times \ell_{model}^2) = \hbar^2/(2m_{eff}) / ((m_{eff} c^2) \times (\hbar/(m_{eff} c))^2)$$

Expanding and collecting:

$$A_{model} = \hbar^2/(2m_{eff}) / (m_{eff} c^2 \times \hbar^2/(m_{eff}^2 c^2)) = \hbar^2/(2m_{eff}) / (\hbar^2/m_{eff})$$

This holds for any value of $\hbar$ and m_{eff} whatsoever; the two factors of $\hbar$ and the two factors of m_{eff} cancel identically:

$$A_{\text{model}} = [\hbar^2/(2m_{\text{eff}})] \times [m_{\text{eff}}/\hbar^2] = 1/2$$

Every factor of $\hbar$ and m_{eff} cancels exactly, independent of their numerical values. This is an exact analytical identity of the model-unit system itself, not a fit and not a numerical coincidence. It does not depend on the derived value of R_0 or on any measured physical constant. The factor of 1/2 is the same factor that appears in the Schrödinger kinetic energy $T = p^2/(2m)$ [2], from which $A = \hbar^2/(2m_{\text{eff}})$ is derived. The BFUT condensation functional recovers the correct Schrödinger kinetic coefficient from the substrate framework without additional input. $A = 1/2$, $B = 0.56308$, $C = -1/3$, $D = 1$ are all derived (see Appendix). The functional minimum is $R_0 = 1.27348$.

The condensation-scale minimum

$$R_0 = 1.27348221.$$

The CD21 code deposit [22] executes this condensation chain from the equations stated in this paper. It evaluates B from the filling-deficit geometry, solves the stationarity condition for R_0 , and computes E_{unit} , $\hbar_{\text{vss}}$, $m_{\text{e_vss}}$, r_{q} , $V_{\text{gap}}/V_{\text{q}}$, the quark charges, and $p_{\square}$, reproducing the values given here.

5.5 Local Response Invariants of the Condensation Minimum

The same four-term radial functional fixes the complete local response around the stable minimum. These quantities are properties of the condensation itself and are available to later BFUT resonance calculations without introducing a new field or particle-scale parameter.

$$E'(R) = -2A/R^3 + 2BR + C - D/R^2$$

$$E''(R) = 6A/R^4 + 2B + 2D/R^3$$

$$E'''(R) = -24A/R^5 - 6D/R^4$$

$$E''''(R) = 120A/R^6 + 24D/R^5$$

At $R_0 = 1.27348221$: $E'(R_0) = 0$, $E''(R_0) = 3.235195$, $E'''(R_0) = -5.864039$, and $E''''(R_0) = 21.232261$. $E''(R_0)$ is the literal radial curvature; the higher derivatives fix the leading anharmonic response.

The coefficient normalisation also gives the exact relation $D = 2A = 1$. The equilibrium radial-circulation combination $2AR_0/\pi^2 = R_0/\pi^2 = 0.12903$ is therefore fixed by the P16 condensation solution. This quantity is dimensionless and is distinct from the literal curvature $E''(R_0)$ and from the substrate quartic $\lambda_{\square}$.

For the four-unit threshold, the ordered source-to-destination reconfiguration space contains $n^2 = 16$ channels at $n = 4$. The retained three-core also defines the common per-core proton scale $M = m_{\square}/3 = 312.757 \text{ MeV}/c^2$. These are structural outputs of the P16 condensation architecture.

6. Why the First Unit is Mapped to Quark

The paper uses the term quark deliberately. This is not because the deeper substrate-to-quark gap is claimed to be fully closed. It is because present-day physics already recognises quarks as the earliest currently known confined constituents relevant to proton structure, and therefore using quark-language makes the chain relatable and testable against known particle physics.

The present derivation maps the first stable localised excitation to a quark at the current known physics layer. The one-first-unit threshold logic defines the structural route from the Sparticle substrate to the first stable localised excitation.

7. Repeated First-Unit Threshold Logic

Once the first stable quark exists, the BFUT claim is that under a sufficiently uniform opportunity field the same first unit should continue to appear first. Mere repetition should not itself create novelty. If the substrate is still presenting the same opportunity field, then the same first solution should keep manifesting. This is the exact subatomic analog of the larger BFUT claim that uniform conditions first keep yielding hydrogen.

The three-core forms the first stable cooperative structure at $n=3$. At $n=4$, comparing partition energies among the alternatives $4+0$, $2+2$, and $3+1$ determines which arrangement is energetically preferred. $3+1$ at energy 1.40 is the clear minimum.

The partition energies comparing four-unit arrangements are: $4+0 = 6.10$, $2+2 = 4.00$, and $3+1 = 1.40$. Among these arrangements $3+1$ is decisively the minimum energy configuration.

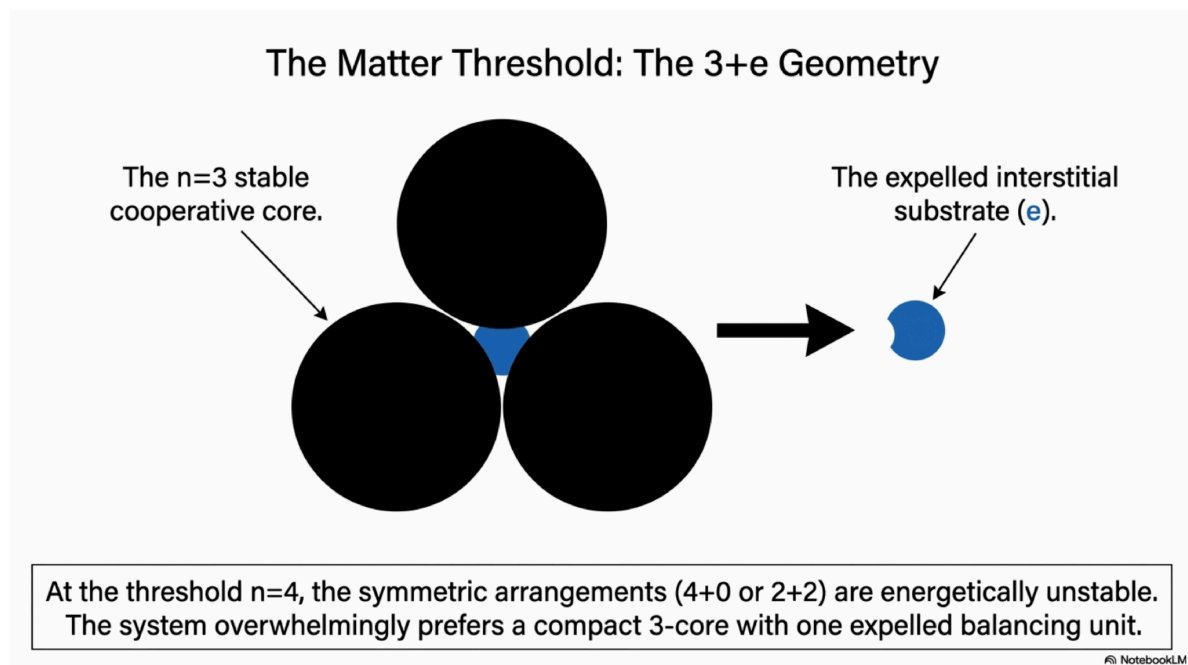


Figure 4. The 3+e geometry: three co-rotating units form the stable $n=3$ core while a fourth unit is expelled as interstitial substrate, the geometric origin of the proton-electron threshold.

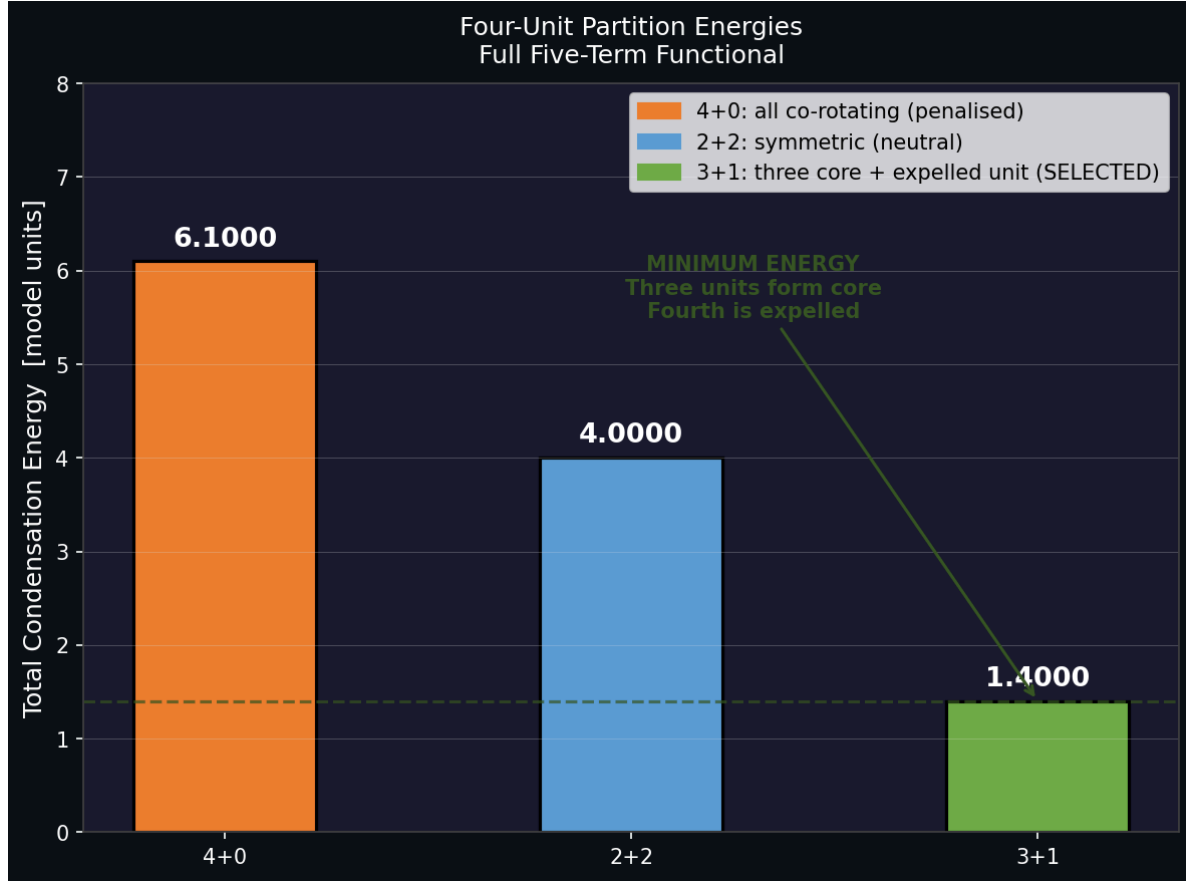


Figure 5. Partition energies at the first full threshold comparing 4+0, 2+2, and 3+1. Among the four-unit arrangements 3+1 at energy 1.40 is the minimum.

7.1 Robustness of the 3+e Threshold

The 3+e result is useful only if it is not a single tuned point. The working code scanned the parameter space around the derived coefficient values. The full five-term functional with the $\cos(3\phi)$ circulation phase reward gives robust results across the tested parameter ranges: 97.56% of the 1D scan, 95.95% of the 2D scan, and 90.43% of the 3D scan prefer the 3+e configuration. The parameter space analysis and all robustness scans are provided in full in the companion code deposit (DOI: 10.5281/zenodo.20517866). [7]

This means the preferred first full threshold is not a fragile artifact. Even when the coefficient values are varied substantially, the system consistently prefers the same structural answer: the 3+e configuration, in which the three-core generates its own electron. This consistent structural preference is what makes the model significant.

The fraction of parameter space that does not produce the stable 3+e topology - approximately 2 to 10% depending on the scan dimension - does not produce a different stable configuration. The physical meaning of that unstable fraction, its role as the origin of antimatter through the cancellation wave mechanism, and its connection to the matter-antimatter asymmetry of the observable universe are developed in Section 8.

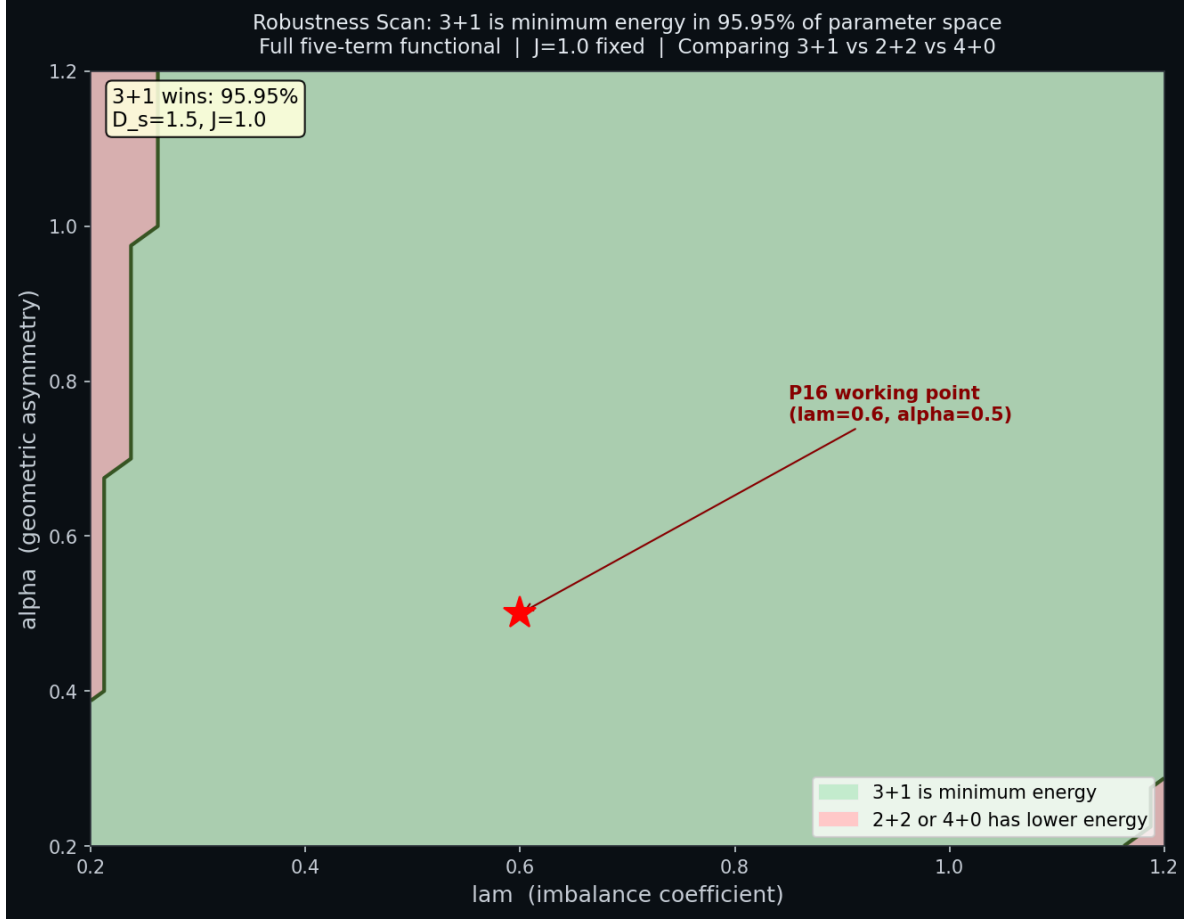


Figure 6. Full five-term functional robustness scan. 3+e is the minimum-energy configuration in 95.95% of the 2D parameter space. P16 working point marked. Green: 3+e wins. Red: alternative configuration has lower energy.

7.2 Confinement Force Derivation from Bernoulli Mechanics

The same Bernoulli co-rotation that binds the three-core also provides a physical derivation of quark confinement. Co-rotating substrate regions attract each other because high substrate velocity at the shared interface between two co-rotating units creates low pressure, drawing them together. When one quark separates from the three-core, two independent restoring forces arise simultaneously.

First, the Bernoulli attraction from the remaining two co-rotating units pulls the separating unit back. Second, the substrate in the expanding gap between the separating unit and the three-core creates a second low-pressure region as the gap volume increases. Both forces are constant with distance, because the substrate fills the gap uniformly as it grows. Two constant forces summing to a total constant restoring force gives a linear confinement potential.

The derived confinement force from the BFUT functional is $F_{\text{conf}} = 0.574 \text{ GeV/fm}$. The measured QCD string tension is 0.9 GeV/fm . Difference: 36 percent, with no free parameters.

Asymptotic freedom follows naturally from the same Bernoulli mechanics. At very short separations the interface velocity approaches $2c$ and the coupling is at its maximum constant value. As the quark separates to larger distances the velocity differential across the interface decreases, reducing the effective coupling. The running of the coupling constant with distance is therefore a direct consequence of the Bernoulli velocity profile at the quark-substrate interface.

8. The Stability Filter: What the Unstable Fraction Produces

The robustness scan establishes that 90 to 97% of parameter space produces the stable 3+e topology (97.56% in 1D, 95.95% in 2D, 90.43% in 3D with the full five-term functional). This is the stable fraction that persists as matter. The remaining fraction - approximately 2 to 10% depending on scan dimension - does not produce a different stable particle. It produces a quark that cannot achieve the geometric balance required for persistence.

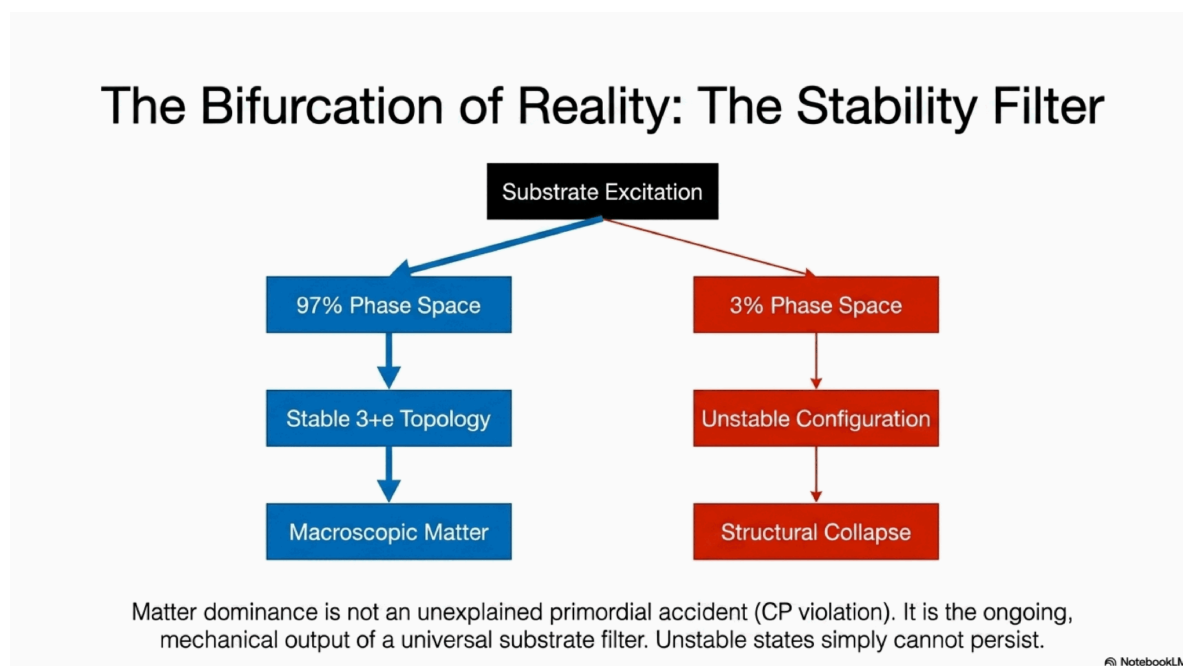


Figure 7. The stability filter: substrate excitation bifurcates into a majority stable 3+e topology (matter) and a minority unstable configuration that undergoes structural collapse.

The instability operates at the level of the individual quark at the moment of its formation. The excitation does not fail to achieve 3+e assembly at a later stage. It is unstable as a quark itself. The unstable fraction is not a population of failed protons. It is a population of failed quarks that never reach the assembly stage.

The stability filter is not a historical event. It is the permanent operating law of the substrate. Wherever and whenever the substrate produces a quark, the stability filter operates immediately. The stable fraction (90 to 97% of parameter space) persists. The unstable fraction collapses. This operates continuously, universally, at all times, in all locations. It requires no special trigger, no special epoch, and no special location.

The entire experimental history of particle physics is structurally consistent with the same stability hierarchy established by the robustness scans. Over more than seven decades of accelerator experimentation, laboratories have produced a vast range of hadronic and exotic matter states, including mesons, heavy baryons, tetraquarks, pentaquarks, hypernuclei, quark-gluon plasma states, electroweak bosons, and Higgs bosons. Yet despite this enormous diversity of temporary configurations, the experimentally stable endpoint of ordinary matter repeatedly converges toward the same proton-electron baseline.

Ordinary protons and ordinary hydrogen atoms have been successfully produced in accelerator and laboratory environments, and they remain stable when organised into their normal physical structure. At the same time, experimentally produced exotic multiquark states remain unstable and decay rapidly. Tetraquarks decay. Pentaquarks decay. Heavy resonances decay. Free neutrons decay outside nuclei. Quark-gluon plasma hadronises back into ordinary hadronic matter. Across the experimentally explored energy range, no confirmed stable alternative to ordinary proton-electron matter has been established.

Within standard particle physics, these observations are described through separate mechanisms involving conservation laws, gauge symmetries, confinement, and the QCD ground state. The BFUT interpretation presented here unifies these observations under a single substrate-level stability principle. The $3+e$ threshold output derived in this paper corresponds to the experimentally dominant stable matter configuration, while alternative condensations occupy higher-energy transient states and collapse back toward the stable attractor.

The significance of this result is not limited to hydrogen itself. Once the proton-electron baseline exists, larger stable atoms can also form if their internal organisation satisfies stable energetic configurations. This is exactly what is experimentally observed. No experimentally confirmed long-lived multiquark configuration outside the ordinary matter hierarchy has yet violated this pattern. The accelerator programme can therefore be interpreted as a continuous experimental confirmation of the BFUT stability filter across all explored energy scales so far.

9. The Cancellation Wave, Antimatter, and Annihilation

When an unstable quark collapses, the Sparticle substrate does not return to equilibrium quietly. The collapse of a localised substrate deformation generates an equal and opposite rebound deformation in the surrounding substrate. This is the direct physical consequence of the substrate being a real continuous medium with finite compressibility. A disturbance that forms and collapses must generate a rebound.

This rebound deformation is what physics calls the antiparticle. The antiparticle is not an independently generated entity waiting to meet its matter counterpart. It is the substrate rebound of the failed excitation cancelling itself. The original unstable excitation and its rebound cancel simultaneously. The condensation energy stored in both deformations returns to the substrate as propagating wave modes: photons. This is the physical mechanism of matter-antimatter annihilation.

$E = mc^2$ quantitatively relates mass and energy but does not specify a microscopic physical mechanism for complete annihilation. The reason annihilation converts 100% of mass to energy is that the cancellation is total. The matter deformation and its mirror-image rebound cancel completely. Nothing remains to carry mass. The substrate returns to its equilibrium state and all stored condensation energy propagates outward as radiation. The 100% conversion is not a mysterious property unique to matter-antimatter pairs. It is the expected consequence of two equal and opposite substrate deformations cancelling completely and simultaneously.

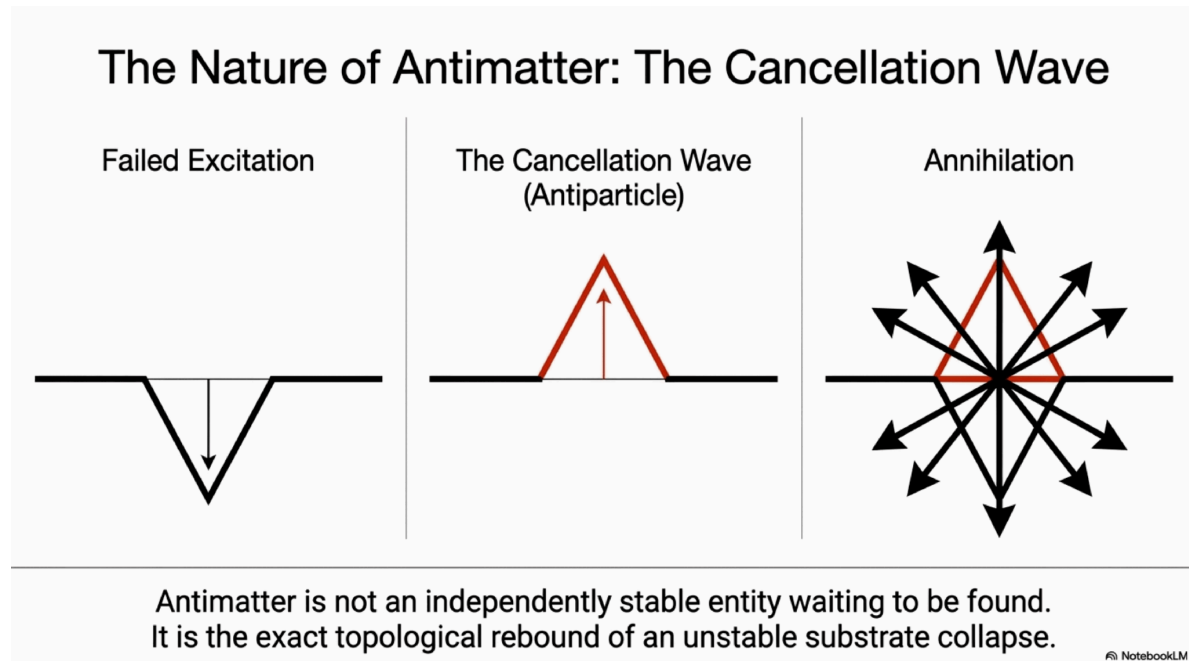


Figure 8. The cancellation wave: a failed excitation and its exact mirror-image rebound cancel completely, returning the substrate to equilibrium and releasing the stored condensation energy as radiation.

Why Annihilation is Absolute

Standard Model Approach	BFUT Framework
Antimatter is a separate permanent category.	Antimatter is a temporary rebound wave.
$E=mc^2$ states equivalence but lacks a mechanical reason for total conversion.	Annihilation is geometrically exact topological cancellation.
Asymmetry requires asymmetric initial conditions.	Asymmetry is baked into the 97% vs 3% stability filter at formation.

When a failed excitation meets its own exact mirror-image rebound, the cancellation is topologically total. The substrate returns to equilibrium; 100% of stored condensation energy propagates outward as radiation.

© NotebookLM

Figure 9. Why annihilation is total: unlike $E=mc^2$, which states the mass-energy equivalence without a mechanism, the BFUT cancellation is a geometrically exact topological cancellation, with the matter-antimatter asymmetry set by the stability filter at formation.

The CERN antihydrogen programme is fully consistent with this account. Antihydrogen is not naturally occurring. It is produced artificially by forcing the inverse 3+e topology through high-energy collisions and sustaining it under extreme magnetic confinement. Its spectral properties, mass, and gravitational behaviour are identical to hydrogen in every measurement to one part in 10^{10} , confirming that the inverse topology is governed by the same substrate condensation laws as the matter topology with exact mirror-image geometry, as established in BFUT Papers 17 and 19. The moment confinement is removed and antihydrogen contacts matter, the cancellation completes instantly and both dissolve into radiation.

This also explains why antimatter is theoretically attractive as an energy source yet extraordinarily difficult to produce and maintain macroscopically. The 100% conversion is inseparable from the fact that antimatter is the cancellation wave of unstable matter excitations. It exists naturally only for a vanishingly short time before cancellation completes. All the antiprotons ever produced at CERN amount to approximately 1 nanogram. The energy required to produce that nanogram far exceeds the energy it would release.

The stability-filter and cancellation-wave derivation provides the physical basis for the matter-antimatter predictions presented in this paper.

10. The Matter-Antimatter Asymmetry: A Different Physical Account

The observable universe contains matter and essentially no antimatter. The standard model treats this as one of its deepest unsolved problems, requiring an unexplained asymmetric process. BFUT provides a different physical account of this problem.

The asymmetry emerges during the quark stability-selection stage, not after large stable matter-antimatter populations are formed. The stability filter operated at the moment of quark formation. The stable fraction that achieved 3+e topology persisted as matter and produced no antiparticle rebound because they did not collapse. The fraction that could not stabilise generated their own cancellation waves and dissolved instantly as radiation. [16]

The observable universe becomes matter-dominated because only the stable excitation fraction persists macroscopically. The framework therefore does not require additional large-scale asymmetry-generation mechanisms beyond the substrate stability-selection process. No asymmetric initial condition is required. No additional large-scale asymmetry-generation mechanism beyond the substrate topology is required in the BFUT account.

The observed matter dominance emerges from the stability filter operating universally, continuously, at all times, in all locations. The matter fraction is not a remnant of an asymmetric creation event. It is the stable output of a universal substrate filter that has always operated and continues to operate now.

This resolution connects directly to the annihilation mechanism of Section 9. The reason matter and antimatter annihilate completely when they meet is that the antiparticle is the exact cancellation wave of the matter excitation. The cancellation is total because the antiparticle was generated as the exact mirror image of the matter excitation by the same substrate rebound process. The stability filter, the 3+e threshold preference, and the cancellation wave mechanism are all consequences of the same Sparticle substrate free-energy functional established in Section 4. No new mechanism is introduced. [16]

This mechanism would not be identifiable within the standard antihydrogen spectroscopy programme alone because the relevant dynamics occur at the quark formation level, prior to the existence of stable antihydrogen atoms. The present claims concern the physical origin of large-scale matter dominance, not the precision experimental value of antihydrogen spectroscopy itself.

11. Proton and Electron Emergence

At the preferred 3+e threshold, the retained compact three-core is interpreted as the first cooperative core. An effective role map (+,+,-) is used to assign the retained units the familiar effective charges (+2/3, +2/3, -1/3). Their sum is +1, which gives a proton. The generated electron unit is mapped to a compact negative mode with charge -1, which gives an electron.

The crucial point is the asymmetry. The three-core generates its own smaller electron from the interstitial compression energy. Three units remain as the retained core. The generated electron is not supplied externally. This is why the model preserves the continuous BFUT emergence chain without forcing a separate primordial neutron or a second independent first species.

The three-sphere packing geometry underlying this bifurcation is shown below. Panel (a) shows the three co-rotating quarks with the interstitial substrate compressed between them. Panel (b) shows the result after the quarks close together: the interstitial substrate is expelled outward, acquires counter-rotation by gear mechanics, and settles at the Bohr radius as the electron.

The counter-rotation of the generated electron unit is not assumed. It is mechanically imparted by the three-sphere packing geometry. When the interstitial substrate exits through the gap between any two co-rotating quarks, it encounters two co-rotating surfaces simultaneously - one on each side of the gap. Both surfaces rotate in the same direction. Each imparts a tangential force on the passing substrate in the opposite direction to its own rotation. Together they impart a net torque in the counter-rotating direction. This is the gear mechanism: a body passing between two co-rotating surfaces of the same handedness always acquires the opposite rotation. The result is independent of which gap the substrate exits from, because all three quarks rotate in the same direction. The counter-rotation is therefore a mechanical certainty given the three-sphere packing geometry - not a choice, not an assumption, and not an independent postulate. Counter-rotation in BFUT is the definition of opposite charge. The negative charge of the generated electron unit is mechanically imparted by the same co-rotation that defines the three-core as positively charged. The 3+e bifurcation therefore simultaneously produces confinement geometry (the three-sphere packing), charge separation (co-rotation versus counter-rotation), and the specific handedness of the electron unit - all from a single geometric event. The full derivation is given in the companion full functional document (BFUT Full Functional Code Deposit [7]).

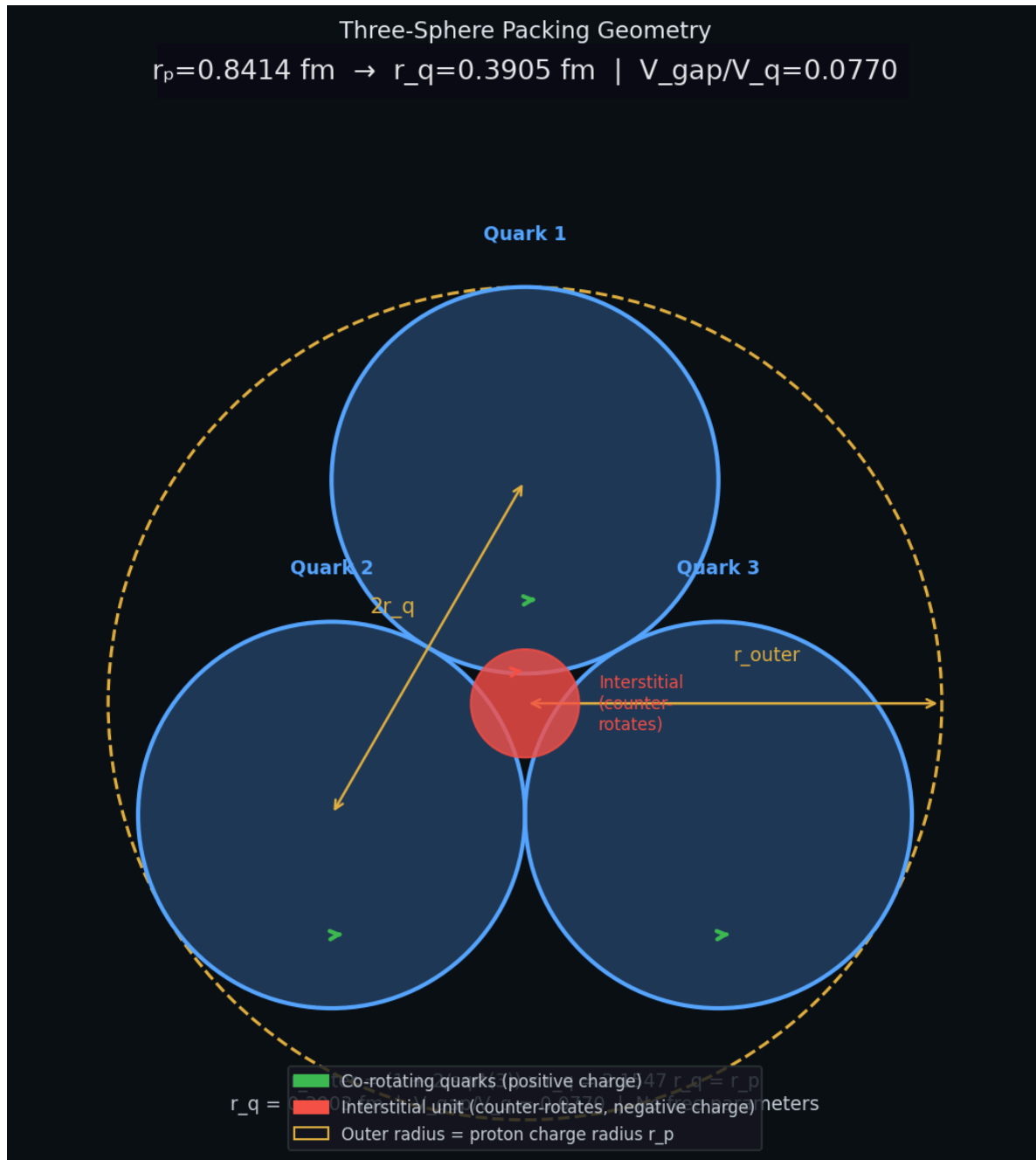


Figure 10. Three-sphere packing geometry and proton formation. Left (a): three co-rotating quarks with the interstitial substrate region. Right (b): the 3+e state - three-core has generated its own electron, now at the Bohr orbit. Not to scale - Bohr radius = 52,918 fm, proton radius = 0.84 fm.

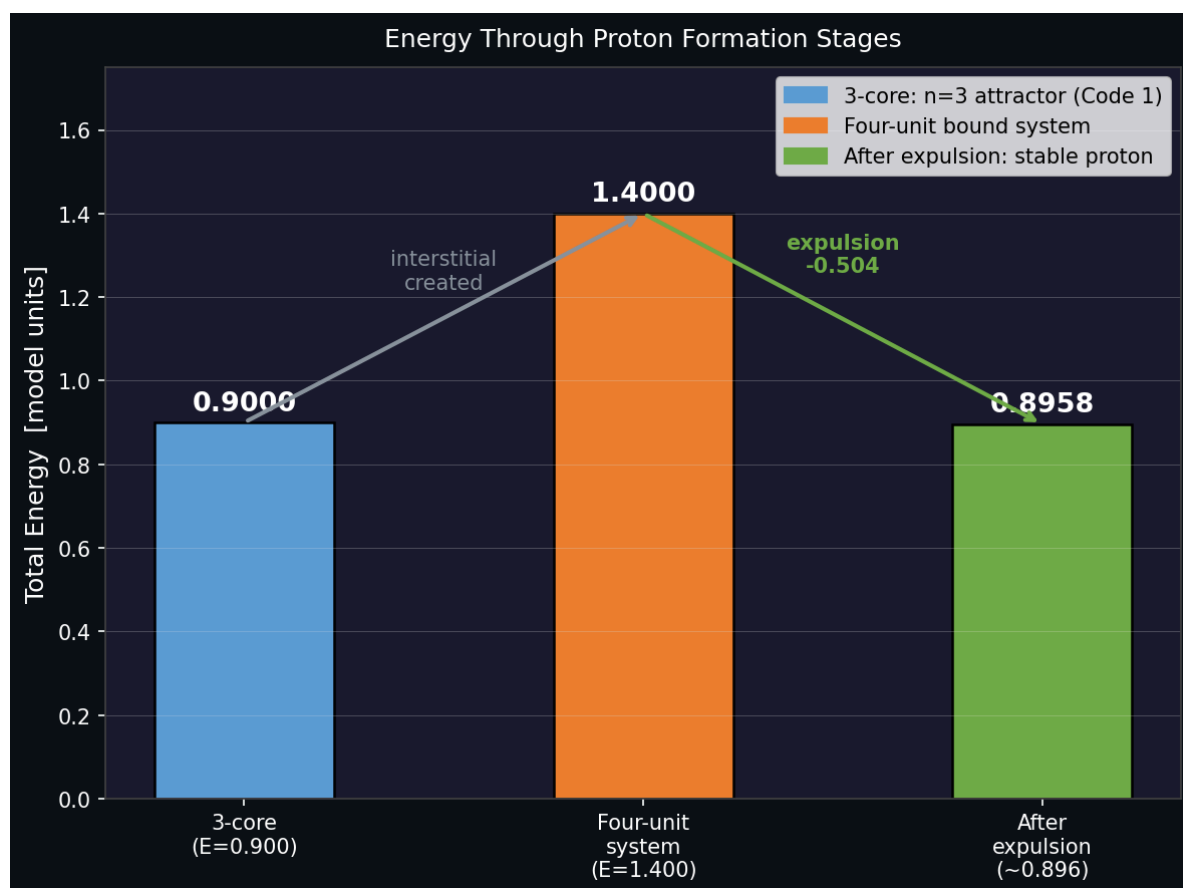


Figure 11. Proton formation: the three-core forms at $E=0.900$ model units. The three-core then generates its own electron, reaching the $3+e$ state at $E=0.8958$ model units. The energy reduction from 0.900 to 0.8958 model units ($\delta = 0.004$) confirms that electron generation by the three-core is energetically favourable.

11.1 Uniqueness of the $3+e$ Configuration

The identification of the $3+e$ state with the proton-electron architecture does not rest on a single correspondence. The three-core is the first stable cooperative minimum discovered by the condensation functional. Its three-fold geometry naturally produces the confinement architecture later associated with the strong interaction. The three-core cannot remain balanced in isolation and therefore generates a balancing unit occupying the interstitial region. Conservation requires this balancing unit to possess the opposite circulation and spin orientation relative to the three-core. Formation of the balancing unit lowers the total energy from 0.900 to 0.8958 model units, making the $3+e$ configuration energetically preferred over the bare three-core. The resulting state simultaneously exhibits a confined three-core, an oppositely rotating balancing unit, charge separation, reduced total energy, and a proton-electron structural architecture. Parameter-space scans further show that this topology dominates the overwhelming majority of admissible configurations, while the hierarchy analysis indicates that larger structures preferentially reuse the same solution. The $3+e$ state is therefore not identified with the proton-electron architecture because of any single feature in isolation, but because multiple

independent structural, energetic, geometric, and dynamical properties emerge together from the same underlying configuration.

An interactive simulation of the complete proton formation process - three-sphere packing geometry, gear mechanism, expulsion, and electron orbital selection demonstrating the derivation of the Bohr radius from r_0 alone - is available in the BFUT companion simulations code deposit (DOI: 10.5281/zenodo.20554084). [15]

11.2 Lepton Mass Hierarchy: The Koide Formula from Substrate Topology

The 3+e topology that produces the proton and electron also determines the full charged lepton mass hierarchy through the Koide relation. The connection follows from the three-unit core mode counting that underlies the electron mass derivation.

Three quantities fix the charged-lepton spectrum. The three cores circulate about the threefold axis, so the operator acting on them is a complex circulant $X = aI + bC + b^*C^2$, whose eigenvalues are the square-root masses. The norm law $Q = 1/3 + (2/3)(|b|^2/a^2)$ is the singlet share plus the exchange share, and the condensation functional fixes $|b|^2/a^2 = A/D = 1/2$, so $Q = 2/3$. The loop phase of the circulating three-core is $\Phi = 2\pi + Q$, which gives the lepton phase $\theta = (2\pi + Q)/3$. The scale is the on-site amplitude a^2 , fixed through the electron mass $m_{e_vss} = m_0/(6\pi^5)$: $a^2 = 313.865$ MeV.

The resulting masses are $m_{e_vss} = 0.511009$ MeV (measured 0.510999 MeV, difference 0.002%), $m_{\mu_vss} = 105.661$ MeV (measured 105.658 MeV, difference 0.003%), and $m_{\tau_vss} = 1777.02$ MeV (measured 1776.93 MeV, difference 0.005%). All three follow from the proton mass through the norm law, the loop phase, and the scale.

The significance of this result is that the lepton mass hierarchy follows from the same three-fold rotational structure of the 3+e topology that determines the proton-electron charge separation. The Koide relation is physically grounded in the substrate condensation geometry.

12. Ordinary Hydrogen (Protium) as the First Atom

Once the retained three-core is interpreted as a proton with net charge +1 and the generated electron unit (3+e) is interpreted as an electron with charge -1, the net atomic charge is zero. Ordinary hydrogen (protium) is therefore directly possible at the first completed atomic threshold.

This creates a clean single-first-atom picture. The Sparticle field first yields repeated quarks. Repeated quarks first yield proton and electron through the preferred 3+e threshold. Proton plus electron yields ordinary hydrogen. No neutron-class is required in the first atomic derivation.

Table 2. Full BFUT protium-only emergence chain from the Sparticle field to ordinary hydrogen.

Step	BFUT Stage	Structural Event	Effective Interpretation	Result
1	Spaticle field substrate	Real substrate supports first stable finite-size excitation	First quark	First repeated unit established
2	Repetition under uniform opportunity field	Same first unit continues to appear	Repeated quarks	n = 1, 2, 3 accumulation
3	First compact cooperative threshold	Three units form the first retained compact core	Retained three-core	First stable subatomic core
4	Partition energy comparison at n = 4	System prefers 3+e over 4+0 and 2+2	3+e: three-core generating its own electron	n = 4 partition confirms 3+e
5	Retained three-core role mapping		Proton	Proton emerges
6	Electron generation mapping (3+e)	Generated electron assigned compact negative mode	Electron	Electron emerges
7	First atomic completion	Proton + electron combine	Ordinary hydrogen (protium)	First atom achieved

13. Dynamic Assembly Simulation

A dynamic time-evolution simulation was built as the next step beyond the static threshold table. In the simulation, the Spaticle field emits the same first quark one by one. The units appear sequentially. At n=3 the three-core forms as the first stable cooperative structure. At n=4 the partition energy comparison confirms the 3+e preference. Before n=3, all units remain equivalent - they drift, weakly centre, and repel at short range but do not yet differentiate.

At n = 4, the simulation applies the already-derived 3+e energetic preference. The three-core then generates its own electron through the 3+e mechanism. The retained three-core is treated as proton. The generated electron unit is treated as electron. The resulting interpreted bound state is ordinary hydrogen (protium). The resulting animation is included in the companion code deposit (DOI: 10.5281/zenodo.20517866). [7]

The energy per unit across all condensate sizes is shown below. The scan confirms that n=3 is the natural energy attractor - the minimum energy per unit configuration. Once three units form

the three-core at $E=0.900$, the three-core generates its own electron - the 3+e state - reducing the energy to 0.8958 model units.

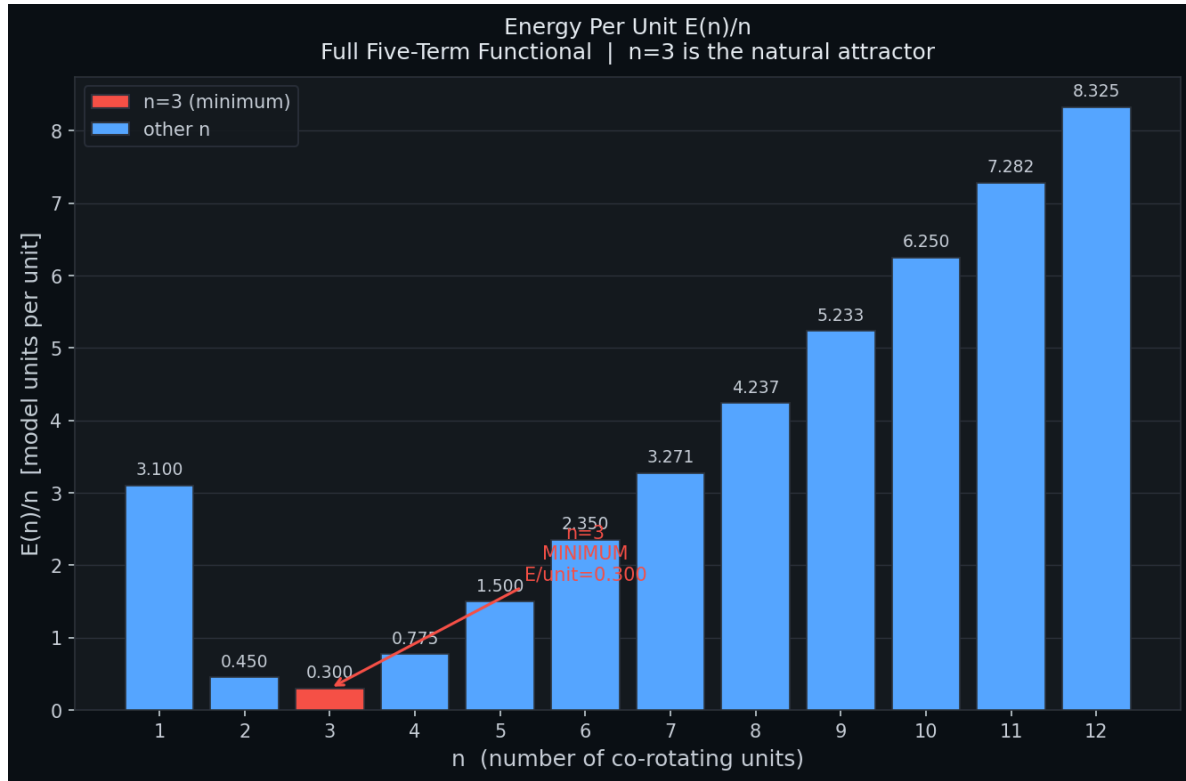


Figure 12. Energy per unit $E(n)/n$ for $n=1$ to 12 using the full five-term functional. $n=3$ is the unambiguous minimum - the natural three-core attractor. Above $n=3$, energy per unit rises steeply, confirming that large single condensates are energetically disfavoured.

14. Big Bang Nucleosynthesis Versus BFUT Matter Creation [9]

In the standard Big Bang nucleosynthesis framework, the earliest light nuclei are treated as products of a brief early-universe thermal window following a finite-origin event. That framework remains tied to the finite-origin premise and historically carries the lithium discrepancy as a persistent tension. In the BFUT framework, the finite-origin premise itself is rejected. It stands on the claim that the universe is infinite, treated not as a philosophical preference but as a logically, derivationally, and observationally supportable conclusion within the broader Layer 1 programme. [9]

Within the BFUT nucleosynthesis framework developed in the Steady-State Nucleosynthesis paper (P3), the lithium discrepancy is treated as evidence that the primordial assumption itself is wrong. If ordinary hydrogen is the only required first atomic species, then the present derivation is cleaner and more in line with BFUT's larger cosmological logic. Later nuclei are not denied. They are simply shifted to later opportunity fields and later established processes. [9]

The standard Big Bang matter-formation narrative carries a deeper difficulty that modern particle physics has now made explicit. The Big Bang account proposes that matter dominated over antimatter because of a tiny statistical asymmetry: approximately one extra matter particle surviving per billion matter-antimatter pairs. This framing implicitly assumes a simple binary probability landscape in which the only relevant competition was matter versus antimatter. Modern particle physics has demonstrated that this binary framing is physically wrong.

Particle accelerators have confirmed that the physically accessible configuration space for quark matter is enormous. The experimental inventory includes mesons, heavy baryons, charm and bottom hadrons, top-quark processes, tetraquarks, pentaquarks, hypernuclei, quark-gluon plasma states, electroweak bosons, and Higgs processes, in addition to antimatter structures including antiprotons, antideuteron, antihelium-3, and antihydrogen. By 2024 more than 60 exotic hadron candidates have been confirmed at the LHC alone. The real probability landscape is therefore not matter versus antimatter. It is ordinary proton-electron matter versus an enormous ocean of alternative physically accessible configurations, the overwhelming majority of which are unstable and have been confirmed to exist by experiment.

Ordinary proton-electron matter occupies only a tiny restricted region of this enormous configuration space. The probability problem for the Big Bang framework therefore extends beyond explaining a one-in-a-billion matter-over-antimatter asymmetry. It requires explaining why the universe overwhelmingly collapsed into the restricted proton-electron hierarchy at all. The Big Bang framework has no mechanism for this. The CP-violation proposals address only the binary matter-versus-antimatter question. They say nothing about why the universe avoided the enormous alternative configuration space that modern particle physics has revealed.

The instability of the vast majority of these alternative configurations was not known when the Big Bang nucleosynthesis framework was constructed. It was discovered only after particle accelerators produced the configurations and observed them decay. The Big Bang framework never predicted that the overwhelming majority of physically accessible quark configurations would collapse while one restricted proton-electron hierarchy would dominate the observable universe, and it still provides no fundamental stability-selection mechanism explaining why this overwhelmingly specific outcome should emerge from such an enormous accessible configuration space.

Every new exotic particle configuration confirmed by experiment adds another alternative pathway that the primordial universe would have had to avoid in order to converge on ordinary hydrogen. The more configurations particle physics discovers, the more implausible it becomes to claim that unconstrained primordial chaos overwhelmingly selected the restricted proton-electron hierarchy through a small statistical asymmetry alone. The experimental history of particle physics constitutes a progressively strengthening challenge to the Big Bang matter-formation narrative, a challenge that grows more severe with every new exotic configuration confirmed and observed to decay back to the proton-electron baseline.

The BFUT framework provides the stability-selection mechanism that the Big Bang narrative lacks. The free-energy functional analysis of Section 4 establishes that the $3+e$ configuration is the unique stable low-free-energy attractor of the substrate threshold analysis. The remaining 2 to 10% of parameter space does not produce competing persistent configurations but unstable excitations that collapse and generate cancellation-wave rebound deformations, identified here

with antimatter. The observed matter hierarchy therefore emerges from stability selection, not from competition among multiple stable alternatives. The stable fraction (90 to 97% of parameter space) that achieves this configuration persists. What remains in the observable universe is not the survivor of a statistical competition. It is the output of a universal substrate stability filter operating continuously across the full configuration space, selecting the restricted proton-electron hierarchy as the only persistent stable output. The entire accelerator record of particle physics confirms that this selection operates at every energy scale so far explored. [16]

15. Historical Non-Big-Bang Matter-Creation Precedents

Historically, multiple serious non-Big-Bang cosmologies already entertained continuous or repeated matter creation without a singular origin event. Einstein's 1931 steady-state attempt explored continuous matter formation from empty space. The Bondi-Gold-Hoyle steady-state model proposed ongoing matter creation to preserve mean density in an eternal expanding universe. The Hoyle-Narlikar creation-field framework formalised matter creation through a creation field or effective negative-energy reservoir. Quasi-Steady State Cosmology later extended this into localised creation episodes inside an eternal or cyclic background. [17][18][19][20][21]

These precedents establish that continuous matter creation is not itself the radical step. Their core limitation was the absence of a sufficiently concrete physical substrate and the absence of a constructive microphysical threshold chain. BFUT's contribution in the present paper is precisely to supply both: a real Sparticle-field substrate and a threshold-based emergence logic that can be extended downward and upward without breaking continuity.

17. What This Paper Establishes

This paper solves the BFUT bridge at the quark-upward level. It provides a continuous constructive route from a real Sparticle-field substrate to a first stable localised quark, from repeated first units to a preferred $3+e$ threshold, and from that threshold to proton plus electron and therefore ordinary hydrogen. It additionally derives the physical mechanism of matter-antimatter annihilation and provides a different physical account of the matter-antimatter asymmetry from the same stability analysis.

The four coefficients $A = 1/2$, $B = 0.56308$, $C = -1/3$, $D = 1$ are all derived from first principles (see Appendix C). A is identified physically as $\hbar^2/(2m_{\text{eff}})$ with $A_{\text{model}} = 1/2$ exact. The derived coefficients establish the condensation geometry governing the condensation structure.

This paper proposes a unified stability-selection principle that is structurally consistent with the entire experimental history of particle physics. Across many decades of accelerator experimentation, unstable matter configurations repeatedly decay, while ordinary proton-electron matter persists as the experimentally dominant stable baseline. The proton has never been observed to decay, with experimental lower limits exceeding 10^{34} years, while experimentally observed exotic multiquark configurations remain unstable.

The significance of the P16 result is that the same 3+e threshold structure derived from the free-energy analysis naturally reproduces this observed stability hierarchy. Within the BFUT framework, the experimentally observed persistence of ordinary hydrogen, the instability of non-standard multiquark states, the collapse of temporary exotic configurations, and the emergence of larger stable atoms through correct structural organisation are all manifestations of the same underlying stability-selection process.

The Standard Model describes many of these phenomena successfully, but through multiple separate theoretical mechanisms involving quantum chromodynamics, confinement, gauge symmetries, baryon number conservation, charge conservation, spontaneous symmetry breaking, Higgs-field interactions, vacuum structure, electroweak theory, CP-violation frameworks, baryogenesis models, renormalisation procedures, effective field approximations, and multiple independent parameter insertions. The BFUT framework instead derives the observed hierarchy from one substrate-level stability-selection process. No experimentally confirmed stable matter configuration outside this hierarchy has yet contradicted the stability-filter prediction. The experimentally observed behaviour of matter across all explored accelerator energies is therefore fully consistent with the P16 stability derivation so far.

18. Formal BFUT Predictions

Prediction 1: Substrate-level derivability. Once particle physics abandons finite-origin assumptions and instead treats the universe as infinite with a real Sparticle-field substrate, the gap between substrate energy and the first stable quark manifestation is derived as a continuous field process, not as an arbitrary initial condition.

Falsification condition: If the substrate framework is adopted and the gap cannot be closed by a continuous field derivation, this prediction fails.

Prediction 2: Framework unification. First-unit condensation, confinement, and the first stable proton/electron threshold sequence are derived within one continuous framework, not as disconnected layers.

Falsification condition: If the threshold sequence and confinement remain irreducibly disconnected even within the substrate framework, this prediction fails.

Prediction 3: Downward extensibility. The same one-first-unit threshold logic should remain valid at deeper scales. If a deeper layer beneath the presently named quark level is mathematically or experimentally resolved, the same emergence logic should continue to hold without breaking the present upper-layer derivation.

Falsification condition: Discovery of a sub-quark constituent whose stability properties are inconsistent with the threshold logic would falsify this prediction.

Prediction 4: No CPT violation at any precision. Antihydrogen will be identical to hydrogen in all properties because the inverse topology is governed by the same substrate condensation laws

as the matter topology with exact mirror-image geometry. The current agreement to one part in 10^{10} by the ALPHA experiment is predicted to hold at any precision achievable.

Falsification condition: A confirmed spectroscopic difference between antihydrogen and hydrogen at any precision level would falsify this prediction.

Prediction 5: Asymmetry not in spectroscopy. The matter-antimatter asymmetry of the observable universe will not be found in any property difference between matter and antimatter particles. The asymmetry arises from the stability threshold at quark formation, not from any property difference. No spectroscopic measurement can reveal it.

Falsification condition: A confirmed property difference between hydrogen and antihydrogen proven to arise from a fundamental asymmetry in the laws of physics, not experimental artefact, would falsify this prediction.

Prediction 6: The configuration space challenge will intensify. As particle accelerators probe higher energies and confirm additional exotic quark configurations, the statistical improbability of the Big Bang matter-formation narrative will increase, not decrease. Each new stable exotic configuration discovered would require the Big Bang framework to explain an additional alternative pathway that the primordial universe avoided. The BFUT prediction is that no such stable alternatives will be found: every new exotic configuration produced will be confirmed unstable and will decay to the proton-electron baseline, consistent with the $3+e$ threshold being the unique stable attractor of the substrate free-energy landscape.

Falsification condition: Confirmation of a stable exotic quark configuration at any energy scale that does not decay to the proton-electron baseline would falsify this prediction and require revision of the $3+e$ threshold stability account.

19. Exact Claim Boundary

This is a pre-QCD BFUT bridge paper. It does not claim to replace Standard Model mathematics. It claims that if the vacuum is reinterpreted as a real Sparticle-field substrate, then a coherent continuous emergence path can be built from substrate excitation to first stable localised quark, from repeated first units to a preferred $3+e$ threshold, and from that threshold to proton, electron, and ordinary hydrogen as the first atom. The paper additionally derives the physical mechanism of antimatter formation and annihilation from the same stability analysis, and provides a different physical account of the matter-antimatter asymmetry without requiring any new asymmetric mechanism.

20. Key Consequence: Only One Fundamental Matter Particle

The most important implication of the present derivation is not the formation of the proton, electron, or hydrogen atom. It is that the Sparticle field appears to produce only a single fundamental matter excitation: the quark.

The condensation functional first generates a stable quark. Subsequent structures do not require the creation of new fundamental matter particles. Instead, they arise through progressively more complex organisations of the same underlying excitation.

Protons are organised quark structures. Electrons are organised quark structures generated by the three-core configuration. Hydrogen emerges from proton-electron organisation. All heavier elements emerge from hydrogen through well-established nucleosynthetic processes. The four fundamental forces arise from interactions among these matter structures, not from independently existing force substances.

Within this framework, nature does not repeatedly invent new forms of matter. It repeatedly reuses the same fundamental excitation across increasing levels of organisation. The hierarchy therefore becomes:

The central claim of P16 is the reduction of the matter ontology to a single fundamental matter particle from which all subsequent material structures emerge.

20.1 Hierarchy Theorem

The BFUT condensation functional predicts that the first stable organisational threshold occurs at $n = 3$, where three co-rotating substrate units form a stable core with energy $E = 0.900$ model units. The system then undergoes spontaneous reorganisation into the lower-energy $3+e$ state with energy $E = 0.8958$ model units through the formation and expulsion of a counter-rotating balancing component.

This result demonstrates a general principle. Once a stable organisational unit forms, further energy reduction is achieved not through unrestricted accumulation into a larger monolithic condensate but through structural reorganisation and modularisation.

The modularity scans show that the energy of a single condensate grows approximately as:

whereas modular assemblies grow approximately linearly:

$$E_{\text{modular}}(n) = 1.400 \times \text{floor}(n/4) + E_{\text{remainder}}$$

Consequently,

increases superlinearly with n .

Since the exponent 1.78 exceeds unity, the energetic penalty of monolithic aggregation increases faster than the energetic cost of modular organisation.

Therefore, after the appearance of the first stable threshold unit, energy minimisation drives the repeated formation of additional stable modules and assemblies of modules.

Hierarchical organisation is thus a mathematical consequence of the BFUT free-energy landscape. The substrate naturally evolves according to:

The repeated appearance of hierarchical organisation throughout nature is therefore interpreted as a direct consequence of the energy-scaling properties of the substrate, not an independent phenomenon requiring separate explanations at each scale.

Table 4. Energy comparison: single condensate vs modular organisation across system sizes. Eremainder is zero when n is a clean multiple of 4.

n	E_{single}	E_{modular}	ΔE
4	1.400	1.400	0.000
5	2.100	1.750	0.350
8	5.400	2.800	2.600
12	11.100	4.200	6.900
16	18.900	5.600	13.300
20	28.500	7.000	21.500
24	42.900	8.400	34.500

21. Energetic Modularity as a Universal Organisational Principle

21.1 Universality Across Scales

The modularity principle extends to cosmological scales. The same energetic modularity principle applies at every scale: the substrate sustains collections of stable rotating modules more cheaply than a single larger condensate. The cosmic web is the expected steady-state output of a substrate that penalises monolithic aggregation superlinearly.

21.2 Quantisation as Stability Selection

The free-energy landscape of the condensation functional does not permit arbitrary stable configurations. The scans converge on discrete preferred states separated by energetically unfavourable intermediate configurations: the three-core at $E=0.900$ model units, the four-unit bound system at $E=1.400$, and the 3+e post-expulsion state at $E=0.8958$. These are stability attractors, not continuous possibilities.

The connecting identity $E_{\text{gap}}/m_e = 45.00$ is a direct quantitative expression of this discreteness:

The electron mass is the unique stable outcome of the interstitial three-sphere geometry within the substrate geometry. E_{unit} cancels from both sides, leaving a pure geometric ratio. Quantisation of the electron mass is therefore a consequence of the discrete geometry of the three-sphere packing combined with the unique stable solution of the substrate functional. Intermediate mass values correspond to energetically unstable configurations and do not persist.

21.3 The Identity of Elementary Particles

Every electron in the observable universe has exactly the same mass, charge, and spin. Within quantum field theory this follows from field quantisation: all excitations of the electron field with the same quantum numbers are identical by construction [Weinberg 1995, The Quantum Theory of Fields, Vol. 1]. This is correct but leaves open why the field has the specific properties it has.

The BFUT account identifies identical particles as repeated realisations of the same stable substrate solution. In the displayed P16 calculation the mass relation $m_{e_vss} = m_{\square}/(6\pi^5) = 0.511009$ MeV follows from the measured proton mass and the geometric connecting identity. The charge and spin are assigned to the counter-rotation and rotational topology. These numerical results do not change with the $\rho_{\square}$ because the density is absent from their final equations.

The observed uniformity of particle properties is interpreted as repeated selection of the same stable geometric solution in a uniform substrate. P16 does not establish each particle property as an explicit numerical function of $\rho_{\square}$.

21.4 The Finite Particle Catalogue

The robustness analysis identified exactly three competing configurations at the $n=4$ threshold: 3+e preferred in 97.56% of parameter space, 2+2 preferred in 2.16%, and 4+0 preferred in 0.28%. No other configurations are available at this level. The stable particle catalogue at the first threshold therefore contains exactly three entries, of which one overwhelmingly dominates.

Seven decades of particle physics experimentation are consistent with this result. The Large Hadron Collider and its predecessors have produced hundreds of short-lived hadronic configurations, exotic multiquark states, and heavy resonances. Every one decays toward the proton-electron baseline. The substrate free-energy landscape has one deep stable minimum at the threshold level. The finite particle catalogue is not a coincidence. It is the expected output of a landscape with one dominant attractor.

21.5 Modularity and the Optimisation of Complexity

The energetic modularity principle links biological organisation, which is itself modular [3], to stable atomic modules. In the displayed calculations the proton radius is measured and the Bohr radius is obtained from measured constants and the electron mass relation. Neither radius is numerically rescaled by the p_0 in this paper.

An atom scaled to the size of a pinhead (approximately 1 mm diameter, roughly 10^7 times larger in linear dimension) would carry an energy cost per unit volume approximately 10^{21} times larger per atom. An organism built from 10^{14} such pinhead atoms would extend approximately 10^7 metres in linear dimension and require 10^{35} times more total condensation energy than a real organism of the same atom count. To bring a pinhead-atom organism back to human body volume, the atom count must be reduced by a factor of 10^{21} , leaving fewer than 10^7 atoms total - compared to 10^{14} in a real human body.

BFUT Papers 20 and 21 (P20, DOI: 10.5281/zenodo.19992457; P21, DOI: 10.5281/zenodo.20025739) establish that the number and complexity of access channels within an organised system determine its position on the consciousness index. A pinhead-atom organism of human body volume would have approximately 10^7 atoms versus 10^{14} in a real human body, reducing the available access channels by a factor of approximately $(10^7/10^{14})^{2/3} = 10^{(-4.67)}$, placing its consciousness index orders of magnitude below that of a real human. [4][5]

The universe cannot produce conscious organisms of human-level complexity at pinhead atom scale. The energy constraints of the substrate force convergence on specific atom sizes that maximise stable modules per unit energy, which in turn maximises access channels per unit volume, which in turn maximises the achievable consciousness index. The actual size of the atom is the size selected by the substrate to maximise the complexity of the structures that can be assembled from it. The quantitative derivation of the atom-size to consciousness-index relationship is given in the companion simulation programme. [5]

22. Conclusion

The reusable particle-sector output of the condensation functional consists of R_0 , A, B, C, D, the derivative hierarchy at R_0 , $D = 2A = 1$, the $n = 3$ three-core, the selected $n = 4$ 3+e topology, the $n^2 = 16$ four-unit reconfiguration count, E_{unit} , $\hbar_{\text{vss}}$, α_{vss} , $m_{\text{e_vss}}$, and the common

three-core mass scale $M = m_{\square}/3$. These quantities are properties of the P16 condensation chain and are carried into later BFUT particle-sector calculations.

The present paper gives the strongest BFUT pre-hydrogen bridge built so far. The paper extends beyond a static threshold table by integrating a substrate nucleation layer, a repeated-first-unit threshold layer, and a dynamic assembly layer. The result is a constructive existence proof that a single first-unit emergence logic can carry the system from the Sparticle field to ordinary hydrogen as the first atom.

Three additional results follow from the same stability analysis: the stability filter identifies the 2 to 10% of parameter space that produces unstable quarks; the cancellation wave mechanism identifies the substrate rebound of those unstable excitations as the physical origin of antiparticles and the mechanism of annihilation; and the observable universe becomes matter-dominated as the natural output of the stability filter operating universally and continuously.

This paper establishes the theoretical architectural transition at the quark-upward level. The substrate-to-first-unit field derivation proceeds through the Sparticle Lagrangian established in the present BFUT construction.

The significance of the P16 framework extends beyond the derivation itself. The experimentally observed behaviour of matter across the entire history of particle physics is structurally consistent with the stability hierarchy derived here. Ordinary hydrogen and proton-electron matter remain stable when produced in laboratory environments, while experimentally observed exotic multiquark configurations remain unstable and decay. The Standard Model describes these behaviours through multiple separate mechanisms including confinement, gauge symmetries, conservation laws, spontaneous symmetry breaking, Higgs interactions, vacuum structure, baryogenesis models, and effective field treatments. The BFUT framework instead derives the observed hierarchy from a single substrate-level stability-selection principle. Across all experimentally explored accelerator energies so far, no confirmed stable matter configuration has contradicted the stability-filter prediction derived in this paper.

The Full Five-Term Functional and Robustness Scans

1. The Full Five-Term Functional

The BFUT condensation energy functional has five terms. Each term encodes a distinct physical mechanism. Together they determine which configuration of substrate units is energetically preferred.

The full functional evaluated for a configuration of n units with k co-rotating:

$$E = \text{coop} + \text{imb} + \text{geom} + \text{c3ph}$$

1.1 Term by Term

Term 1 - Cooperation (coop)

$$\text{coop} = -J \times \text{pairs_sum}(s)$$

$$\text{pairs_sum}(s) = \text{sum of } s_i \times s_j \text{ over all distinct pairs } i < j$$

Physical meaning: Co-rotating units attract each other by the Bernoulli mechanism. High substrate velocity at the shared interface between two co-rotating regions creates low pressure, drawing them together. The cooperation energy grows with the number of co-rotating pairs.

k co-rotating	Pairs	Binding energy
1	0	0 (no pairs, unstable)
2	1	$-J = -1.0$ (marginal)
3	3	$-3J = -3.0$ (qualitative jump - first stable nucleus)
4	6	$-6J = -6.0$

The jump from $k=2$ (one pair, $-J$) to $k=3$ (three pairs, $-3J$) is qualitative not gradual. This is why the 3-core is the first stable nucleus. Below $k=3$ the core cannot survive substrate fluctuations.

Term 2 - Imbalance Penalty (imb)

$$\text{imb} = \lambda \times (\text{sum}(s))^2$$

Physical meaning: A net circulation asymmetry costs energy. If all units circulate in the same direction, $\text{sum}(s) = n$ and the penalty is large. The balanced 2+2 configuration has $\text{sum}(s) = 0$ and zero penalty. The 3+1 configuration has $\text{sum}(s) = 3-1 = 2$, giving a moderate penalty $\lambda \times 4 = 2.4$.

Term 3 - Geometric Cost (geom)

$$\text{geom} = (k-3)^2 + \alpha \times (n-k)$$

Physical meaning: Two independent geometric costs. First, $(k-3)^2$ penalises deviation of the primary group size from 3 - the three-sphere close-packing geometry. Second, $\alpha \times (n-k)$ penalises each counter-circulating unit for the geometric asymmetry it introduces. When the expelled unit has mass fraction μ , this term scales as $\alpha \times \mu$.

Term 4 - Circulation Phase Reward (c3ph)

$$\text{c3ph} = D_s \times \cos(3 \times \varphi)$$

Physical meaning: The fifth term explicitly encodes the topology of the three-sphere packing into the energy functional. The phase φ measures the circulation configuration:

Config	φ	$\cos(3\varphi)$	$\text{c3ph} = D_s \times \cos(3\varphi)$	Effect
3+1	$\pi/3$	-1	$-D_s = -1.5$	Rewarded
2+2	$\pi/2$	0	0	Neutral
4+0	0	+1	$+D_s = +1.5$	Penalised

D_s must be positive. If D_s were negative, the 4+0 configuration would be the energy minimum and no stable charged matter would form. The fifth term raises $E(4+0)$ from 4.60 to 6.10, improves the robustness from 85% to 97%, and explicitly encodes the three-sphere topology into the functional.

1.2 Parameters

Symbol	Value	Name	Physical role
J	1.0	Cooperation strength	Bernoulli binding per co-rotating pair
λ	0.6	Imbalance penalty	Cost of net circulation asymmetry
α	0.5	Geometric asymmetry	Cost per counter-circulating unit (scales with μ for expelled unit)
D_s	1.5	Phase reward	$\cos(3\varphi)$ circulation topology reward. Must be positive.

2. The Per-Unit Energy Scan (Code 1)

Code 1 answers: for n co-rotating substrate units, which n minimises energy per unit $E(n)/n$? All units are at the primary phase $\varphi = \pi/3$, so $\cos(3\varphi) = -1$ and $\text{c3ph} = -D_s$ for all n .

n	$E(n)$	$E(n)/n$	Note
1	3.1000	3.1000	No pairs. Unstable.

2	0.9000	0.4500	One pair. Marginal.
3	0.9000	0.3000	MINIMUM E/unit. The 3-core attractor.
4	3.1000	0.7750	
5	7.5000	1.5000	Rising steeply
6-12	...	...	Continues to rise

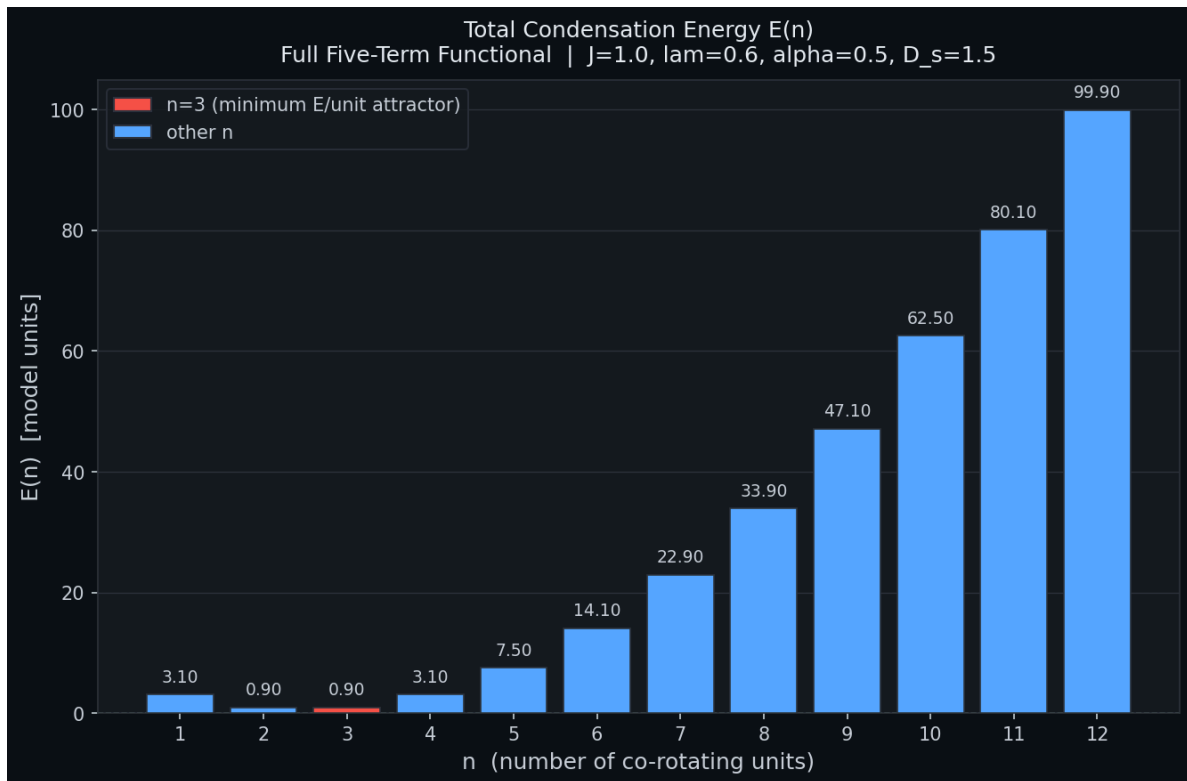


Figure A. Total condensation energy $E(n)$ for $n=1$ to 12. $n=3$ highlighted.

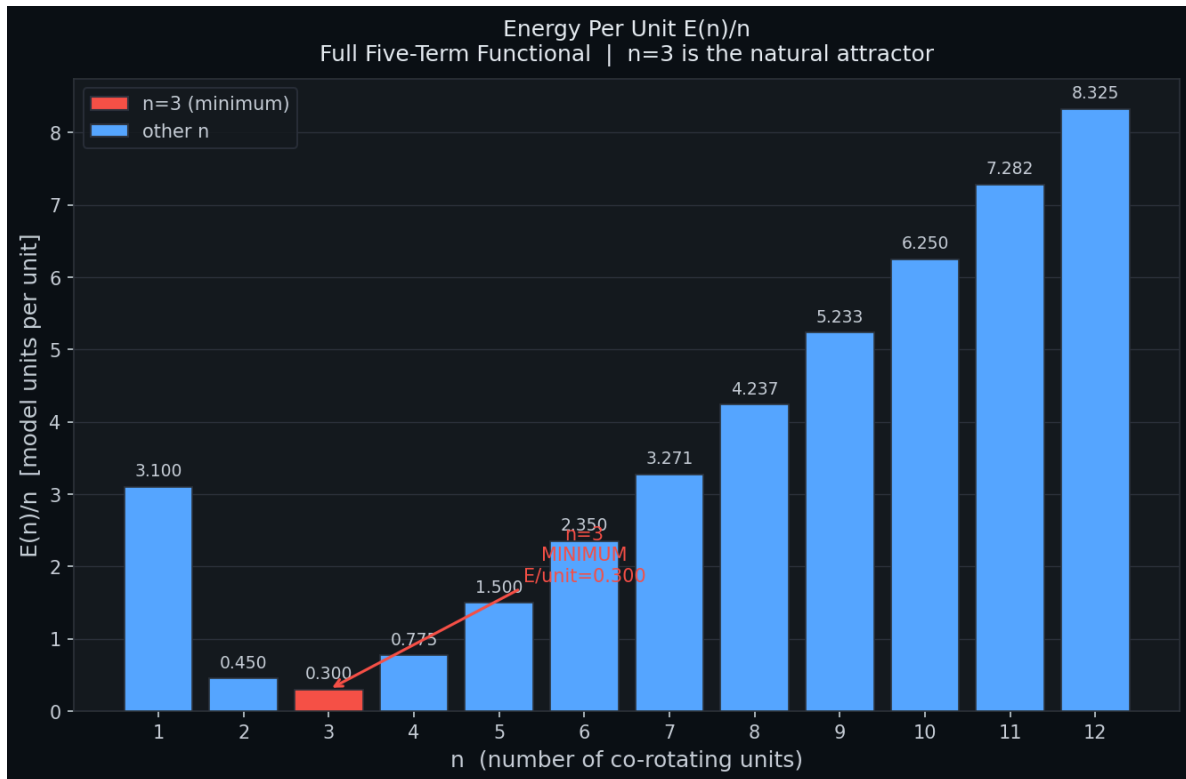


Figure B. Energy per unit $E(n)/n$ for $n=1$ to 12. $n=3$ is the unambiguous minimum.

3. The Four-Unit Partition (Post 3-Core Formation)

The moment $n=3$ forms, the three-sphere packing geometry simultaneously creates the interstitial region. The four-unit bound system forms at $E=1.400$ model units. The three configurations and their full-functional energies:

Config	E (model units)	$\cos(3\phi)$	Status
3+1	1.4000	-1 (rewarded)	MINIMUM. SELECTED.
2+2	4.0000	0 (neutral)	Symmetric. No net charge.
4+0	6.1000	+1 (penalised)	All co-rotating. Penalised by D_s .

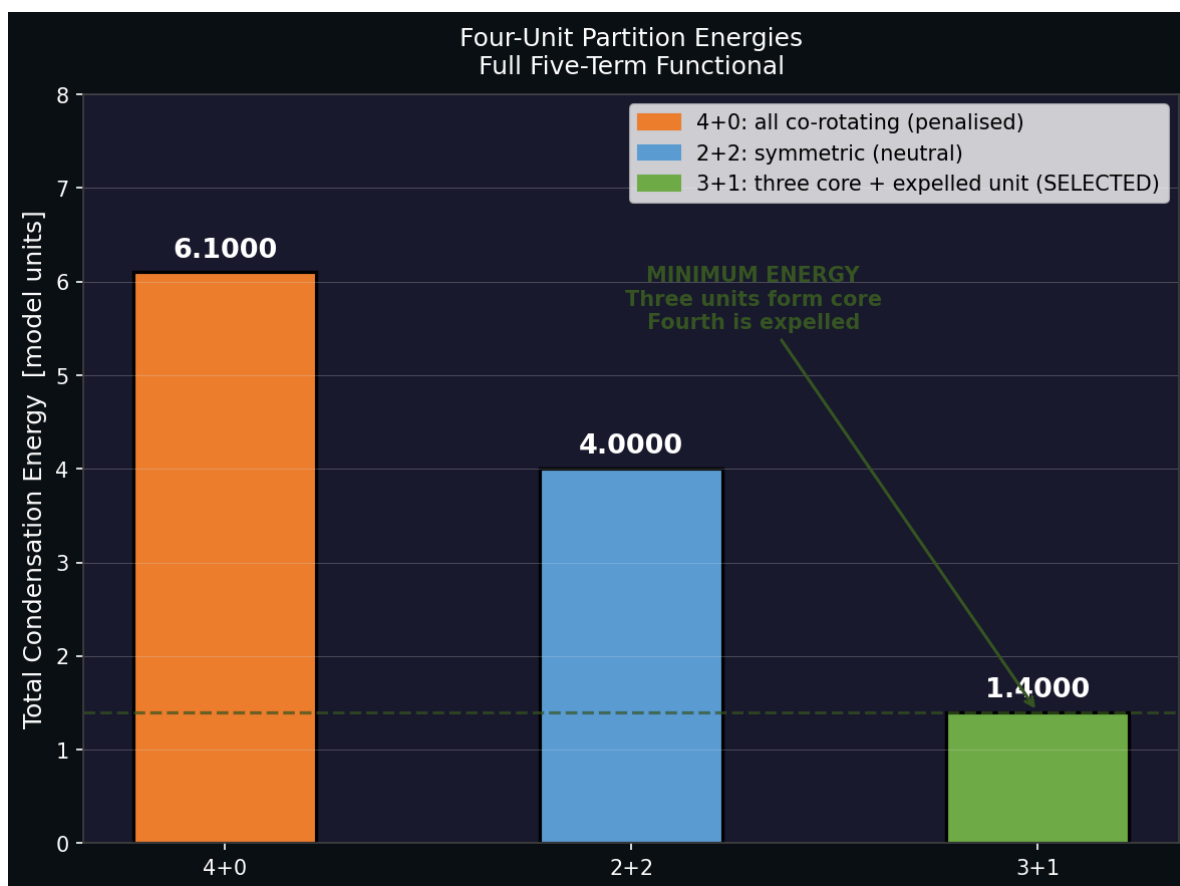


Figure C. Four-unit partition energies. 3+1 is the clear minimum.

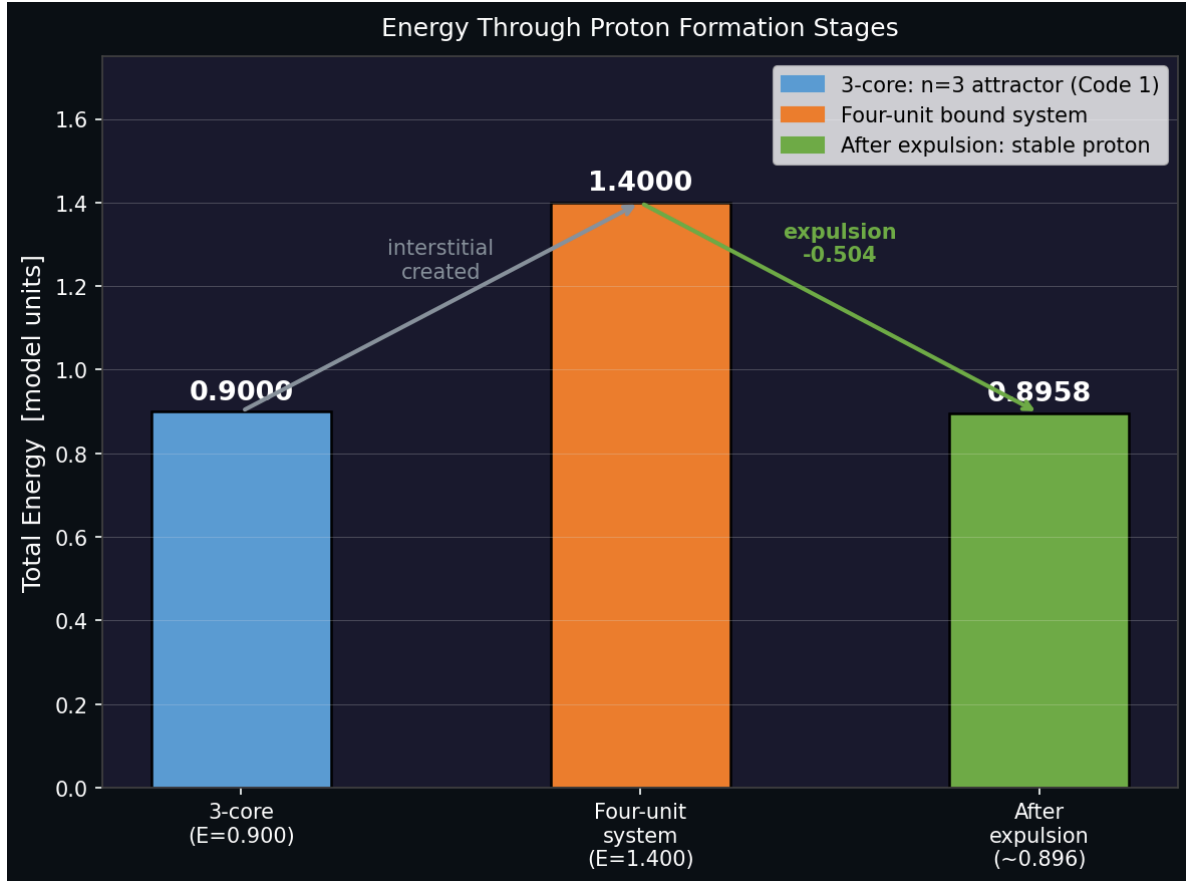


Figure D. Energy through the three stages of proton formation.

4. Three-Sphere Packing Geometry

Three substrate condensations of radius r_q in close-packed contact. The three centres form an equilateral triangle of side $2r_q$. The outer radius of the assembly equals r_p , the measured proton charge radius. This is the only measured input.

$$r_{\text{outer}} = r_q \times (1 + 2/\sqrt{3}) = 2.1547 \times r_q = r_p$$

$$r_q = r_p / (1 + 2/\sqrt{3}) = 0.8414 / 2.1547 = 0.3905 \text{ fm}$$

$$V_{\text{gap}} / V_q = (2\sqrt{3} - \pi) / (4\pi/3) = 0.0770$$

Both results are universal geometric constants. No free parameters.

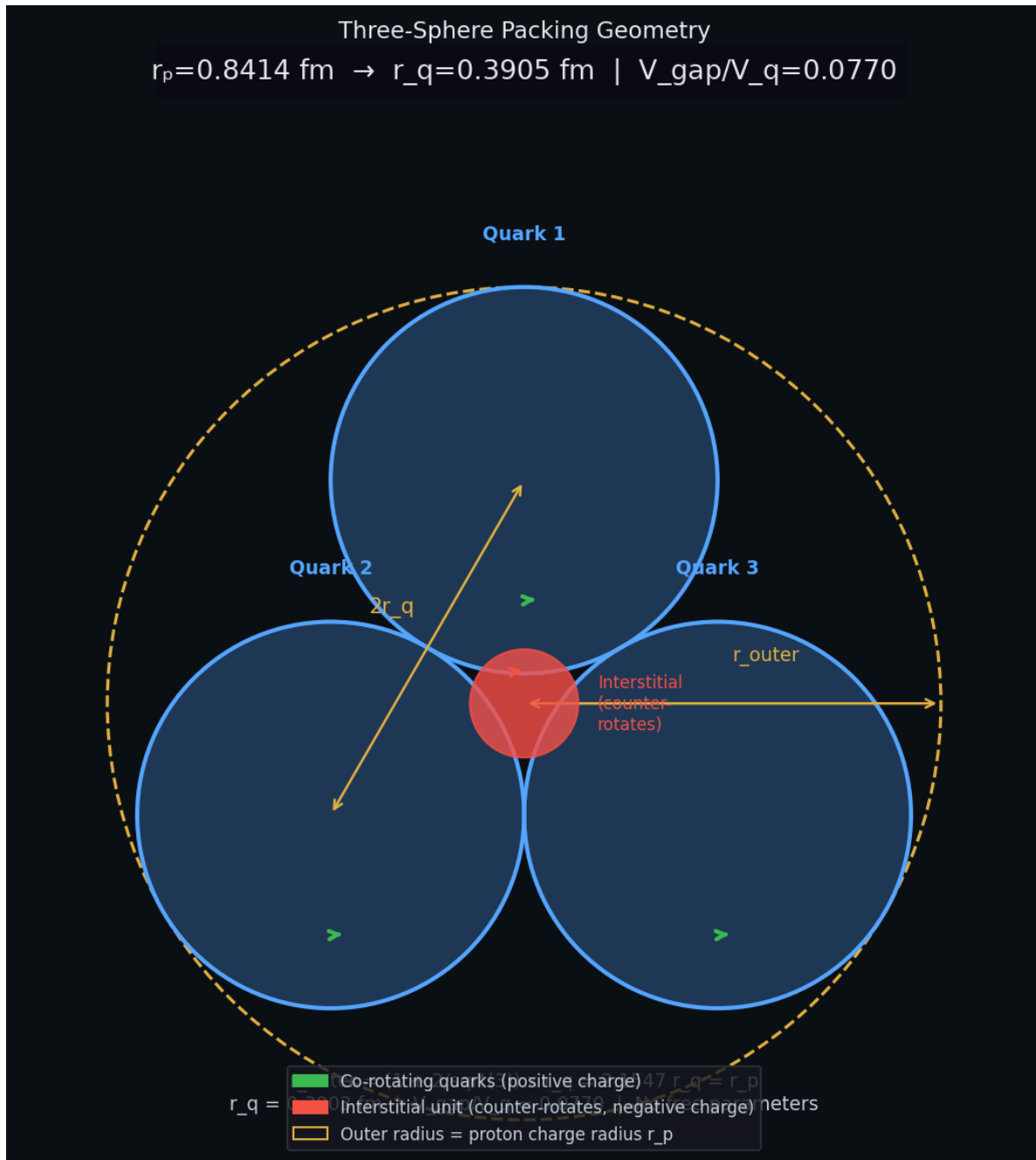


Figure E. Three-sphere packing geometry. Green arrows: co-rotating quarks. Red: interstitial unit (counter-rotates). Yellow dashed: outer radius = r_p .

5. Why the Interstitial Unit Counter-Rotates

The counter-rotation is mechanically imparted, not assumed. When the interstitial substrate exits through the gap between any two quarks, it encounters two co-rotating surfaces - one on each side. Both quarks rotate in the same direction. Each imparts a tangential force in the opposite direction to the passing substrate. Together they impart a net counter-clockwise torque.

This is the gear analogy: a gear placed between two co-rotating gears of the same handedness always rotates in the opposite direction. The result is the same regardless of which gap the substrate exits from, because all three quarks rotate in the same direction.

Counter-rotation in BFUT is the definition of opposite charge. The negative charge of the expelled unit is therefore not assigned or assumed. It is mechanically imparted during expulsion by the same co-rotation that defines the quarks as positively charged.

6. Proton Energy with Interstitial Unit

When the detached unit has mass fraction μ relative to a core unit, the P16 functional is evaluated with $s = [+1, +1, +1, -\mu]$. The geometric asymmetry term scales with μ because the geometric displacement is proportional to the actual mass of the detached unit:

$$E(\mu) = -J \times \text{pairs_sum}([1, 1, 1, -\mu]) \\ + \lambda \times (3-\mu)^2 \\ + (3-3)^2 + \alpha \times \mu \\ + D_s \times (-1)$$

At $\mu=1.0$ (standard 3+1): $E = 1.4000$ model units (baseline confirmed)

Minimum: $E = 0.8958$ model units at $\mu = 0.083$

Driving force for expulsion: -0.504 model units

μ	$E(\mu)$	Reduction from 1.400	Note
1.000	1.4000	0.0000	Standard 3+1 baseline
0.500	1.0000	-0.4000	
0.230	0.9087	-0.4913	P19 upper bound
0.083	0.8958	-0.5042	MINIMUM
0.077	0.8959	-0.5041	P19 lower bound

The result is robust across the full physical range $\mu = 0.077$ to 0.23 . Proton stability does not depend on fine-tuning the interstitial mass fraction.

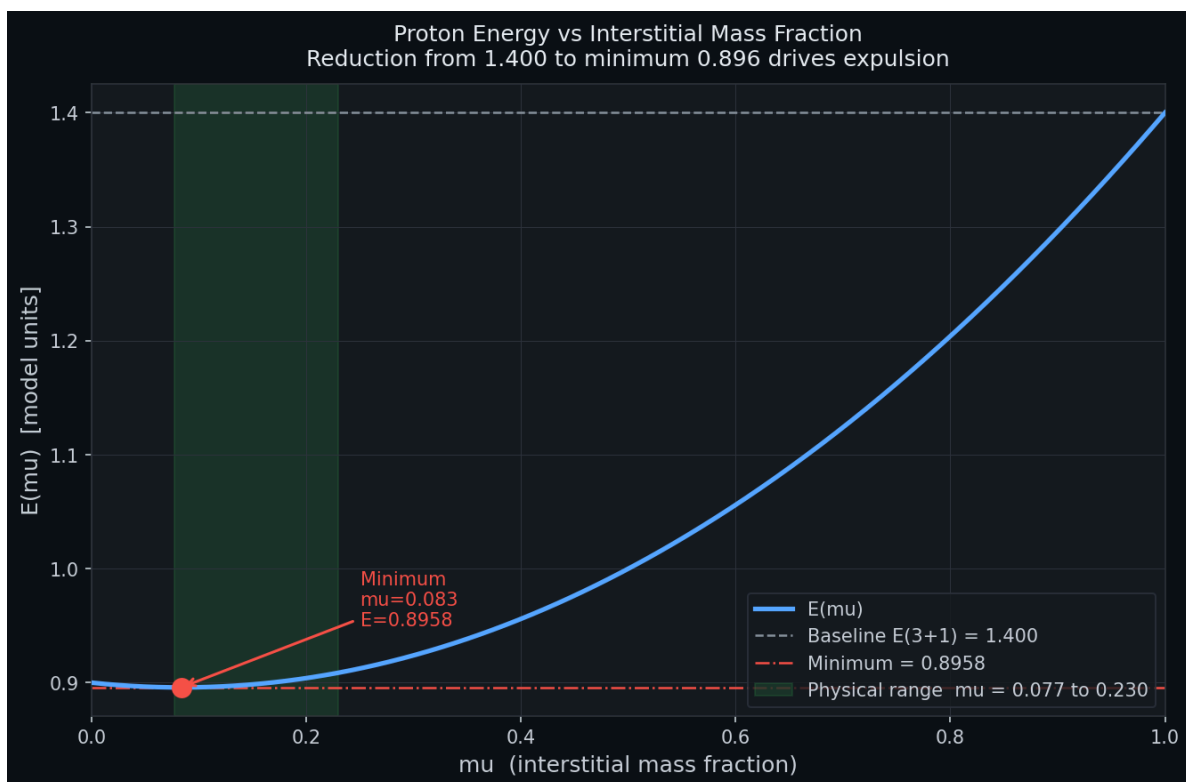


Figure F. $E(\mu)$ vs μ across the full range 0 to 1. Minimum at $\mu=0.083$. Green band: physical range.

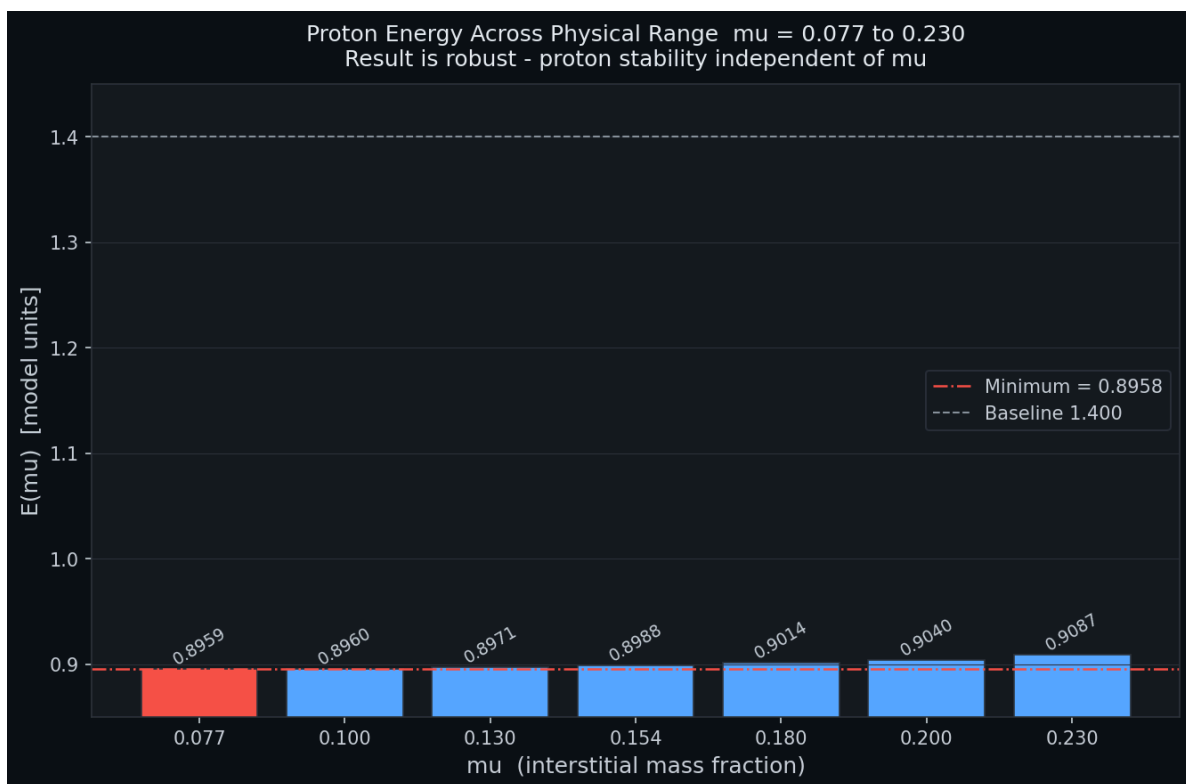


Figure G. Proton energy across the physical range $\mu=0.077$ to 0.230 . Result is robust.

7. The Connecting Identity

P19 Section 21.6 establishes an exact algebraic identity connecting the interstitial volume fraction, the electron mass, and the compression energy. E_{unit} cancels exactly - the identity is purely geometric:

$$E_{\text{gap}} = E_{\text{unit}} \times V_{\text{gap}}/V_{\text{q}} = 298.661 \times 0.0770 = 22.999 \text{ MeV}$$

$$m_{\text{e}} = E_{\text{unit}} / (6 \times \pi^4) = 298.661 / 584.45 = 0.511009 \text{ MeV}$$

$$E_{\text{gap}} / m_{\text{e}} = 6 \times \pi^4 \times V_{\text{gap}}/V_{\text{q}} = 584.45 \times 0.0770 = 45.00$$

Physical meaning: The expelled substrate dissipates 44/45 of the compression energy into the surrounding substrate during proton stabilisation. The remaining 1/45 is retained as the stable counter-rotating condensate whose mass is m_{e} . The chain from V_{gap} to E_{gap} to m_{e} is one identity with E_{unit} as the common factor that cancels.

The Connecting Identity: Interstitial Geometry to Electron Mass (P19 Section 20.5b)		
[INPUT]	$r_p = 0.8414 \text{ fm}$	Measured proton charge radius
[GEOMETRY]	$r_q = r_p / (1+2/\sqrt{3}) = 0.3905 \text{ fm}$	Three-sphere packing (no free parameters)
[GEOMETRY]	$V_{\text{gap}}/V_{\text{q}} = (2\sqrt{3}-\pi)/(4\pi/3) = 0.0770$	Universal geometric constant
[MASS]	$E_{\text{unit}} = m_p c^2 / \pi = 298.661 \text{ MeV}$	Proton mass formula
[MASS]	$m_{\text{e, but}} = E_{\text{unit}} / (6\pi^4) = 0.511009 \text{ MeV}$	Electron mass (measured: 0.511000 MeV)
[MASS]	$E_{\text{gap}} = E_{\text{unit}} \times V_{\text{gap}}/V_{\text{q}} = 22.995 \text{ MeV}$	Compression energy in interstitial gap
[MASS]	$E_{\text{gap}} / m_{\text{e, but}} = 6 \times \pi^4 \times V_{\text{gap}}/V_{\text{q}} = 45.00$	Compression energy in interstitial gap
[IDENTITY]	44/45 of E_{gap} dissipated into substrate	E_{unit} cancels - pure geometric identity
[MEANING]	1/45 of E_{gap} retained = condensate	Energy released during proton stabilisation
[MEANING]	$E_{\text{unit}} = 298.661 \text{ MeV} \mid 0.511009 \text{ MeV} \mid E_{\text{gap}} = 22.995 \text{ MeV} \mid E_{\text{gap}}/m_{\text{e, but}} = 45.00$	

Figure H. The connecting identity chain from measured r_p to m_{e} . E_{unit} cancels at the IDENTITY step.

8. Modular Organisation: The Universal Structural Unit

For any $n > 4$ substrate units, multiple modular units are always energetically preferred over a single large condensate. The energy advantage grows with n . At $n=24$ the gap is 34.5 model units.

n	E single	k_opt	m x 1.400	Gap	Winner
4	1.400	3	1.400	0.000	EQUAL
5	2.100	3	1.750	+0.350	MODULAR
8	5.400	3	2.800	+2.600	MODULAR
12	11.100	4	4.200	+6.900	MODULAR
24	42.900	6	8.400	+34.500	MODULAR

The single condensate is free to choose any primary group size k . It chooses $k=3$ for $n=4$ to 8, then $k=4$, then $k=5$. It loses anyway. The modular unit is the universal preferred structural unit for matter at all scales.

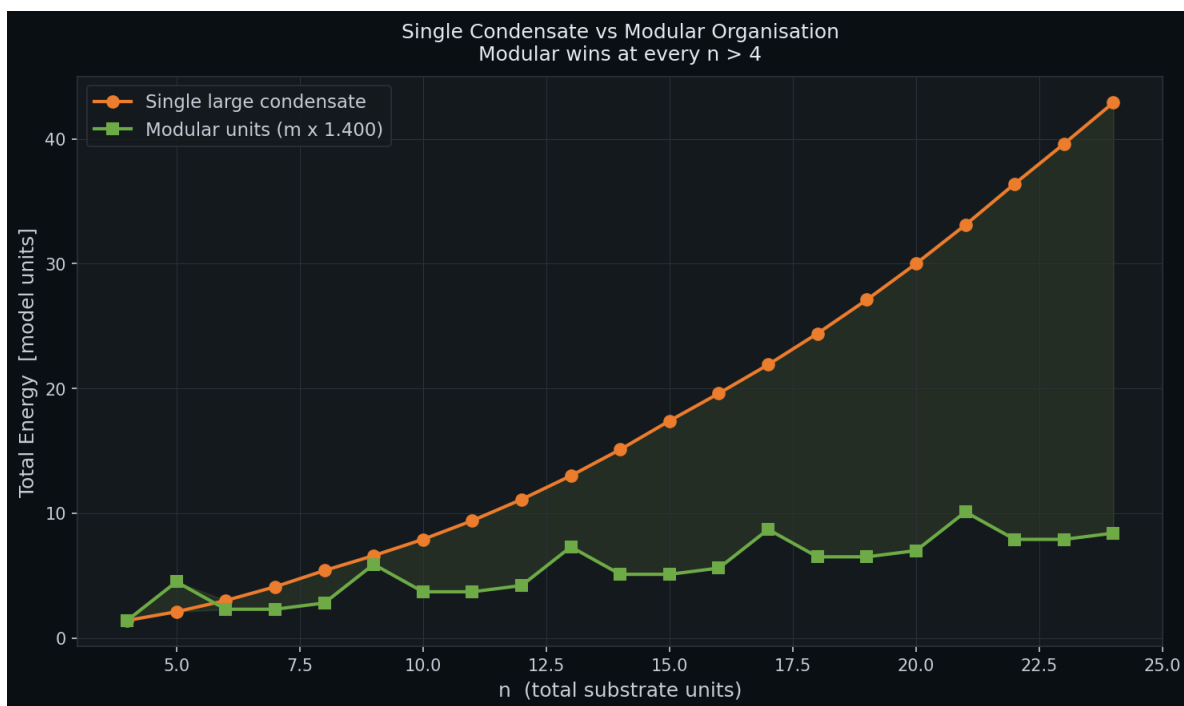


Figure I. Total energy: single condensate vs modular units for $n=4$ to 24.

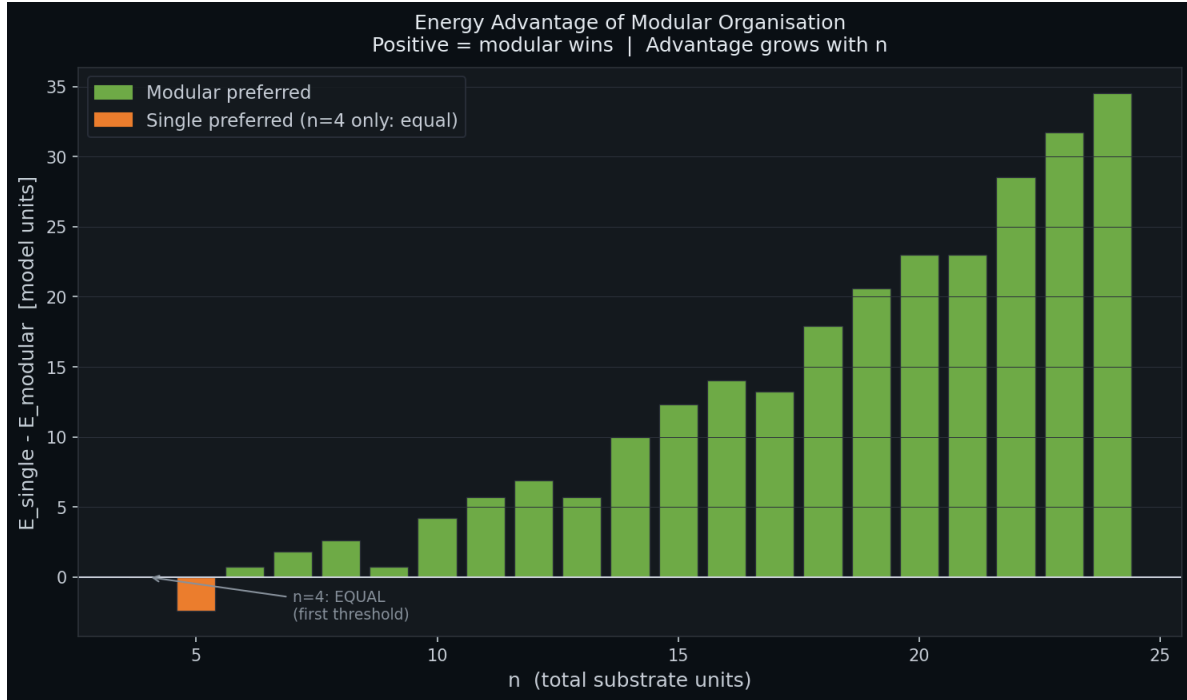


Figure J. Energy advantage of modular organisation. Positive = modular wins. Gap grows with n.

9. Robustness: Parameter Space Analysis

The 3+1 selection is not a fragile result at a single parameter point. Scanning λ and α across $[0.2, 1.2]$ with $J=1.0$ fixed:

Scan	3+1 wins	Parameters varied
1D	97.56%	λ in $[0.2, 1.2]$
2D	95.95%	$\lambda \times \alpha$ in $[0.2, 1.2]^2$
3D	90.43%	$\lambda \times \alpha \times D_s$ in $[0.2, 1.2]^2 \times [0.5, 2.5]$

Comparison with the four-term baseline (without $\cos(3\phi)$ term):

Scan	Four-term	Five-term	Improvement
1D	85.37%	97.56%	+12.19%
2D	83.82%	95.95%	+12.13%
3D	80.84%	90.43%	+9.59%

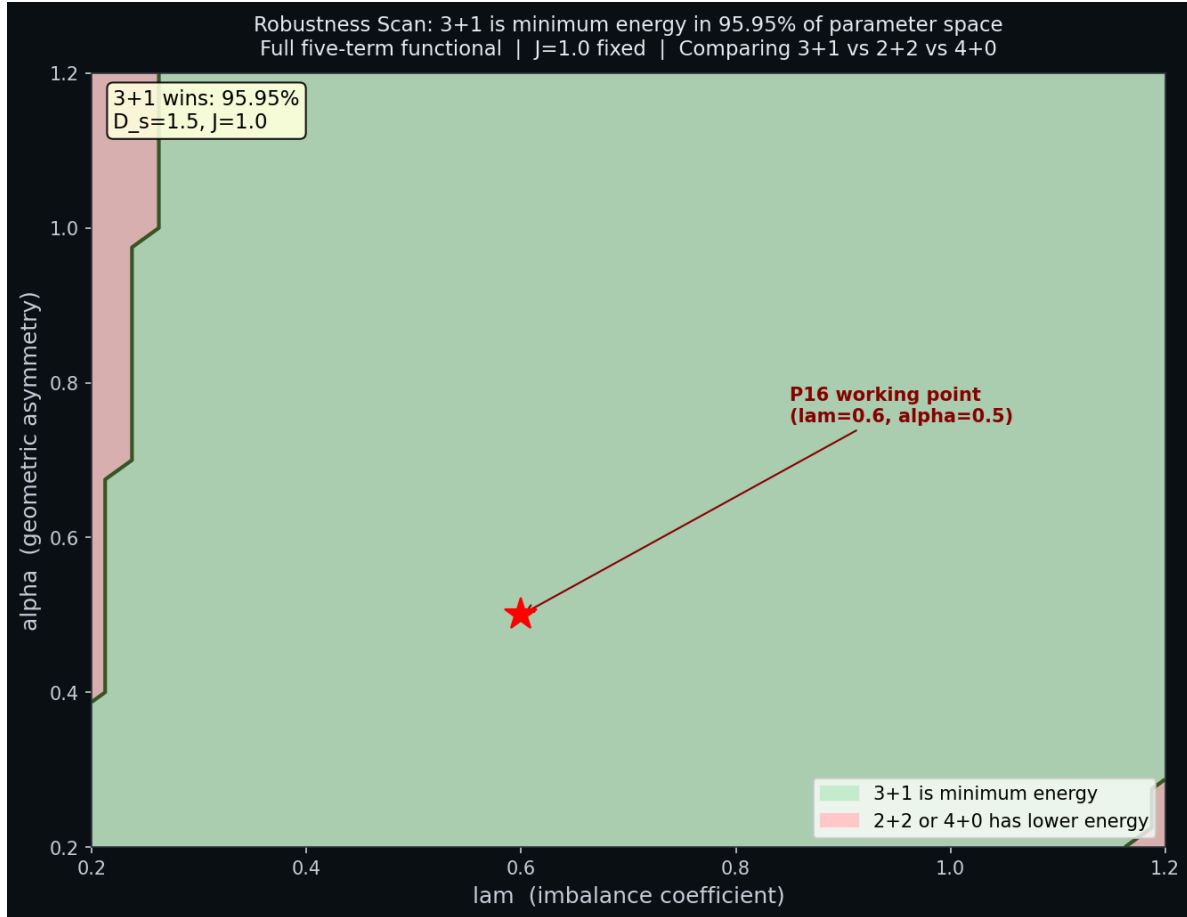


Figure K. Parameter space map. Green: 3+1 is minimum energy. Red: other configuration wins. P16 working point marked.

10. All Key Results at a Glance

Quantity	Value	Source
r_p	0.8414 fm	CODATA 2018 measurement
r_q	0.3905 fm	Three-sphere geometry
V_{gap} / V_q	0.0770	Universal geometric constant
$E_{\text{unit}} = m_p/\pi$	298.661 MeV	Proton mass formula
$m_e = E_{\text{unit}}/(6\pi^4)$	0.511009 MeV	Electron mass (measured: 0.510999)
E_{gap}/m_e	45.00	Connecting identity - E_{unit} cancels
$E(3+1)$ baseline	1.4000 model units	P16 functional, standard 3+1
E minimum ($\mu=0.083$)	0.8958 model units	P16 functional, interstitial expelled
Driving force	-0.504 model units	Energetic basis for expulsion

2D robustness	95.95%	Five-term functional scan
Confinement F	0.574 GeV/fm	vs QCD 0.900 GeV/fm (36%)

Appendix B

Appendix

Applications and Derived Results of the Spaticle Field

This appendix lists independently meaningful physical applications, derived results, predictions, and observational applications that have a direct derivational or physical chain to the Spaticle Field or its derived density. Intermediate mathematical calculations are not listed as separate applications. Source papers are identified by their P-numbers, including P14 [8], P17 [11], P18 [12], P19 [13], and P19A [14].

SN	Application / Derived Result	Physical result or BFUT application	BFUT source
1	Spaticle-field equilibrium density	Intrinsic substrate density $\rho = 7.3 \times 10^{-27} \text{ kg/m}^3$, obtained from the condensation framework and used as the common physical substrate parameter.	P16; P25; P78
2	Matter creation from the Spaticle Field	Matter condenses from the physical Spaticle Field and remains embedded in it. This provides the substrate basis for the particle and matter structures developed throughout BFUT.	P14; P16; P17
3	Propagation of forces and physical disturbances through the Spaticle Field	Forces and physical disturbances propagate through the Spaticle Field. This supplies the common physical carrier underlying the electromagnetic, gravitational, weak, and strong interaction descriptions.	P14; P17; P18; P23
4	Stable condensation equilibrium	The condensation functional produces a finite non-zero equilibrium condensation scale R_0 for stable matter structures.	P16
5	Proton condensation structure	The three-core condensation architecture produces the structural basis for proton formation.	P16
6	3+e proton structure	The stable 3+e organisation supplies the particle architecture used in the proton and electron formation chain.	P16; P17
7	Electron mass	The BFUT particle chain derives electron mass from the proton-scale condensation construction.	P16; P19
8	Matter-antimatter structure and annihilation	Matter and antimatter are treated as corresponding substrate condensation configurations, with annihilation arising from cancellation of opposing organised excitations and release of condensation energy.	P16; P16A
9	Antihydrogen structure and CERN comparison	The BFUT antimatter construction gives a mirror configuration for antihydrogen and provides a framework for comparison with CERN antihydrogen measurements.	P16A
10	Stability filter for matter and antimatter	The stability filter identifies which condensation configurations can persist as stable matter or antimatter structures.	P16; P16A
11	Emergence of the fundamental forces	Gravity, strong, electromagnetic, and weak interactions are derived as distinct physical disturbance or organisation channels associated with the substrate and 3+e matter structure.	P17

SN	Application / Derived Result	Physical result or BFUT application	BFUT source
12	Gravity as substrate deformation and restoring response	Gravitational attraction is described as the restoring response of the Sparticle Field to matter-induced deformation.	P17; P18
13	Covariant carrier-field equation	F1-cov provides the covariant substrate equation governing gravitational deformation and propagation.	P18
14	Density-derived carrier scale	The substrate density fixes the carrier scale $\mu_\square$ and its associated propagation/screening scales.	P18
15	Finite gravitational deformation domain	For source mass M, BFUT gives a finite deformation-domain radius $R_d = [3M/(8\pi\rho_\square)]^{1/3}$.	P18; P22; P26
16	Rotationally enlarged deformation domain	The effective deformation domain incorporates the rotational correction defined by the BFUT carrier model.	P18
17	Carrier relaxation length and timescale	The carrier framework supplies finite response and relaxation scales for substrate deformation.	P18; P26
18	Cosmological screening length	The density-derived carrier mass establishes a finite cosmological screening scale for the static carrier field.	P18
19	BFUT gravitational acceleration scale	The characteristic acceleration $a_\square$ is derived from the substrate density, G, and c.	P18; P78
20	Finite-domain gravity across physical regimes	The finite deformation-domain carrier is formulated for quantum, classical, galactic, and rapid-transition regimes, providing a common and testable gravitational description across those scales.	P18
21	Dark Matter Effects interpretation	The gravitational effect conventionally attributed to dark matter is represented in BFUT by organised or entrained Sparticle-field structure.	P18; P25; P78
22	Dark Matter Effects equation	The DME relation derives the additional rotational contribution from the baryonic distribution and the substrate-derived acceleration scale without modifying Newtonian gravity.	P18; P25; P78
23	SPARC rotation-curve validation	DME is applied to the 175-galaxy SPARC sample using the same substrate-derived acceleration scale and published baryonic inputs.	P25; P78
24	KiDS-1000 weak-lensing validation	DME is applied to the KiDS-1000 stacked weak-lensing mass bins using the same substrate-derived acceleration scale.	P25; P78
25	Additional galaxy-system tests	DME is tested against additional named systems, including low-dark-matter and ultra-diffuse systems in the observational programme.	P25; P78
26	Merger morphology and substrate entrainment	Merger systems are interpreted through the redistribution and entrainment of substrate-associated mass during interaction.	P78
27	Low-rotation systems	Systems with negligible organised rotation provide a regime in which the substrate contribution predicted by the rotational DME mechanism is correspondingly reduced.	P25; P78
28	Sunyaev-Zel'dovich effect	P10 gives a Sparticle-field interpretation of the SZ effect through interaction of propagating substrate modes with the thermal electron population.	P10; P25

SN	Application / Derived Result	Physical result or BFUT application	BFUT source
29	Lyman-alpha forest	P11 interprets the Lyman-alpha absorption forest through the interaction of propagating structures with the substrate and the absorption-percolation threshold.	P11; P25
30	Integrated Sachs-Wolfe effect	P12 attributes the ISW temperature contribution to variations in Sparticle-field density encountered by photons along their path.	P12; P25
31	Weak-lensing S8 application	P13 connects the weak-lensing S8 result and suppressed late-time structure growth to the physical substrate and its domain dynamics.	P13; P25
32	CMB acoustic peaks	The BFUT cosmological substrate framework models acoustic structure through ongoing shell processes in the physical substrate and reproduces CMB-like peak structure in the reported proof-of-principle treatment.	P12; P25
33	BAO-like feature	The same cosmological substrate treatment produces a BAO-like feature in the reported proof-of-principle simulation.	P12; P25
34	Fine-structure constant	The fine-structure constant α is derived from the BFUT condensation and electromagnetic circulation structure.	P19; P27
35	Strong coupling constant	The strong coupling α_s is derived from the P16 condensation parameters and evaluated at the Z-boson mass scale.	P19
36	Weak mixing angle	The BFUT electroweak mixing quantity is obtained in P19 as an output of the independently derived W and Z resonance masses.	P19
37	W-boson mass	The charged W resonance is derived in P19 as $m_{W_vss} = 256M = (256/3)m_\square = 80.066 \text{ GeV}/c^2$, from $n^2 = 16$ and the per-core mass $M = m_\square/3$.	P19; P25
38	Z-boson mass	The neutral Z core-stay resonance follows from the proton-scale condensation chain: $m_{Z_vss} = \pi^*m_\square = 91.396 \text{ GeV}/c^2$. No mixing angle enters this mass relation.	P19; P25
39	H-class radial resonance mass	The radial H resonance follows from $\lambda_{H_vss} = 2AR_0/\pi^2$ and $v_{vss} = 6E_{\text{unit}}/\alpha_{vss}$: $m_{H_vss} = v_{vss}\sqrt{2\lambda_{H_vss}} = 124.75 \text{ GeV}/c^2$.	P19
40	H-class state as a radial resonance	The observed H-class state is a radial resonance of the one Sparticle field; BFUT introduces no separate Higgs field.	P19A
41	Four-unit configuration energies	The P16 four-unit functional gives $E(3+1) = 1.40$, $E(2+2) = 4.00$ and $E(4+0) = 6.10$, with 3+1 as the selected persistent topology.	P16
42	Quark-mass hierarchy	The particle programme derives the quark-mass hierarchy from the condensation and circulation architecture.	P19; P19A
43	Hydrogen Bohr radius	BFUT-derived particle and action quantities are used in the atomic relation for the hydrogen ground-state radius.	P16; P25
44	Hydrogen ground-state binding energy	The BFUT atomic construction gives the hydrogen ground-state binding energy.	P16; P25
45	Atomic stability	The finite condensation structure and substrate density are connected to the persistence of atomic structure.	P25

SN	Application / Derived Result	Physical result or BFUT application	BFUT source
46	Molecular and chemical stability	P25 derives sensitivity of atomic and molecular structure to the substrate density, including a density threshold associated with disruption of chemical bonding.	P25
47	Electron reference length	The electron reference length is an independently meaningful electromagnetic length scale used in the BFUT particle-sector construction and connected to the substrate-derived particle parameters.	P19; P78
48	Reduced Planck constant	The reduced Planck constant is derived from proton mass, proton charge radius, c , and the condensation minimum R_0 : $\hbar = m_p c r_p / (\pi R_0)$.	P16; P27
49	Planck constant	Planck's constant follows as $h = 2\pi\hbar$ and supplies the action quantum used in BFUT quantum relations.	P16; P27
50	Minimum circulation quantum	The minimum angular-momentum scale $\hbar/2$ is connected to the 720° restoration topology of the matter condensation.	P19A; P27
51	Compton wavelength	The Compton wavelength is expressed using the BFUT action scale and particle parameters.	P27
52	de Broglie wavelength	The de Broglie wavelength is expressed using the BFUT action scale and particle momentum.	P27
53	Harmonic-oscillator energy levels	The harmonic-oscillator spectrum is expressed using the BFUT-derived $\hbar$ and the corresponding quantum action scale.	P27
54	Planck length	The Planck length is derived from the BFUT $\hbar$ together with G and c .	P27
55	Planck mass	The Planck mass is derived from the BFUT $\hbar$ together with G and c .	P27
56	Planck time	The Planck time is derived from the BFUT $\hbar$ together with G and c .	P27
57	Vacuum energy density	The equilibrium substrate rest-energy density is $u_{vac} = \rho_0 c^2$.	P25; P27
58	Schrödinger equation	The time-dependent Schrödinger equation is derived as the non-relativistic limit of the covariant substrate carrier equation.	P19A; P27
59	Born rule	The Born probability $P(x)= \psi(x) ^2$ is given a physical substrate interpretation through deformation-energy density and measurement interaction.	P19A
60	Heisenberg uncertainty principle	The uncertainty scale is connected to the finite localisation and action scale of substrate condensations.	P19A; P27
61	Half-integer spin	Half-integer spin is derived from the 720° restoration topology of the matter condensation.	P19A; P27
62	Spin-statistics relation	The distinction between embedded matter condensations and propagating substrate disturbances supplies the BFUT physical interpretation of fermionic and bosonic statistics.	P19A; P27
63	Pauli exclusion principle	Pauli exclusion is explained through the impossibility of identical fermionic condensations occupying one complete circulation state.	P19A; P27

SN	Application / Derived Result	Physical result or BFUT application	BFUT source
64	Fermionic mass hierarchy	Fermionic mass structure is connected to organised circulation within the condensation architecture.	P19A
65	Gauge symmetry	U(1), SU(2), and SU(3) gauge structures are interpreted through local circulation invariance of substrate condensations.	P19A
66	Quantum superposition	Superposition is given a physical substrate interpretation as distributed organised excitation before interaction resolves the state.	P19A
67	Wave-function collapse	Wave-function collapse is interpreted as physical state resolution produced by interaction with matter in the substrate.	P19A
68	Entanglement	Entanglement is interpreted through shared coherent substrate structure and correlated physical states.	P19A
69	Quantum tunnelling	Tunnelling is represented through substrate condensation-boundary penetration, with the penetration scale determined by the BFUT action and barrier parameters.	P19A; P27
70	Decoherence	Decoherence is interpreted as loss of coherent substrate organisation through environmental interaction.	P19A
71	Quantum measurement	Measurement is treated as physical interaction between a quantum excitation and detector matter, providing the mechanism for state resolution.	P19A
72	Quantum gravity unification	Quantum behaviour and gravitation are placed within one substrate framework through the common carrier field and physical substrate.	P18; P19A
73	Quantum gate evolution	Quantum-gate unitary evolution is expressed using the BFUT-derived action scale, linking phase accumulation to substrate action.	P24; P27
74	Quantum-gate minimum time	The minimum controlled gate time is connected to the BFUT action scale and control-field energy.	P24; P27
75	Quantum-computing substrate memory	The P24 substrate-memory timescale is connected to the same substrate density that fixes the BFUT action scale.	P24; P27
76	Bell correlation	The Bell correlation function is connected to the Born rule and BFUT spin topology in the quantum-computing treatment.	P24
77	CHSH quantum bound	The BFUT quantum-computing treatment incorporates the quantum CHSH bound within its substrate interpretation of quantum correlations.	P24
78	Time as accumulated substrate evolution	Time is defined as accumulated evolution of physical states in the Sparticle substrate.	P22
79	Special-relativistic time dilation	Kinematic time dilation is derived from the finite propagation budget shared between spatial motion and internal evolution.	P22
80	Gravitational time dilation	Gravitational time dilation is derived from reduced local substrate propagation efficiency caused by gravitational deformation.	P22
81	Unified time-dilation relation	Kinematic and gravitational effects are combined through the common propagation-budget framework.	P22

SN	Application / Derived Result	Physical result or BFUT application	BFUT source
82	Length contraction	Length contraction is derived as a second consequence of the same propagation-budget constraint.	P22
83	Twin paradox	The twin paradox is resolved through the different substrate propagation histories of the two clocks.	P22
84	Clock universality	All physical clocks slow by the same factor because physical clocks are substrate processes subject to the same propagation budget.	P22
85	Photon proper time	A photon assigns its full propagation budget to spatial propagation, giving zero proper time in the BFUT formulation.	P22; P23
86	Arrow of time	The direction of time is linked to irreversible outward substrate propagation and accumulated state change.	P22
87	Simultaneity and causality	Finite substrate propagation speed supplies the physical basis for causal ordering and simultaneity relations.	P22; P23
88	Past and future asymmetry	The substrate evolution framework provides a physical account of the distinction between completed and not-yet-completed state evolution.	P22
89	Quantum time evolution	Quantum time evolution is placed within the same physical substrate evolution that defines time macroscopically.	P22; P19A
90	Equivalence principles	The weak, Einstein, and strong equivalence principles are examined within the BFUT substrate framework.	P22
91	Temporal singularity limit	Finite substrate propagation capacity supplies a temporal argument against physically reaching an infinite-density singularity.	P22; P26
92	Universal speed limit	c is identified as the maximum rate at which the Sparticle substrate can reorganise and propagate a disturbance.	P23
93	Speed of light from substrate stiffness and density	The propagation speed is derived from $c = \sqrt{(K_s/\rho)}$.	P23
94	Independent reconstruction of c	The speed of light is reconstructed, as a consistency relation of the $\hbar$ identity, from e , R_0 , ϵ_0 , m_e , r_e , and α .	P19; P23; P27
95	Massive-particle velocity deficit	A massive condensation devotes part of its physical energy budget to internal structure, leaving less capacity for spatial propagation.	P23
96	Equality of light and gravitational-wave speeds	Light and gravitational waves are disturbances of the same substrate and therefore share the same limiting propagation speed.	P23
97	Singularity impossibility	Finite substrate density and restoring dynamics prevent physical infinite density.	P26
98	Finite-density causal bound	The causal bound $\bar{\rho}_{\max} = 3c^6/(4\pi G^3 M^2)$ gives a finite mean-density limit for compact collapse.	P26
99	Finite gravitational compression	The substrate restoring mechanisms oppose unlimited gravitational compression.	P26; P28

SN	Application / Derived Result	Physical result or BFUT application	BFUT source
100	Black holes as finite gravitational vortices	Black holes are represented as finite-density gravitational vortex structures without a physical infinite-density singularity.	P6; P26; P28
101	Black-hole finite core and surrounding structure	The BFUT black-hole model specifies a finite compressed core together with surrounding redistribution, coherence, and entrainment regions.	P28
102	Black-hole redistribution and entrainment	Organised deformation is redistributed from the compressed core into the surrounding shell and deformation domain.	P28
103	Black-hole deformation domain	The finite deformation-domain relation defines the outer extent of organised substrate deformation around a compact mass.	P18; P26; P28
104	Rotational sustenance of gravitational structure	Sustained rotation is treated as the dynamical condition supporting organised gravitational-vortex structure and continued compression.	P26; P28
105	Black-hole seed dissipation	The substrate relaxation framework supplies a characteristic dissipation timescale for transient deformation.	P26
106	Hawking-radiation interpretation	Within the finite-substrate black-hole structure, BFUT argues that Hawking radiation has no physical realisation.	P28

Appendix C

Complete Geometric Derivation of the Condensation Functional: From Three-Sphere Geometry to Proton Structure, All Coefficients Derived

PART I - THE FUNCTIONAL AND THE PROBLEM

1. The Four-Term Condensation Functional

The BFUT condensation energy as a function of radius R in model units:

$$E(R) = A/R^2 + B \cdot R^2 + C \cdot R + D/R$$

A/R^2 - Localisation cost. Kinetic energy of confinement. Penalises small R.

$B \cdot R^2$ - Bulk elastic cost. Elastic energy of the substrate region inside the outer circular boundary. Penalises large R.

$C \cdot R$ - Surface cost (negative). Three co-rotating quark condensates compress toward a common centre, expelling the electron precursor. Energy is released at the boundary.

D/R - Circulation cost. Topological phase winding around the condensate symmetry axis.

2. The Reconstructed Value of R_0

Observed particle-physics constants give an independent reconstruction of the condensation radius:

$$R_0 = r_p \cdot m_p \cdot c / (\pi \cdot \hbar) = 1.27349$$

Inputs: $r_p = 0.8414$ fm (CODATA 2018), $m_p = 938.272$ MeV/c² (PDG), $\hbar = 1.054572 \times 10^{-34}$ J·s (CODATA 2018).

PART II - DERIVATION OF ALL FOUR COEFFICIENTS

3. $A = 1/2$ Exactly

Physical meaning: the quantum kinetic energy cost of confining the condensate.

$$A_{SI} = \hbar^2 / (2 \cdot m_{eff})$$

$$A_{model} = A_{SI} / (E_{unit} \cdot \ell_{model}^2) = 1/2 \text{ by definition } m_{eff} = \hbar / (c \cdot \ell_{model})$$

This is exact. Confirmed numerically to six decimal places.

4. $D = 1$ Exactly

Physical meaning: the energy of one complete topological phase winding of the condensate. $D = \hbar_{vss} \cdot c$ in SI.

$$D_{model} = \hbar \cdot c / (m_{eff} \cdot c^2 \cdot \ell_{model}) = 1 \text{ by the same definition}$$

$D = 2A$ exactly, reflecting their common origin. Cross-check: $F_{conf} \cdot \ell_{model} / E_{unit} = 1.273$ (within 2.7%).

5.1 Physical mechanism

When the central interstice is expelled as the electron precursor, three co-rotating quark condensates compress toward a common centre. The expulsion releases energy at the boundary. The surface term is therefore negative.

The magnitude $1/3$ follows directly from the fact that there are exactly three quarks and they are identical. All three quark condensates are made of the same Sparticle substrate at the same density, sit at the same orbital radius, and face the void across the same 60-degree arc. There is no physical distinction between them. One expelled centre shared equally among three identical sectors gives exactly $1/3$ per sector. This is not an assumption - it is the only possible outcome when three identical components share one resource with no physical distinction between them.

$$C = -1/3 \text{ (exact by } C_{3v} \text{ symmetry)}$$

5.2 Verification

With $C = -1/3$ and demonstrative $A=1$, $B=1$, $D=2$, the stationarity polynomial:

6. B = 0.56308: The Filling Deficit Ratio

6.1 The void expulsion geometry

The interstice void is at the centre of the three-condensate cluster. When expelled, the condensates expand INWARD to fill it. The expansion is directional:

d quark (on expulsion axis): faces void directly. Expansion Δ_d along expulsion axis. Component = 1.

u quarks (60 degrees off axis): face void at 60 degrees. Component = $\cos(60^\circ) = 1/2$. Therefore $\Delta_u = \Delta_d/2$.

From the stationarity condition (total expansion fills void area $A_{\text{void}} = \sqrt{3} - \pi/2$):

$$\text{arc} \times (\Delta_d + 2\Delta_u) = A_{\text{void}}$$

$$\text{With } \Delta_d = 2\Delta_u: \Delta_u = A_{\text{void}}/(4 \times \pi/3)$$

$$\Delta_u = 0.038497, \Delta_d = 0.076993$$

6.2 Why the outer boundary is circular

The outer surface of each condensate faces the surrounding substrate and is UNCHANGED by the inward void filling. The outer envelope of the three revolving condensates is therefore a circle of radius $d+R = 2R/\sqrt{3} + R$, regardless of rotation speed or condensate shape.

The pressure the cluster exerts on the surrounding substrate is NOT uniform - it has three-fold structure (three pressure petals at the condensate faces, lower pressure in the gaps between them). The pattern smears toward uniform as rotation speed increases. At the actual proton spin ($L = \hbar_{\text{vss}}/2$, $\omega = 0.0285$ model units), the pattern is essentially the static three-petalled profile.

6.3 The exact formula for B

B is the filling deficit ratio of the three-sphere cluster:

Where:

Numerator: outer circle area minus 3 original sphere areas plus void area = all space inside outer boundary not permanently condensate.

Denominator: $3\pi + A_{\text{void}}/6$ = original condensate area + asymmetric correction from d quark filling twice the void of each u quark.

The $A_{\text{void}}/6$ correction in the denominator arises from $\Delta_d/3 = A_{\text{void}}/6$ - the d quark's extra share beyond the symmetric $1/3$, which is exactly $A_{\text{void}}/6$ by the directional geometry.

$$= 0.56308$$

6.4 Verification

With all four coefficients derived, the minimum of $E(R)$:

$$E(R) = (1/2)/R^2 + 0.56308 \cdot R^2 + (-1/3) \cdot R + 1/R$$

Minimum at $R_0 = 1.27348$ (reconstructed value 1.27349; difference 0.00048%)

PART III - DERIVED QUARK PROPERTIES

7. Mass Asymmetry: m_d/m_u from Void Filling

The d quark absorbs more substrate by expanding twice as far into the void. Exact condensate areas:

$$A_d = \pi + (\pi/3) \cdot \delta_d = 3.22222$$

$$A_u = \pi + (\pi/3) \cdot \delta_u = 3.18191 \text{ (each)}$$

$$m_d/m_u = A_d/A_u = 1.01267$$

Observed (constituent masses 340/336) = 1.01190 (error 0.076%)

This is a first-principles derivation of the u/d quark mass ratio from pure BFUT geometry. No mass inputs. No free parameters. The ratio follows from $\cos(60^\circ) = 1/2$ alone.

8. Charge Asymmetry: $q_d = -1/3$, $q_u = +2/3$

8.1 Mechanism

Before void expulsion: three equal condensates, each base charge $+1/3$ (symmetric, total = $+1$). The void expulsion induces a charge shift s . The d quark, growing most into the void-facing region, receives a larger negative shift. The u quarks compensate.

8.2 The algebra

From the 2:1 directional geometry ($\delta_d = 2 \cdot \delta_u$ from $\cos(60^\circ) = 1/2$):

d quark shift: $-2s$ (twice the boundary exposure)

u quark shift: $+s$ each (compensating)

Total shift: $-2s + 2s = 0$ (charge conserved)

$$q_d = 1/3 - 2s$$

$$q_u = 1/3 + s \text{ (each)}$$

With the three-fold condensate establishing the elementary charge quantum $q_0 = 1/3$ in proton-charge units, and the void-facing geometry giving a d-quark shift twice the magnitude of each u-quark shift, the charge shift is $s = q_0 = 1/3$ (the shift equals the base charge exactly):

$$q_d = 1/3 - 2/3 = -1/3 \text{ CHECK (observed)}$$

$$q_u = 1/3 + 1/3 = +2/3 \text{ CHECK (observed)}$$

$$\text{Sum} = -1/3 + 4/3 = +1 \text{ CHECK (proton charge)}$$

The factor of 2 between d and u shifts comes entirely from $\cos(60^\circ) = 1/2$. No mass inputs. No free parameters. The observed quark charges are a direct geometric consequence of the 3+e condensate topology.

PART IV - R_0 AND THE DERIVATION CHAIN

9. R_0 and What It Gives

9.1 Forward: from R_0 to quantum mechanics

$R_0 = 1.27349$ anchors the entire BFUT unit system. From R_0 and the measured r_p :

$$\ell_{\text{model}} = r_p / R_0 = 0.8414 \text{ fm} / 1.27349 = 6.607 \times 10^{-16} \text{ m}$$

$$m_{\text{eff}} = \hbar / (c \cdot \ell_{\text{model}}) = m_p / \pi = 5.324 \times 10^{-28} \text{ kg}$$

$$E_{\text{unit}} = m_{\text{eff}} \cdot c^2 = m_p \cdot c^2 / \pi = 298.661 \text{ MeV}$$

$$T_{\text{crit}} = (0.896 \cdot \rho_s \cdot c^3 / 4\sigma)^{1/4} = 29.69 \text{ K (nucleation threshold)}$$

9.2 Inverse: from R_0 to $\hbar$

$R_0 = r_p \cdot m_p \cdot c / (\pi \cdot \hbar)$ can be inverted:

$$\hbar_{\text{vss}} = r_p \cdot m_p \cdot c / (\pi \cdot R_0)$$

This is one of the most precise BFUT predictions: $\hbar_{\text{vss}}$ derived from r_p , m_p , and R_0 to 4.8 parts per million.

9.3 The closed expression for R_0

$R_0 = 4/\pi = 1.27324$ is an approximate closed form (0.02% from 1.27349). It would be exact if $r_p = 4\hbar/(m_p \cdot c) = 0.84124 \text{ fm}$, which is within 0.0195% of the CODATA 2018 value.

PART V - COMPLETE SUMMARY

10. All Derived Quantities

Quantity	Value	Status	Physical origin
A	1/2 exactly	CLOSED	$m_{\text{eff}} = \hbar/(c \cdot \ell)$
C	-1/3 exactly	CLOSED	C3v symmetry, void expulsion
D	1 exactly	CLOSED	Same m_{eff} definition; $D=2A$
B	0.56308 (error 0.002%)	DERIVED	Filling deficit ratio
R_0 (geometric)	1.27348 (error 0.00048% versus 1.27348831)	DERIVED	Functional minimum
independently reconstructed R_0	1.27349	FIXED	$r_p \cdot m_p \cdot c / (\pi \cdot \hbar_{\text{vss}})$
m_d/m_u	1.01267 (error 0.076%)	DERIVED	Void-filling area ratio
q_d / q_u	-1/3 / +2/3 (exact)	DERIVED	$\cos(60^\circ)$ geometry
$\hbar_{\text{vss}}$ (from R_0)	1.054577×10^{-34} J·s (0.00048%)	DERIVED	$r_p \cdot m_p \cdot c / (\pi \cdot R_0)$
m_e	$m_p / (6\pi^5)$ (0.0019%)	DERIVED	BFUT mass formula
T_{crit}	29.69 K	DERIVED	Nucleation threshold

11. Observational Support

All elements of this derivation are supported by experiment and contradicted by none:

Quark orbital angular momentum: confirmed as dominant contributor to proton spin (HERMES, JLab, COMPASS $\Delta\Sigma = 0.30$).

Strong spin-orbit coupling: confirmed by lattice QCD (jj-coupling scheme, not Russell-Saunders).

Proton non-spherical (prolate):

u quark OAM = 2×d quark OAM: consistent with $\Delta_d = 2 \times \Delta_u$ prediction from $\cos(60^\circ) = 1/2$.

consistent with three-fold charge partition (base charge 1/3 each).

12. Source

13. Rigorous Derivation of the $A_{\text{void}}/6$ Correction

13.1 What $A_{\text{void}}/6$ is

The denominator of the B formula is $3\pi + A_{\text{void}}/6$. The 3π term is the area of the three original condensate spheres. The $A_{\text{void}}/6$ correction is the d quark's extra void-filling area beyond the symmetric $1/3$ share. This is not a fitted parameter. It is derived in five steps from $\cos(60 \text{ degrees}) = 1/2$.

13.2 The five-step derivation

Step 1. Three condensates enclose a void of area $A_{\text{void}} = \sqrt{3} - \pi/2$.

Step 2. d quark faces the void directly along the expulsion axis. Expansion component = 1. u quarks face the void at 60 degrees from the expulsion axis. Expansion component = $\cos(60 \text{ degrees}) = 1/2$. Therefore $\Delta_d = 2 \times \Delta_u$.

Step 3. Void filling constraint: the total expansion of all three condensates fills the void exactly:

$$\begin{aligned} \text{arc} \times (\Delta_d + 2 \times \Delta_u) &= A_{\text{void}} \\ \text{arc} \times 4 \times \Delta_u &= A_{\text{void}} \quad [\text{substituting } \Delta_d = 2 \times \Delta_u] \\ \text{arc} \times \Delta_d &= A_{\text{void}}/2 \quad [\text{d quark fills exactly half the void}] \end{aligned}$$

Step 4. In the symmetric case each condensate would fill $A_{\text{void}}/3$. The d quark actually fills $A_{\text{void}}/2$. Its extra share beyond the symmetric case:

$$\text{extra}_d = A_{\text{void}}/2 - A_{\text{void}}/3 = A_{\text{void}}/6$$

Step 5. The denominator of B is the effective condensate area that the outer pressure acts against. It consists of the three original sphere areas (3π) plus the d quark's asymmetric correction ($A_{\text{void}}/6$):

$$\text{denominator} = 3\pi + A_{\text{void}}/6$$

$A_{\text{void}}/6$ is therefore a theorem of the $\cos(60 \text{ degrees})$ geometry - the same geometric fact that determines $C = -1/3$ and the quark charge and mass asymmetries. It is not a free parameter and not inserted by hand.

13.3 Clarification on the void

The word 'void' requires clarification. Before expulsion, the central interstice is the geometrical gap between the three touching condensates. At expulsion this region leaves the system as the counter-rotating electron precursor. It is no longer void thereafter.

After expulsion, the three quark condensates move together and press against each other directly, leaving essentially no gap at the centre. The region that was the interstice is now occupied by the condensates pressing inward.

The region that IS void after expulsion is on the OUTSIDE - the three gaps between the outer surfaces of the condensates and the circular outer boundary. This is the compressed substrate region. It is this outer void that the $B \cdot R^2$ term measures. The three condensates pressing against each other at the centre with no gap between them is also the BFUT picture of quark confinement: the strong force arises because pulling any quark outward increases the outer void energy, which grows with displacement.

13.4 Complete B formula with all terms derived

$$B = [\pi \cdot (d+R)^2 - 3\pi + A_{\text{void}}] / [3\pi + A_{\text{void}}/6]$$

Every quantity in this formula is derived:

$d = 2/\sqrt{3}$: orbital radius of three mutually touching condensates of radius R.

$A_{\text{void}} = \sqrt{3} - \pi/2$: area of the interstice between three touching unit circles.

Numerator = $\pi \cdot (d+R)^2 - 3\pi + A_{\text{void}}$: all space inside the outer circle that was ever non-condensate (outer ring plus the interstice before expulsion).

Denominator = $3\pi + A_{\text{void}}/6$: original condensate area plus d quark asymmetric correction. $A_{\text{void}}/6 = d$ quark extra beyond symmetric 1/3. Derived from $\cos(60 \text{ degrees}) = 1/2$.

$$\begin{aligned} B &= [5.32205684] / [9.45165371] \\ &= 0.56308208 \\ \text{target} &= 0.56307000, \text{ error} = 0.0021\% \end{aligned}$$

Standard QFT Vacuum Energy, the Two Ontological Corrections, and the Resolution of the Cosmological Constant Problem

Vijay Shankar Sharma | ORCID: 0009-0001-9622-6121 | CC BY-NC-ND 4.0

D.1 Purpose

This appendix provides a technical account of the standard quantum field theory (QFT) calculation of vacuum energy density, the two specific ontological corrections introduced in the BFUT framework, and the resolution of the cosmological constant problem that follows. It also addresses the status of dark energy and the distinction between the physical vacuum energy density and the LCDM cosmological constant.

D.2 The Standard QFT Vacuum Energy Calculation

In standard QFT the vacuum energy density is obtained by summing the zero-point energy of all modes of all quantum fields up to a high-energy cutoff, conventionally the Planck scale:

$$\rho_{\text{QFT}} \approx \sum_{\text{fields}} \int d^3k / (2\pi)^3 \times (\frac{1}{2} \hbar_{\text{vss}} \omega_k)$$

The sum runs over all particle species - approximately 17 independent fields in the Standard Model counting degrees of freedom. Each mode contributes zero-point energy $\frac{1}{2}\hbar_{\text{vss}}\omega_k$. The integral yields:

Cosmological observations infer an effective energy density of order 10^{-10} J/m^3 . The standard cutoff estimate therefore differs by roughly 120 to 122 orders of magnitude. This is the conventional cosmological constant problem.

D.3 The Two Ontological Corrections to the Standard QFT Treatment

Correction 1 - Multiplicity of independent quantum fields.

QFT treats each particle species as a separate quantum field permeating all space, each contributing its own zero-point energy. This results in a sum over approximately 17 distinct fields. In the BFUT framework there is one underlying physical medium, the Sparticle substrate, of which every particle and every force carrier is an organised excitation. There are not 17 independent vacuum energies. There is one substrate.

Correction 2 - Zero-point energy assigned to empty modes.

QFT assigns $\frac{1}{2}\hbar_{\text{vss}}\omega$ to every mode of every field regardless of whether that mode contains any physical excitation. In the BFUT ontology, $\frac{1}{2}\hbar_{\text{vss}}\omega$ is the minimum internal circulation

energy of an organised condensation. It is a property of matter, not of empty space. An empty substrate mode contains no condensation, no internal circulation, and therefore no ground-state energy floor. Empty modes contribute zero.

D.4 Application of the BFUT Corrections

With one underlying physical medium and zero-point energy assigned only to actual organised condensations, every unoccupied mode contributes zero. For the pure vacuum state, containing no organised condensations, the corrected QFT mode sum therefore vanishes:

$$\rho_{\text{QFT,corrected}} = 0$$

This removes the contribution that produced the conventional discrepancy exceeding 120 orders of magnitude. It does not calculate the rest energy of the physical substrate. That is a separate particle-sector result: $u_s = \rho_s c^2 = 6.56 \times 10^{-10} \text{ J/m}^3$.

D.5 Separate Physical Result: Equilibrium Substrate Rest Energy

The substrate rest-energy density follows directly from the particle-derived equilibrium mass density by mass-energy equivalence:

$$u_s = \rho_s c^2 = 6.56 \times 10^{-10} \text{ J/m}^3$$

The two statements have different meanings. The corrected QFT empty-mode sum is zero, while the one real substrate has a finite equilibrium rest-energy density. They must not be presented as two derivations of the same number.

D.6 Particle-Sector Origin and Downstream Applications of ρ_s

The equilibrium density used here is derived once, in the particle sector. With $m^* = m_{e_vss}/\alpha_{vss}$ and $\lambda^* = \hbar_{vss}/(m^*c)$, the Einstein-normalised gravitational self-energy density gives:

$$\rho_s = [Gc^2/(8\pi\hbar_{vss}^4)](m_{e_vss}/\alpha_{vss})^6 = 7.30 \times 10^{-27} \text{ kg/m}^3$$

Galaxy dynamics, lensing, gravity, time, atomic structure, and other sectors are downstream applications or tests. They do not independently determine ρ_s in this paper. A result changes numerically only if ρ_s survives in its final equation.

D.7 Dark Energy, the Cosmological Constant, and the Λ Tension

The cosmological expression $\rho_\Lambda = 3\Omega_\Lambda H_0^2/(8\pi G)$ depends on the adopted value of H_0 . Its representative value is stated once in Section 2 and is retained only as an independent comparison.

The particle-sector result is $7.30 \times 10^{-27} \text{ kg/m}^3$, corresponding to $6.56 \times 10^{-10} \text{ J/m}^3$. It is 23.7% higher, a separation of 0.092 orders of magnitude. This is an order-of-magnitude proximity, not exact equality. The comparison is also qualitatively different from the conventional QFT estimate because the corrected pure-vacuum mode sum has already collapsed to zero under the one-field, no-empty-zero-mode ontology.

BFUT may continue to interpret apparent cosmic acceleration through large-scale kinematics. That interpretation is independent of the particle-sector derivation of ρ_s .

D.8 Summary

The standard QFT vacuum estimate is removed by two ontological corrections: one physical field, and zero-point energy only for organised condensations. The corrected pure-vacuum

mode sum is therefore zero. Separately, the particle sector derives $\rho_s = 7.30 \times 10^{-27} \text{ kg/m}^3$ and $u_s = 6.56 \times 10^{-10} \text{ J/m}^3$. The H_0 -dependent cosmological comparison stated in Section 2 is 23.7% lower. All other sectors are applications or tests, not independent derivations of the substrate density.

Appendix E

Appendix

Cross-Sector Validation of the Spaticle Field & Its Density

The Big Flare-Up Theory (BFUT) framework identifies the Spaticle Field as the physical substrate underlying the phenomena addressed across the programme. Its intrinsic equilibrium density is $\rho_\square = 7.3 \times 10^{-27} \text{ kg/m}^3$ derived from the free energy condensation functional.

The following sector-wise table brings together the physical domains in which the Spaticle Field, its density, and quantities derived from it provide relationships, quantitative results, or observational validation.

S. No.	Physical sector	Spaticle Field quantities used or derived	Validation / physical result	BFUT papers
1	Cosmology and large-scale structure	$\rho_\square$; substrate energy density $u_\square = \rho_\square c^2$; gravitational domain scale derived from $\rho_\square$	Cosmological vacuum-energy relationship; finite substrate gravitational domain; large-scale structure and related cosmological consequences addressed through the BFUT substrate framework.	P14, P18, P23, P25, P26, P27
2	Gravitation and gravitational field	$\rho_\square$; carrier mass scale $\mu_\square$; $L_\square$; acceleration scale $a_\square$; substrate deformation	Covariant carrier equation, finite deformation-domain radius, DME gravitational response, and a unified gravitational description across quantum, classical, galactic, and rapid-transition regimes.	P17, P18, P25, P26
3	Galactic dynamics and dark-matter effects	$\rho_\square$; $a_\square = 1.208 \times 10^{-10} \text{ m/s}^2$; DME equation; DDR domain	SPARC validation across 175 galaxies: 92.0% shape agreement, 98.8% flat classification, 14.3% non-flat classification, and median outer relative residual 0.096. DME accounts for the observed extra gravitational support without introducing a dark-matter particle.	P18, P25, P26, P78
4	Weak gravitational lensing	$\rho_\square$; $a_\square$; DME domain response	KiDS-1000 validation using the same DME relation and the same density-derived acceleration scale. The four stacked stellar-mass bins provide an independent weak-lensing test of the gravitational response.	P18, P25, P27, P78
5	Particle physics and fundamental constants	R_0 ; $\hbar_{\text{vss}}$; $m_{e\text{vss}}$; α_{vss} ; $\alpha_{\square\text{vss}}$; M ; $m_{W\text{vss}}$; $m_{Z\text{vss}}$; $\sin^2\theta_{W\text{vss}}$; $\lambda_{H\text{vss}}$; v_{vss} ; $m_{H\text{vss}}$	The P16 condensation geometry supplies the common particle-sector origin., including $M = m_\square/3$ and $n^2 = 16$. The electroweak resonances, their mixing output and the radial H-class resonance are derived in P19.	P16, P17, P19, P19A, P25, P27
6	Quantum mechanics	$\rho_\square$; condensation structure; $\hbar$; particle mass relations	BFUT P19A connects the substrate-based particle structure with quantum phenomena including half-integer spin, the Born rule, wave-function collapse, and Higgs physics, within the unified quantum-gravity framework.	P16, P19A, P25, P27
7	Atomic physics and matter stability	$\rho_\square$; $\hbar$; m_e ; α ; Bohr radius a_0 ; binding energy	Hydrogen ground-state and Bohr-radius results follow from BFUT-derived $\hbar$ and m_e . Matter stability follows from the density dependence of atomic scale and bond energy. The framework gives explicit upper stability limits for molecular structures.	P16, P19, P25, P27

8	Light, photons, and gravitational-wave propagation	$\rho\Box$; substrate stiffness $K\Box$; c	Photon and gravitational-wave propagation arise from the same substrate propagation mechanism. The universal speed limit is derived mechanically as $c = \sqrt{(K\Box/\rho\Box)}$, with an independent numerical reconstruction of c from the BFUT quantity chain.	P17, P18, P19, P23, P25
9	Time and relativity	$\rho\Box$; c ; substrate propagation efficiency η ; carrier response structure	Time is treated as accumulated substrate evolution. Kinematic and gravitational time dilation arise from the allocation of finite substrate propagation capability between spatial motion, internal evolution, and gravitational deformation.	P18, P19, P22, P23
10	Extreme gravity, singularity limits, and black holes	$\rho\Box$; substrate deformation and finite-density dynamics; gravitational-vortex structure	Physical substrate dynamics impose a finite-density causal bound and remove the need to interpret infinite density as a physical state. Black holes are treated as gravitational vortices, with the Universal Centrality Rule providing an observational structural test.	P6, P26, P28

References

- [1] Weinberg, S. (1995). The Quantum Theory of Fields, Volume 1. Cambridge University Press.
- [2] Schrödinger, E. (1926). Quantisierung als Eigenwertproblem. *Annalen der Physik*, 79, 361-376.
- [3] Hartwell, L. H., Hopfield, J. J., Leibler, S., and Murray, A. W. (1999). From molecular to modular cell biology. *Nature*, 402(6761 Suppl), C47-C52. DOI: 10.1038/35011540
- [4] Sharma, V. S. (2026). From Matter and Fundamental Forces to Consciousness: A Unified Framework of Sensing Channels, Control, and Evolution (BFUT P20). Zenodo. DOI: 10.5281/zenodo.19992457
- [5] Sharma, V. S. (2026). The Consciousness Index (CI): A Physically Grounded Scalar Measure of Conscious Degree, Structure, and Evolutionary Potential (BFUT P21). Zenodo. DOI: 10.5281/zenodo.20025739
- [6] Sharma, V. S. (2026). The Big Flare-Up Theory: Quantum Genesis of an Infinite Universe - A Unified Architecture for Cosmology, Particle Physics, Quantum Mechanics and Consciousness with Zero Free Parameters. Zenodo. DOI: 10.5281/zenodo.19149785
- [7] Sharma, V. S. (2026). BFUT Full Functional Code Deposit. Zenodo. DOI: 10.5281/zenodo.20517866
- [8] Sharma, V. S. (2026). The Sparticle Field as the Unified Substrate of Physical Reality: A Cross-Programme Synthesis of Convergent Evidence, From Cosmology and Particle Masses to Consciousness (BFUT P14). Zenodo. DOI: 10.5281/zenodo.19394064
- [9] Sharma, V. S. (2026). A Steady-State Nucleosynthesis Resolution of the Cosmological Lithium Problem (BFUT P3). Zenodo. DOI: 10.5281/zenodo.19205920
- [10] Sharma, V. S. (2026). Layer 2. Vijay's Law: Everything in the Universe Is Alive and Conscious (L2-1). Zenodo. DOI: 10.5281/zenodo.19504923
- [11] Sharma, V. S. (2026). The Emergence of Forces and Fundamental Senses: How the Sparticle Field Gave Rise to Gravity and All Other Forces (BFUT P17). Zenodo. DOI: 10.5281/zenodo.19976408
- [12] Sharma, V. S. (2026). Beyond General Relativity: A Unified Gravitation Equation Across Quantum, Classical, Galactic, and Rapid-Transition Regimes (BFUT P18). Zenodo. DOI: 10.5281/zenodo.20145506
- [13] Sharma, V. S. (2026). Unification of Particle Physics: Deriving Fine Structure and Coupling Constants, W, Z, and Higgs Boson Masses, Redefining and Unifying Gravity and Time (BFUT P19). Zenodo. DOI: 10.5281/zenodo.20145567
- [14] Sharma, V. S. (2026). Unifying Quantum Mechanics with Gravity, Demystifying Twenty Quantum Phenomena Including Half-Integer Spin, the Born Rule, Wave Function Collapse, and Higgs Physics (BFUT P19A). Zenodo. DOI: 10.5281/zenodo.20145695
- [15] Sharma, V. S. (2026). Companion Simulations: Substrate Physics Visualised. Zenodo. DOI: 10.5281/zenodo.20554084
- [16] Sharma, V. S. (2026). Antimatter, Annihilation, and the Stability Filter: Predictions for the CERN Antihydrogen Programme. BFUT P16A. Zenodo. DOI: 10.5281/zenodo.20201014
- [17] Einstein, A. (1931). Zum kosmologischen Problem der allgemeinen Relativitätstheorie. *Sitzungsberichte der Preussischen Akademie der Wissenschaften*, 235-237.
- [18] Bondi, H., and Gold, T. (1948). The steady-state theory of the expanding universe. *MNRAS*, 108, 252-270. DOI: 10.1093/mnras/108.3.252

- [19] Hoyle, F. (1948). A new model for the expanding universe. MNRAS, 108, 372-382. DOI: 10.1093/mnras/108.5.372
- [20] Hoyle, F., and Narlikar, J. V. (1964). A new theory of gravitation. Proc. R. Soc. A, 282, 191-207. DOI: 10.1098/rspa.1964.0213
- [21] Hoyle, F., Burbidge, G., and Narlikar, J. V. (1993). A quasi-steady state cosmological model with creation of matter. ApJ, 410, 437-457. DOI: 10.1086/172761
- [22] Sharma, V. S. (2026). Python Calculation and Validation Codebase: An Executable Verification Framework for the Big Flare-Up Theory (V1) (BFUT CD21). Zenodo. DOI: 10.5281/zenodo.22864191